

A) Modified minimum jerk model

Find the trajectory $(x(t), y(t))_{t \in [0,1]}$ that minimizes

$$\int_0^1 \overline{x}^2 + \overline{y}^2 + \gamma \left(\frac{d}{dt} \left(\sqrt{\dot{x}^2 + \dot{y}^2}\right)\right)^2$$

subject to the constraints

$$\begin{aligned} x(0) &= x_0, \ \dot{x}(0) = v_0^x, \ \ddot{x}(0) = a_0^x, \ x(1) = x_1, \ \dot{x}(1) = v_1^x, \ \ddot{x}(1) = a_1^x \\ y(0) &= y_0, \ \dot{y}(0) = v_0^y, \ \ddot{y}(0) = a_0^y, \ y(1) = y_1, \ \dot{y}(1) = v_1^y, \ \ddot{y}(1) = a_1^y \end{aligned}$$

$$y(0) = y_0, \ \dot{y}(0) = v_0^y, \ \ddot{y}(0) = a_0^y, \ y(1) = y_1, \ \dot{y}(1) = y_1$$

where the x_0, v_0^x, \ldots were set to the average experimental values. Approximated solutions in the subspace of polynomials of degrees ≤ 7 .

B) Optimal feedback control model

- stochastic version of the previous modified minimum jerk (MMJ) model
- based on a simplified optimal feedback control scheme [Hoff & Arbib 1993, Todorov & Jordan 2002]

Random perturbation Initially planned

> Re-planned trajectory

trajectory



Open-loop and feedback processes in the formation of trajectories during visual and nonvisual locomotion in humans

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Models

Target uncertainty (nonvisual condition)



- **Algorithm 1** 1. Discretize the movement into n steps ($10 \le n \le 20$ depending on the target) 2. At each step i, compute first a MMJ trajectory between the current state s(i) (position, velocity, acceleration at time i) and the final state. This is the "initially planned trajectory"
- 3. Add a random perturbation to s'(i+1), the state of the "initially planned trajectory" at step i+1. This yields set to be an increasing function of the absolute value of the curvature
- 4. Compute the MMJ between s(i) and s(i+1). This yields the actual trajectory between i and i+15. Repeat from step 2

the target in the NV condition

C) Results

Good reproduction of the typical features of actual trajectories In particular:

- VI: bump-shaped variability profile
- NV: variability first increases linearly, then decreases near the end



