Shape and spin determination of Barbarian asteroids

M. Devogèle^{1,2}, P. Tanga², P. Bendjoya², J.P. Rivet², J. Surdej¹, J. Hanuš^{2,3}, L. Abe², P. Antonini⁴, R.A. Artola⁵, M. Audejean^{4,7}, R. Behrend^{4,8}, F. Berski⁹, J.G. Bosch⁴, M. Bronikowska⁶, A. Carbognani¹², F. Char¹⁰, M.-J. Kim¹¹, Y.-J. Choi¹¹, C.A. Colazo⁵, J. Coloma⁴, D. Coward¹³, R. Durkee¹⁴, O. Erece^{15,16}, E. Forne⁴, P. Hickson¹⁷, R. Hirsch⁹, J. Horbowicz⁹, K. Kamiński⁹, P. Kankiewicz¹⁸, M. Kaplan¹⁵, T. Kwiatkowski⁹, I. Konstanciak⁹, A. Kruszewki⁹, V. Kudak^{19,20}, F. Manzini^{4,21}, H.-K. Moon¹¹, A. Marciniak⁹, M. Murawiecka²², J. Nadolny^{23,24}, W. Ogłoza²⁵, J.L Ortiz²⁶, D. Oszkiewicz⁹, H. Pallares⁴, N. Peixinho^{10,27}, R. Poncy⁴, F. Reyes²⁸, J.A. de los Reyes²⁹, T. Santana–Ros⁹, K. Sobkowiak⁹, S. Pastor²⁹, F. Pilcher³⁰, M.C. Quiñones⁵, P. Trela⁹, and D. Vernet²

(Affiliations can be found after the references)

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ABSTRACT

Context. The so-called Barbarian asteroids share peculiar, but common polarimetric properties, probably related to both their shape and composition. They are named after (234) Barbara, the first on which such properties were identified. As has been suggested, large scale topographic features could play a role in the polarimetric response, if the shapes of Barbarians are particularly irregular and present a variety of scattering/incidence angles. This idea is supported by the shape of (234) Barbara, that appears to be deeply excavated by wide concave areas revealed by photometry and stellar occultations.

Aims. With these motivations, we started an observation campaign to characterise the shape and rotation properties of Small Main-Belt Asteroid Spectroscopic Survey (SMASS) type L and Ld asteroids. As many of them show long rotation periods, we activated a worldwide network of observers to obtain a dense temporal coverage.

Methods. We used light-curve inversion technique in order to determine the sidereal rotation periods of 15 asteroids and the convergence to a stable shape and pole coordinates for 8 of them. By using available data from occultations, we are able to scale some shapes to an absolute size. We also study the rotation periods of our sample looking for confirmation of the suspected abundance of asteroids with long rotation periods.

Results. Our results show that the shape models of our sample do not seem to have peculiar properties with respect to asteroids with similar size, while an excess of slow rotators is most probably confirmed. *Conclusions.*

Key words. asteroids – asteroid shape – asteroid rotation

1. Introduction

Shape modeling is of primary importance in the study of asteroid properties. In the last decades, ~ 1000 asteroids have had a shape model determined by using inversion techniques¹; most of them are represented by convex shape models. This is due to the fact that the most used technique when inverting the observed light-curves of an asteroid - the so-called light-curve inversion is proven to mathematically converge to a unique solution only if the convex hypothesis is enforced (Kaasalainen and Torppa 2001; Kaasalainen et al. 2001). At the typical phase angles observed for Main Belt asteroids, the light-curve is almost insensitive to the presence of concavities according to Durech and Kaasalainen (2003). Although the classical light-curve inversion process cannot model concavities, Kaasalainen et al. (2001) point out that the convex shape model obtained by the inversion is actually very close to the convex hull of the asteroid shape. Since the convex hull corresponds to the minimal envelope that contains the non-convex shape, the location of concavities corresponds to flat areas. Devogèle et al. (2015) developed the flat

surfaces derivation technique (FSDT) which considers flat surfaces on such models to obtain indications about the possible presence of large concavities.

Cellino et al. (2006) reported the discovery of the anomalous polarimetric behaviour of (234) Barbara. Polarisation measurements are commonly used to investigate asteroid surface properties and albedos. Usually, the polarisation rate is defined as the difference of the photometric intensity in the directions parallel and perpendicular to the scattering plane (normalised to their sum): $P_r = \frac{I_\perp - I_\parallel}{I_\perp + I_\parallel}$. It is well known that the intensity of polarisation is related to the phase angle, that is, to the angle between the light-source direction and the observer, as seen from the object. The morphology of the phase-polarisation curve has some general properties that are mainly dependent on the albedo of the surface. A feature common to all asteroids is a "negative polarisation branch" for small phase angles, corresponding to a higher polarisation parallel to the scattering plane. For most asteroids, the transition to positive polarisation occurs at an "inversion angle" of $\sim 20^{\circ}$. In the case of (234) Barbara, the negative polarisation branch is much stronger and exhibits an uncommonly large value for the inversion angle of approximately 30°. Other Barbarians were found later on (Gil-Hutton et al. 2008; Masiero and Cellino 2009; Cellino et al. 2014; Gil-Hutton et al. 2014; Bag-

Article number, page 1 of 23

¹ See the Database of Asteroid Models from Inversion Techniques (DAMIT) data base for an up-to-date list of asteroid shape models: http://astro.troja.mff.cuni.cz/projects/asteroids3D/

nulo et al. 2015; Devogèle et al. 2017), and very recently, it was discovered that the family of Watsonia is composed of Barbarians (Cellino et al. 2014).

Several hypotheses have been formulated in the past to explain this anomaly. Strong backscattering and single-particle scattering on high-albedo inclusions were invoked. Nearinfrared (NIR) spectra exhibit an absorption feature that has been related to the presence of spinel absorption from fluffytype Calcium-Aluminium rich Inclusions (CAIs) (Sunshine et al. 2007, 2008). The meteorite analogue of these asteroids would be similar to CO3/CV3 meteorites, but with a surprisingly high CAI abundance (~ 30%), never found in Earth samples. If this interpretation is confirmed, the Barbarians should have formed in an environment very rich in refractory materials, and would contain the most ancient mineral assemblages of the Solar System. This fact link, the explanation of the polarisation to the presence of high-albedo CAIs, is the main motivation for the study of Barbarians, whose composition challenges our knowledge on meteorites and on the mechanisms of the formation of the early Solar System.

The compositional link is confirmed by the evidence that all Barbarians belong to the L and Ld classes of the Small Main-Belt Asteroid Spectroscopic Survey (SMASS) taxonomy (Bus and Binzel 2002), with a few exceptions of the K class. While not all of them have a near-infrared spectrum, all Barbarians are found to be L-type in the DeMeo et al. (2009) NIR-inclusive classification (Devogèle et al. 2017).

However, the variety of polarimetric and spectroscopic properties among the known Barbarians, also suggests that composition cannot be the only reason for the anomalous scattering properties. In particular, Cellino et al. (2006) suggested the possible presence of large concavities on the asteroid surfaces, resulting in a variety of (large) scattering and incidence angles. This could have a non-negligible influence on the detected polarisation, but such a possibility has remained without an observational verification up to now.

Recent results concerning the prototype of the class, (234) Barbara, show the presence of large-scale concavities spanning a significant fraction of the object size. In particular, interferometric measurements (Delbo et al. 2009) and wellsampled profiles of the asteroid obtained during two stellar occultations indicate the presence of large-scale concave features (Tanga et al. 2015). Testing the shape of other Barbarians for the presence of concavities is one of the main goals of the present study, summarising the results of several years of observation. To achieve this goal, we mainly exploit photometry to determine the shape, to be analysed by the FSDT. We compare our results with the available occultation data (Dunham et al. 2016) in order to check the reliability of the inverted shape model, scale in size, and constrain the spin axis orientation. We also introduce a method capable of indicating if the number of available light-curves is sufficient to adequately constrain the shape model solution.

As we derive rotation periods in the process, we also test another evidence, rather weak up to now: the possibility that Barbarians contain an abnormally large fraction of "slow" rotators, with respect to a population of similar size. This peculiarity – if confirmed – could suggest a peculiar past history of the rotation properties of the Barbarians.

The article is organised as follows. In Sect. 2, we describe the observation campaign and the obtained data. Sect. 3 presents the approach that was followed to derive the shape models. A new method for analysing the shape model of asteroids is presented and tested on well-known asteroids. In Sect. 4, the characteristics

of some individual asteroids are presented as well as a general discussion about the main results of the present work. The incidence of concavities and the distribution of the rotation periods and pole orientations of L-type asteroids are presented. Finally Sect. 5 contains the conclusions of this work.

2. The observation campaigns

2.1. Instruments and sites

Our photometric campaigns involve 15 different telescopes and sites distributed on a wide range in Earth longitudes in order to optimise the time coverage of slowly rotating asteroids, with minimum gaps. This is the only strategy to complete light-curves when the rotation periods are close to 1 day, or longer, for ground-based observers.

The participating observatories (Minor Planet Center (MPC) code in parentheses) and instruments, ordered according to their geographic longitudes (also Tab. 1), are:

- the 0.8m telescope of Observatori Astronòmic del Montsec (OAdM), Spain (C65),
- the 1.04m "Omicron" telescope at the Centre Pédagogique Planète et Univers (C2PU) facility, Calern observatory (Observatoire de la Côte d'Azur), France (010),
- the 0.81m telescope from the Astronomical Observatory of the Autonomous Region of the Aosta Valley (OAVdA), Italy (B04),
- the 0.4m telescope of the Borowiec Observatory, Poland (187),
- the 0.6m telescope from the Mt. Suhora Observatory, Cracow, Poland,
- the 0.35m telescope from Jan Kochanowski University in Kielce, Poland (B02),
- the 1m Zadko telescope near Perth, Australia (D20),
- the 0.61m telescope of the Sobaeksan Optical Astronomy Observatory (SOAO), South Korea (345),
- the 0.7m telescope of Winer Observatory (RBT), Arizona, USA (648),
- the 0.35m telescope from the Organ Mesa Observaory (OMO), NM, USA (G50),
- the 0.6m telescope of the Southern Association for Research in Astrophysics (SARA), La Serena Observatory, Chile (807),
- the 0.35m telescope from the UBC Southern Observatory, La Serena Observatory, Chile (807),
- the 1.54m telescope of the Estación Astrofisica de Bosque Alegre (EABA), Argentina (821),
- the 1.5m telescope of the Instituto Astrofisica de Andalucia (IAA) in Sierra Nevada, Spain (J86),
- the 0.77m telescope from the Complejo Astron
 ømico de La Hita, Spain (I95).

All observations were made in the standard V or R band as well as sometimes without any filter. The CCD images were reduced following standard procedures for flat-field correction and dark/bias subtraction. Aperture photometry was performed by the experienced observers operating the telescopes, and the auxiliary quantities needed to apply the photometric inversion (lighttime delay correction, asterocentric coordinates of the Sun and the Earth) were computed for all the data.

The whole campaign is composed of 244 individual lightcurves resulting from approximatively 1400 hours of observation and 25000 individual photometric measurements of asteroids. All the new data presented in this work are listed in Table A1 of Appendix A.

Observat.	D	Longitude	Latitude	MPC	N _{lc}
	[m]			code	
OAdM	0.8	000°44′13"	42°01′28"	C65	16
C2PU	1.04	006°56′00"	43°45′00"	010	89
OAVdA	0.81	007°28'42"	45°47′23"	B04	16
Borowiec	0.4	016°52′48"	52°24′00"	187	41
Suhora	0.60	020°04′01"	49°34′09"	-	2
Kielce	0.35	020°39′24"	50°52′52"	B02	2
Zadko	1	115°42′49"	-31°21′24"	D20	9
SOAO	0.61	128°27'27"	36°56′04"	345	4
RBT	0.7	248°01′15"	31°42′00"	648	21
OMO	0.35	253°19′48"	32°17′46"	G50	11
SARA	0.6	289°11′47"	-30°10′10"	807	11
UBC	0.35	289°11′37"	-30°10′07"	807	15
EABA	1.54	295°27′25"	-31°35′46"	821	12
IAA	1.5	356°36′51"	37°03′47"	J86	5
LA HITA	0.77	356°48′50″	39°34′07″	I95	1

 Table 1. List of the observatories participating in the observation campaigns, with telescope aperture (D), position, and number of light-curves. A rather good longitude coverage was ensured.

In addition to these observations, we exploited light-curves published in the literature. For the most ancient light-curves, the APC (Asteroid Photometric Catalogue (Lagerkvist et al. 2001)) was used. The most recent ones are publicly available in the DAMIT database (Ďurech et al. 2010).

As explained in the following section, we also used sparse photometry following the approach of Hanuš et al. (2011, 2013). The selected data sets come from observations from the United States Naval Observatory (USNO)-Flagstaff station (International Astronomical Union (IAU) code 689), Catalina Sky Survey Observatory (CSS, IAU code 703 (Larson et al. 2003)), and Lowell survey (Bowell et al. 2014).

The already published data used in this work are listed in Table B1 of Appendix B.

2.2. The target sample

We coordinated the observation of 15 asteroids, selected on the basis of the following criteria:

- Known Barbarians, with a measured polarimetric anomaly;
- SMASS L or Ld type asteroids, exhibiting the 2 μm spinel absorption band;
- members of dynamical families containing known Barbarians and/or L-type asteroids: Watsonia (Cellino et al. 2014), the dispersed Henan (Nesvorný et al. 2015); Tirela (Mothé-Diniz and Nesvorný 2008), renamed Klumpkea in Milani et al. (2014).

Fig. 1 shows the location (red dots) in semi-major axis and inclination of the asteroids studied in this work. In general, Barbarians are distributed all over the main belt. The concentration in certain regions is a direct consequence of the identification of the Watsonia, Henan, and Tirela families. Future spectroscopic surveys including objects with a smaller diameter could better portray the global distribution.

For each of the 15 asteroids that have been targeted in this work, our observations have led to the determination of a new rotation period, or increase the accuracy of the previously known one. For eight of them, the light-curves dataset was sufficiently large to determine the orientation of the spin axis and a reliable convex shape model. Table 2 lists the class in the Tholen (Tholen 1984), SMASS (Bus and Binzel 2002; Mothé-Diniz and Nesvorný 2008) and Bus-Demeo (DeMeo et al. 2009; Bus 2009) taxonomies of the 15 asteroids observed by our network. Each known Barbarian from polarimetry is labelled as "Y" in the corresponding column. The number of the family parent member is given in the corresponding column. The bottom part of Table 2 gives the same information for asteroids not observed by our network, but included in this work to increase the sample.

3. Modelling method and validation of the results

3.1. Shape modelling

The sidereal rotation period was searched for by the light-curve inversion code described in Kaasalainen and Torppa (2001) and Kaasalainen et al. (2001) over a wide range. The final period is the one that best fits the observations. It is considered as unique if the chi-square of all the other tested periods is > 10% higher. In order to obtain a more precise solution, sparse data are also included in the procedure, as described by Hanuš et al. (2013). When the determination of a unique rotation period is possible, the pole solution(s) can be obtained. As is well known, paired solutions with opposite pole longitudes (i.e. differing by 180°) can fit the data equally well. If four or less pole solutions (usually two sets of two mirror solutions) are found, the shape model is computed using the best fitting pole solution.

The accuracy of the sidereal rotation period is usually of the order of 0.1 to 0.01 times the temporal resolution interval $P^2/(2T)$ (where P is the rotation period and T is the length of the total observation time span). For the typical amount of optical photometry we have for our targets the spin axis orientation accuracy for the light-curve inversion method is, in general, ~ 5°/ cos β for λ and ~ 10° for β (Hanuš et al. 2011).

All possible shapes were compared with the results derived from stellar occultations whenever they were available. The projected shape model on the sky plane is computed at the occultation epoch using the Ďurech et al. (2011) approach. Its profile is then adjusted, using a Monte-Carlo-Markov-Chain algorithm, to the extremes of the occultation chords.

With this procedure, the best absolute scale of the model is found, thus allowing us to determine the size of the target. For ease of interpretation, the absolute dimensions of the ellipsoid best fitting- the scaled shape model and the volume-equivalent sphere R_{eq} are computed.

In some cases, the result of stellar occultations also allows one to discriminate different spin axis solutions.

Eventually, the FSDT is used to analyse all the derived convex shape models. As this procedure depends on the presence of flat surfaces, we must ensure that the shape models are reliable. In fact, portions of the asteroid surface not sufficiently sampled by photometry, can also produce flat surfaces. We thus established the approach explained in the following section, allowing us to estimate the reliability of a shape derived by the light-curve inversion.

3.2. Shape validation by the bootstrap method

Our goal is to evaluate the reliability of shape model details, and to check if a set of light-curves provides a good determination of the spin parameters.

As mentioned above, the light-curve inversion process often provides several sets of spin parameters (rotation period and spin axis orientation) that fit the optical data equally well. In other



Fig. 1. Inclination versus semi-major axis plot of main-belt asteroids. The asteroids studied in this work are plotted as red circular dots, while the thinner blue dots represent the asteroid population as a whole.

cases, when only a few light-curves are available, the parameter set may converge with a single, but incorrect solution, often associated with an incorrect rotation period. We see below that the bootstrapping method detects such cases.

Our approach consists in computing the shape model that best fits a subset of light-curves, randomly selected among all those that are available for a given asteroid. By studying how the fraction of flat surfaces η_s evolves with the number of selected light-curves, we obtain a solid indication on the completeness of the data, that is, the need for new observations or not.

In more detail, we proceed as follows:

- First, a large number of light-curve samples is extracted from the whole data set. Each of these subsets may contain a number of light-curves n_l ranging from $n_l = 1$ to all those available ($n_l = N_{dl}$). Sets of sparse data are also included in the process and equal for all samples. In fact, the availability of a sparse data set is a necessary condition to apply the bootstrapping technique. Since shape models can sometimes be derived using sparse data only, they allow the inversion process to converge to a solution even for low values of n_l .
- The second step consists in deriving the shape model corresponding to all the light-curve samples generated in the previous step. The spin axis parameters found by using all the light-curves are exploited as initial conditions for each

inversion computation. If different sets of spin parameters are found with equal probability, the whole procedure is executed for each of them.

- Once all the shape models are determined, we apply the FSDT in order to find the best value of η_s for each shape model.
- The last step consists in determining the mean value and the dispersion of η_s corresponding to each subset group characterised by $n_l = 1, 2, 3, ..., N_{dl}$ light-curves.

An excess of flat surfaces is often interpreted as the qualitative indication that the available photometry does not constrain the shape model adequately. The addition of supplementary light-curves is then a necessary condition to improve the shape. In our procedure, we make the hypothesis that, as the number of light-curves increases, the η_s parameter decreases. In the process, the model converges to the convex hull of the real shape. Ideally, the only flat surfaces remaining should then correspond to concave (or really flat) topological features. Such a convergence should ideally show up as a monotonic decrease of η_s towards an asymptotic value for a large n_l . Here, we apply our procedure and show that our quantitative analysis is consistent with this assumption.

Devogèle et al.: Shape and spin determination of Barbarian asteroids

Asteroid	Tholen	SMASS	DM	Barbarian	Family
(122) Gerda	ST	L			
(172) Baucis	S	L		Y	
(234) Barbara	S	Ld	L	Y	
(236) Honoria	S	L	L	Y	
(387) Aquitania	S	L	L	Y	
(402) Chloe	S	Κ	L	Y	
(458) Hercynia	S	L		Y	
(729) Watsonia	STGD	L	L	Y	729
(824) Anastasia	S	L	L		
(980) Anacostia	SU	L	L	Y	
(1332) Marconia		Ld	L		
(1372) Haremari		L			729
(1702) Kalahari	D	L			
(2085) Henan		L	L		2085
(3844) Lujiaxi		L	L		2085
(15552) Sandashounkan					1400
(234) Barbara	S	Ld	L	Y	
(599) Luisa	S	Κ	L	Y	
(606) Brangane	TSD	Κ	L		606
(642) Clara	S	L			
(673) Edda	S	S	L		
(679) Pax	Ι	Κ	L	Y	
(1284) Latvia	Т	L			
(2448) Sholokhov		L	L		

Table 2. List of the targets observed by our network (upper part). Some targets that were not observed by us but discussed in this work were added in the lower part. The first column corresponds to the number and name of the considered asteroid. The columns Tholen (Tholen 1984), SMASS (Bus and Binzel 2002; Mothé-Diniz and Nesvorný 2008) and Bus-Demeo (DM) (DeMeo et al. 2009; Bus 2009) stand for the taxonomic class in these three types of taxonomy. The Barbarian column indicates whether or not the asteroid is considered as a Barbarian (Cellino et al. 2006; Gil-Hutton et al. 2008; Masiero and Cellino 2009; Bagnulo et al. 2015). Finally, the Family column indicates the number of the parent member of the family in which the asteroid is classified (606 for the Brangane, 729 for the Watsonia, 1400 for the Tirela/Klumpkea and 2085 for the Henan family).

We stress here that the number of possible subsets that can be extracted is potentially large, as it is given by the binomial coefficient $\binom{N}{k}$.

If the number of light-curves is below 14, all subsets are exploited. If there are additional light-curves, the number of possible combinations increases, but we do not generate more than 10,000 random subsets to limit the computation time. Our results show that this is not a limitation when the light-curve sample is very rich.

3.2.1. Test on (433) Eros

The bootstrap method was first tested on (433) Eros for which the shape is well known thanks to the images taken by the NEAR mission (Gaskell 2008). A large number of dense photometric light-curves (N = 134) is also available for this asteroid which allows us to derive an accurate shape model using light-curve inversion.

The data set of (433) Eros contains 134 dense light-curves and 2 sets of sparse data. Fig. 2 shows the average of the flat surface fraction (η_s) as a function of the number of dense lightcurves (N_{dl}) used for the shape modelling.

As expected (Fig. 2), the η_s versus N_{dl} curve (hereafter called the bootstrap curve) is monotonically decreasing. It is straightforward to verify that an exponential function $y = a \exp(-bx) + c$ is well suited to fit the bootstrap curve. In this expression the *c* parameter corresponds to the asymptotic value η_a , that is, the η_s



Fig. 2. Bootstrap curves for the asteroid (433) Eros

that would be detected if a very large number of light-curves was used. In the case of (433) Eros we find $\eta_a = 0.134$.

For a comparison to the "real" shape, we can take advantage of the detailed shape model of (433) Eros obtained by the analysis of the NEAR space probe images, obtained during the close encounter. For our goal, a low-resolution version (Gaskell 2008) is sufficient, and was used to check the result described above.

By taking the convex-hull (i.e. the smallest convex volume that encloses a non-convex shape), we obtain the shape model that, in an ideal case, the light-curve inversion should provide. In that specific case, the FSDT yields $\eta_a = 0.12$. This value is

within 6% of the value obtained by the bootstrapping method. This is a first indication that our approach provides a good approximation and can be used to evaluate the "completeness" of a light-curve set.

We may compare our result to the value corresponding to the complete set of N_{dl} available light-curves. In this case, $\eta_s = 0.18$, a much larger discrepancy (20%) with respect to the correct value. This result means that the convex shape model of (433) Eros (derived by photometry only) could probably be somewhat improved by adding new dense light-curves.

In the following sections, we apply this analysis to other objects for the evaluation of their shape as derived from the photometric inversion.

3.2.2. Sensitivity of the bootstrap method to the spin axis coordinates

The behaviour of the bootstrap curve (exponentially decreasing) is related to the choice of the correct spin axis parameters.

This property is illustrated on the asteroid (2) Pallas. Even though Pallas has not been visited by a space probe, its spin axis orientation and shape are well known thanks to stellar occultations and adaptive optics observations (Carry et al. 2010).

The other difference with the case of (433) Eros is that there are less observed dense light-curves. As a matter of fact, the light-curve inversion provides two ambiguous solutions for the spin axis coordinates, at $(37.9^\circ, -15.1^\circ)$ and $(199.6^\circ, 39.4^\circ)$. Both poles yield the same RMS residuals for the fit to the light-curves.

A priori, there is no way to know which solution is the best, without additional constraint such as disk-resolved observations, since both solutions reproduce equally well the observed photometry. However, there is a clear difference between the two when analysing the bootstrap curve (Fig. 3). The first solution follows the well-defined exponential convergence providing $\eta_a = 0.045$, which seems to be consistent with the shape model as it is known so far. For the second spin axis orientation solution, we see that the bootstrap curve does not seem to follow the exponential trend. The corresponding $\eta_a \sim 0.15$ is in contradiction with the fact that the shape of (2) Pallas does not show any sign of large concave topological features. The rejection of the second pole solution is consistent with the result of stellar occultations and adaptive optics (Carry et al. 2010).

3.2.3. Distribution of flat surfaces across the available shape-model population.

The bootstrap method gives us information on the possible presence of concave topological features. Here, a large number of asteroid shape models are analysed. These shape models are used as a reference population with which the derived shape models of Barbarians can be compared.

This reference was constructed using the shape models available on the DAMIT database (Ďurech et al. 2010). More than 200 asteroid shape models were analysed. For many of them, the result of the bootstrap method clearly shows that more data would be needed to obtain a stable shape. In a minority of cases, we find a behaviour suggesting incorrect pole coordinates. We selected a sample of 130 shape models, for which the bootstrap curve had the expected, regular behaviour towards a convergence, and for them we computed η_a .

4. Results and interpretation

In Fig. 4, one example of a composite light-curve for two asteroids observed by our network is shown. For each target, the synodic period (P_{syn}) associated to the composite light-curve is provided. Additional light-curves are displayed in Appendix C. For the cases where too few light-curves have been obtained by our survey to derive a reliable synodic period, the sidereal period (Psid) determined based on multi-opposition observations and obtained by the light-curve inversion method is used as an initial guess. In the case of (824) Anastasia, no error bars are provided since our observations were obtained during only one (very long) revolution. In Fig. 5 is displayed two examples of shape model derived in this work. Additional shape models are displayed in Appendix D. The bootstrap curves (see Sec. 3.2.1) are also shown for the different solutions of the pole orientation (except for (387) Aquitania for which no sparse data were used). Table 3 summarises the information about these asteroids, whose physical properties have been improved by our observations. Table 4 is the same as Table 3, except that it lists asteroids that we did not directly observe ourselves, but that are relevant to our discussion.

4.1. Individual asteroids

In the following we compare our results for each asteroid to some data available in the literature; asteroid occultation results (Dunham et al. 2016) in particular.

In Figs. 6 to 9, the occultations data are represented in the so-called fundamental plane (i.e. the plane passing through the centre of the Earth and perpendicular to the observer-occulted star vector) (Durech et al. 2011). In that plane, the disappearance and reappearance of the occulted star are represented respectively by blue and red squares and the occultation chords represented by coloured continuous segments. Error bars on the disappearance and reappearance absolute timing are represented by discontinuous red lines. Negative observations (no occultation observed) are represented by a continuous coloured line. Discontinuous segments represent observations for which no absolute timing is available. For each asteroid, the corresponding volume-equivalent radius is computed (corresponding to the radius of a sphere having the same volume as the asteroid shape model). The dimensions of the ellipsoid best fitting the shape model are also given. The uncertainties on the absolute dimensions of the shape models adjusted to stellar occultations are derived by varying various parameters according to their own uncertainties. First, the different shape models obtained during the bootstrap method are used. The spin axis parameters are randomly chosen according to a normal distribution around their nominal values with standard deviation equal to the error bars given in Table 3. Finally the extremes of each occultation chord are randomly shifted according to their timing uncertainties. The observed dispersion in the result of the scaling of the shape model on the occultations chords is then taken as the formal uncertainty on those parameters.

The list of all the observers of asteroid occultations which are used in this work can be found in Appendix D (Dunham et al. 2016). In the following we discuss some individual cases.

(172) Baucis - There are *two* reported occultations. The first event is a single-chord, while the other (18 December 2015) has two positive chords and two negative ones, and was used to scale the shape model (Fig. 6). According to the fit of the shape model to the occultation chords, both pole solutions seemed equally likely. The two solutions give similar absolute dimen-



Fig. 3. Bootstrap curves for the asteroid (2) Pallas. The panels illustrate the curve obtained for different coordinates of the spin axis.



Fig. 4. Composite light-curves of two asteroids in our sample. Each light-curve is folded with respect to the synodic period of the object, indicated below the plot.

sions of $(41.1 \pm 2, 36.3 \pm 1.8, 31.8 \pm 1.6)$ and $(40.8 \pm 2.4, 36.1 \pm 1.7, 33.5 \pm 1.6)$ km, respectively. The corresponding volumeequivalent radii are $R_{eq} = 36.2 \pm 1.8$ km and $R_{eq} = 36.7 \pm 1.8$ km, to be compared to the NEOWISE (Mainzer et al. 2016), AKARI (Usui et al. 2012) and IRAS (Tedesco 1989) radii: 35.3 ± 0.4 , 33.5 ± 0.4 and 31.2 ± 0.6 km, respectively. Even though the occultation observations cannot provide information about the best spin axis solution, the bootstrap curve indicates a clear preference for the one with retrograde rotation.

(236) Honoria - There are eight observed occultations. However, over these eight events, only two have \geq two positive chords (in 2008 with two positive chords and 2012 with three positive chords). These were used to constrain the pole orientation and scale the shape model. The result shows that the first pole solution (λ_1 and β_1 from Table 3) is the most plausible. By simultaneously fitting the two occultations, the obtained dimensions are (48.8 ± 1.4, 48.3 ± 1.3, 33.7 ± 1.0) km, and the volume-equivalent radius $R_{eq} = 43.0 \pm 2.1$ km. In the case of the second pole solution, the dimensions of the semi-axes are (52.3 ± 2.7, 52.1 ± 2.6, 37.1 ± 1.9) km and the equivalent radius is $R_{eq} = 45.6 \pm 2.3$ km. These solutions are compatible with the NEOWISE, AKARI, and IRAS measurements which are respectively 38.9±0.6, 40.6±0.5 and 43.1±1.8 km. The fit of the shape model for the two pole solutions is shown in Fig. 7. (387) Aquitania - For this asteroid, the result of the lightcurve inversion process gives different solutions for the rotation period when sparse data are included. However, the noise on the sparse data is higher than the amplitude of the light-curves themselves. For this reason we decided to discard them. As a consequence, we did not apply the bootstrap method to this asteroid.

There is one well sampled occultation of (387) Aquitania providing four positive and four negative chords. The adjustment of the unique solution of the shape model on the occultation chords shows a good agreement. The scaling leads to an equivalent radius $R_{eq} = 50.4 \pm 2.5$ km. The absolute dimensions are $(54.2 \pm 2.7, 50.6 \pm 2.5, 46.6 \pm 2.3)$ km. This is consistent with the WISE (Masiero et al. 2011), AKARI, and IRAS radii, which are respectively $48.7 \pm 1.7, 52.5 \pm 0.7$, and 50.3 ± 1.5 km. The fit of the shape model on the occultation chords is shown in Fig. 8.

Hanuš et al. (2017) found a relatively similar model, spin axis solution ($P_{\text{sid}} = 24.14012$ hours, $\lambda = 123^{\circ} \pm 5^{\circ}$, and $\beta = 46^{\circ} \pm 5^{\circ}$), and size (48.5 ± 2 km) using an independent approach.

(402) Chloe - There are six reported occultations, but only two can be used to adjust the shape models on the occultation chords. These two occultations occurred on the 15 and 23 December 2004. The result clearly shows that the first pole solution is the best one. The other one would require a deformation of the shape that would not be compatible with the constraints imposed by the negative chords. The derived di-



Fig. 5. Example of two asteroid shape models derived in this work. For both shape model, the reference system in which the shape is described by the inversion procedure, is also displayed. The *z* axis corresponds to the rotation axis. The *y* axis is oriented to correspond to the longest direction of the shape model on the plane perpendicular to *z*. Each shape is projected along three different viewing geometries to provide an overall view. The first one (left-most part of the figures) corresponds to a viewing geometry of 0° and 0° for the longitude and latitude respectively (the *x* axis is facing the observer). The second orientation corresponds to $(120^{\circ}, 30^{\circ})$ and the third one to $(240^{\circ}, -30^{\circ})$. The inset plot shows the result of the Bootstrap method. The *x* axis corresponds to the number of light-curves used and the *y* axis is η_a .



Fig. 6. Fit of the derived shape models for (172) Baucis on the observed occultation chords from the 18 December 2015 event. The left panel represents the shape model corresponding to the first pole solution (λ_1 , β_1). The right panel represents the shape model obtained using the second pole solution.

mensions of (402) Chloe, for the first spin axis solution, are $(38.3 \pm 1.9, 33.7 \pm 1.7, 24.7 \pm 1.2)$ km and the equivalent radius is $R_{eq} = 31.3 \pm 1.6$ km. The second spin solution leads to the dimensions $(46.9 \pm 2.4, 41.3 \pm 2.1, 29.0 \pm 1.5)$ km and $R_{eq} = 38.3 \pm 1.9$ km. The NEOWISE radius is 27.7 ± 0.8 km while the AKARI and IRAS radii are 30.2 ± 1.5 and 27.1 ± 1.4 km, respectively, which agree with the first pole solution, but not with the sec-

ond one. The fit of the shape model on the occultation chords is shown in Fig. 9.

(824) Anastasia - The light-curve inversion technique provided three possible pole solutions. However, two of them present a rotation axis which strongly deviates from the principal axis of inertia. This is probably related to the extreme elongation of the shape model. The light-curve inversion technique is

Devogèle et al.: Shape and spin determination of Barbarian asteroids

Aster.	b/a	c/b	$P_{\rm sid}$	λ_1	β_1	λ_2	β_2	N _{dl}	N_{opp}	N689	N_{703}	N_{LO}	η_a	D
			[hours]	[deg]	[deg]	[deg]	[deg]							[km]
122	0.85	0.96	10.6872 ± 1	30 ± 5	20 ± 10	209 ± 5	22 ± 10	24	6	181	108		0	(70.7 ± 0.9)
172	0.93	0.90	27.4097 ± 4	171 ± 11	-64 ± 10	14 ± 9	-57 ± 10	61	6	159	75		0.17	77.4 ± 3.9
236	0.88	0.86	12.3375 ± 1	196 ± 9	54 ± 10	36 ± 7	44 ± 10	57	5	187	120		0.16	86.0 ± 4.3
387	0.93	0.88	24.14 ± 2	142 ± 8	51 ± 10			26	6					100.7 ± 5.3
402	0.88	0.70	10.6684 ± 1	306 ± 10	-61 ± 10	162 ± 7	-41 ± 10	15	4	169	65		0	64.6 ± 3.2
458	0.86	0.80	21.81 ± 5	274 ± 6	33 ± 10	86 ± 5	14 ± 10	14	3	197	103		0.38	(36.7 ± 0.4)
729	0.88	0.86	25.195 ± 1	88 ± 26	-79 ± 10			60	3	182	104		0.14	(50.0 ± 0.4)
824			252.0 ± 7					25	2	133	149			(32.5 ± 0.3)
980	0.93	0.83	20.114 ± 4	24.2 ± 6	35 ± 10	203 ± 5	-5 ± 10	48	6	167	68		0.28	(74.7 ± 0.6)
1332			32.120 ± 1					16	2			408		(46.8 ± 0.1)
1372			15.23 ± 4					18	2	84	60			(26.5 ± 0.3)
1702			21.15 ± 2					21	2	90	155			(34.6 ± 0.1)
2085			111 ± 1					12	1	27	93			(13.35 ± 0.04)
3844			13.33 ± 2					10	1		87			(15.5 ± 0.7)
15552			33.63 ± 7					19	2		58			(6.2 ± 0.2)

Table 3. Summary of the results pertaining to our survey. The b/a and c/b columns represent the relative axis dimensions of the ellipsoid best fitting the shape model. The P_{sid} column indicates the sidereal rotation period of the asteroid in hours. The uncertainties are given with respect to the last digit. Columns λ_n and β_n , with n = 1 and 2, represent the two or the unique pole solution(s). The N_x columns represent respectively the number of dense light-curves, the number of oppositions and the number of sparse points from the USNO (MPC code 689), Catalina (MPC code 703) and Lowell surveys. η_a represents the fraction of flat surfaces present on the shape model as inferred by the bootstrap method. Finally, the *D* column represents the equivalent diameter of the sphere having the same volume as the asteroid shape model. When we were not able to scale the shape model of the asteroid, the NEOWISE diameter (Mainzer et al. 2016) (or WISE diameter (Masiero et al. 2011) when NEOWISE data are unavailable) is given in parentheses.

Asteroid	b/a	c/b	P _{sid}	λ_1	β_1	λ_2	β_2	η_a	D	Ref.
			[hours]	[deg]	[deg]	[deg]	[deg]		[km]	
234	0.90	0.88	26.474	144	-38			0.33	43.7	[1]
599			9.3240						71	[2]
606	0.82	0.92	12.2907	183	20	354	26		35.5	[3]
642			8.19						38.2	[4]
673			22.340						41.6	[5]
679	0.72	0.92	8.45602	220	32	42	-5	0.38	51.4	[6]
1284			9.55						46	[7]
2448			10.061						43	[8]

Table 4. Same as Table 3, but for asteroids which were not observed during this campaign. The bootstrap method was not applied to (606) because the number of dense light-curves was not sufficient. References : [1] Tanga et al. (2015), [2] Debehogne et al. (1977), [3] Hanuš et al. (2011), [4] LeCrone et al. (2005), [5] Marciniak et al. (2016), [6] Marciniak et al. (2011), [7] Carreño-Carcerán et al. (2016), [8] Strabla et al. (2013)

known to have difficulty in constraining the relative length along the axis of rotation, in particular. In the case of highly elongated bodies, the principal axis of inertia is poorly constrained.

Two occultations were reported for this asteroid. The models cannot fit the two occultations simultaneously using a single scale factor. We decided therefore not to present the shape model and spin solutions in this paper as new observations are required to better constrain the pole solution. Because of the very large rotation period of this asteroid, the presence of a possible tumbling state should also be tested.

(2085) Henan - This asteroid possesses a relatively large rotation period. Based on our photometric observation, two synodic periods can be considered (110 ± 1 hours and 94.3 ± 1 hours). However, the light-curve inversion technique seems to support the first one based on our observations and sparse data.

4.2. Presence of concavities

We have applied the flat detection method (FSDT) described in Devogèle et al. (2015) to all the shape models presented in this paper, thus (Sec. 3.2) providing a quantitative estimate for the presence of concavities and for the departure of an asteroid shape from a smooth surface with only gentle changes of curvature. Fig. 10 presents the result of the FSDT for the shape models presented in this work (blue diamonds, see Tables 3 and 4). These results can be compared to the average value of η_a computed by bins of 15 asteroids (red squares) using the asteroid population described in Sec. 3.2.3 (black dots).

From this distribution, a correlation between diameter and fraction of flat surfaces seems to be apparent. Such correlation is expected since small asteroids are more likely to possess irregular shapes than larger ones. However, the quality of asteroid light-curves is directly correlated to the asteroids diameter. For small asteroids (< 50 km), this effect might also increase the mean value of η_a . Fig. 10 does not show clear differences between Barbarians and other asteroids, as Barbarians seem to populate the same interval of values. As expected, some asteroids like Barbara show a large amount of flat surfaces, but this is not a general rule for Barbarians. Of course the statistics are still not so high, but our initial hypothesis that large concave topological features could be more abundant on objects having a peculiar polarisation does not appear to be valid in view of this first attempt of verification.



Fig. 7. Fit of the derived shape models for (236) Honoria on the observed occultation chords from the 11 October 2011 and the 7 September 2012 events. The left panel represents the 2008 event with the top and bottom panels corresponding to the first and second pole solutions, respectively. The right panel is the same as the left one, but for the 2012 event.



Fig. 8. Fit of the derived shape model for (387) Aquitania on the observed occultation chords from the 26 July 2013 event.

4.3. Are Barbarian asteroids slow rotators ?

In this Section, we compare the rotation periods of Barbarians and Barbarian candidates with those of non-Barbarian type. At first sight the rotation period of confirmed Barbarian asteroids seems to indicate a tendency to have long rotation periods, as the number of objects exceeding 12h is rather large. For our analysis we use the sample of objects as in Tables 3 and 4. By considering only asteroids with a diameter above 40 km, we are relatively sure that our sample of L-type asteroids is both almost complete, and not affected by the Yarkovsky-O'Keefe-Radzievskii-Paddack effect (Bottke et al. 2006). However, as only 13 asteroids remain in the sample, we also consider a second cut at 30 km, increasing it to 18. As shown below, our findings do not change as a function of this choice.

We proceed by comparing the rotation period of the Barbarians with that of a population of asteroids that possess a similar size distribution. Since the distribution of rotation periods is dependent on the size of the asteroids, we select a sample of asteroids with the same sizes, using the following procedure. For each Barbarian, one asteroid is picked out randomly in a population for which the rotation period is known, and having a similar radiometric diameter within a ± 5 km range. This way we construct a population of asteroids with the same size distribution as the Barbarians. We now have two distinct populations that we can compare. By repeating this process several times, we build a large number of populations of 'regular' asteroids. We can then check the probability that the distribution of rotation periods of such a reconstructed population matches the one of the Barbarians.

Considering the sample of asteroids with a diameter larger than 40 km, the sample is too small to derive reliable statistics. However, we notice that the median of the rotation period of the Barbarians is 20.1 hours while the median of the population regular asteroid is only 12.0 hours.



Fig. 9. Fit of the derived shape models for (402) Chloe on the observed occultation chords from 15 and 23 December 2014 events. The leftmost part of the Figure represents the 15 event with the upper and lower parts corresponding to the first and second pole solutions, respectively. The rightmost part of the Figure is the same as the leftmost part, but for the 23 December event.



Fig. 10. Values of η_a as a function of the asteroids diameters. The black dots correspond to individual asteroids. The red squares correspond to the mean values of η_a and diameter for bins of 15 asteroids. The blue diamonds correspond to Barbarian asteroids.

In order to improve the statistic, we can also take into account asteroids with a diameter between 30 and 40 km. The median of the Barbarian asteroids is now 20.6 hours while the regular asteroids population has a median of 11.4 hours.

Fig. 11 represents the histograms of the rotation periods of Barbarian asteroids (with diameter > 30 km) compared to the population of regular asteroids constructed as described at the beginning of this section. The histogram of the Barbarian aster-



Fig. 11. Normalised histograms of the Barbarian compared to the histogram asteroids having a diameter between 110 and 30 km.

oids shows a clear excess of long rotation periods and a lack of fast-spinning asteroids.

We adopt the two-samples Kolmogorov-Smirnov (KS) test to compare the distributions of Barbarians and regular asteroids.

This is a hypothesis test used to determine whether two populations follow the same distribution. The two-sample KS test returns the so-called asymptotic *p*-value. This value is an indication of the probability that two samples come from the same population.

In our case, we found p = 0.6%, clearly hinting at two distinct populations of rotation period.

In conclusion our results show that there is clear evidence that the rotations of Barbarian asteroids are distinct from those of the whole population of asteroids. The abnormal dispersion of the rotation periods observed for the Barbarian asteroids is more probably the result of a true difference than a statistical bias.

5. Conclusions

We have presented new observations here for 15 Barbarian or candidate Barbarian asteroids. For some of these asteroids, the observations were secured by us during several oppositions. These observations allow us to improve the value of the rotation period. For eight of them, we were able to determine or improve the pole orientation and compute a shape model.

The shape models were analysed using a new approach based on the technique introduced by Devogèle et al. (2015). We show that this technique is capable of providing an indication about the completeness of a light-curve data set indicating whether or not further observations are required to better define a shape solution of the photometric inversion method. The extrapolation of the trend towards a large number of light-curves gives a more precise determination of η_s . This new method was applied to a large variety of shape models in the DAMIT database. This allowed us to construct a reference to which the shape models determined in this work were compared. Our results show that there is no evidence that our targets have more concavities or are more irregular than a typical asteroid. This tends to infirm the hypothesis that large-scale concavities may be the cause of the unusual polarimetric response of the Barbarians.

The improvement and new determination of rotation periods has increased the number of asteroids for which a reliable rotation period is known. This allows us to have an improved statistic over the distribution of rotation periods of the Barbarian asteroids. We show in this work possible evidence that the Barbarian asteroids belong to a population of rotation periods that contains an excess of slow rotators, and lacks fast spinning asteroids. The relation between the polarimetric response and the unusual distribution of rotation periods is still unknown.

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- ¹ Université de Liège, Space sciences, Technologies and Astrophysics Research (STAR) Institute, Allée du 6 Août 19c, Sart Tilman, 4000 Liège, Belgium
- e-mail: devogele@astro.ulg.ac.be
- ² Université Côte d'Azur, Observatoire de la Côte d'Azur, CNRS, Laboratoire Lagrange
- Astronomical Institute, Faculty of Mathematics and Physics, Charles University in Prague, Czech Republic
- 4 CdR & CdL Group: Light-curves of Minor Planets and Variable Stars, Switzerland
- ⁵ Estación Astrofísica Bosque Alegre, Observatorio Astronómico Córdoba, Argentina
- ⁶ Institute of Geology, Adam Mickiewicz University, Krygowskiego 12, 61-606 Poznań
- Observatoire de Chinon, Chinon, France
- 8 Geneva Observatory, Switzerland
- Astronomical Observatory Institute, Faculty of Physics, A. Mickiewicz University, Słoneczna 36, 60-286 Poznań, Poland
- 10 Unidad de Astronomía, Fac. de Ciencias Básicas, Universidad de Antofagasta, Avda. U. de Antofagasta 02800, Antofagasta, Chile
- 11 Korea Astronomy and Space Science Institute, 776 Daedeokdae-ro, Yuseong-gu, Daejeon, Republic of Korea
- ¹² Osservatorio Astronomico della regione autonoma Valle d'Aosta,Italy
- 13 School of Physics, University of Western Australia, M013, Crawley WA 6009, Australia
- ¹⁴ Shed of Science Observatory, 5213 Washburn Ave. S, Minneapolis,MN 55410, USA
- 15 Akdeniz University, Department of Space Sciences and Technologies, Antalya, Turkey
- ¹⁶ TUBITAK National Observatory (TUG), 07058, Akdeniz University Campus, Antalya, Turkey
- ¹⁷ Department of Physics & Astronomy, University of British Columbia, 6224 Agricultural Road, Vancouver, B.C. V6T 1Z1, Canada
- ¹⁸ Astrophysics Division, Institute of Physics, Jan Kochanowski University, Świ etokrzyska 15,25-406 Kielce Poland
- ¹⁹ Laboratory of Space Researches, Uzhhorod National University, Daleka st., 2a, 88000, Uzhhorod, Ukraine
- 20 Institute of Physics, Faculty of Natural Sciences, University of P.J. Safarik, Park Angelinum 9, 040 01 Kosice, Slovakia
- ²¹ Stazione Astronomica di Sozzago, Italy
- NaXys, Department of Mathematics, University of Namur, 8 Rempart de la Vierge, 5000 Namur, Belgium
- 23 Instituto de Astrofísica de Canarias (IAC), E-38205 La Laguna, Tenerife, Spain

- ²⁴ Departamento de Astrofísica, Universidad de La Laguna (ULL), E-38206 La Laguna, Tenerife, Spain
- 25 Mt. Suhora Observatory, Pedagogical University, Podchorażych 2, 30-084, Cracow, Poland
- 26 Instituto de Astrofísica de Andalucía, CSIC, Apt 3004, 18080 Granada, Spain
- 27 CITEUC - Centre for Earth and Space Science Research of the University of Coimbra, Observatório Astronómico da Universidade de Coimbra, 3030-004 Coimbra, Portugal
- Agrupación Astronómica Región de Murcia, Orihuela, Spain
- ²⁹ Arroyo Observatory, Arroyo Hurtado, Murcia, Spain
- ³⁰ 4438 Organ Mesa Loop, Las Cruces, New Mexico 88011 USA

Appendix A: Summary of the new observations used in this work

Appendix B: Summary of previously published observations used in this work

Appendix C: Light-curves obtained for this work

- Appendix D: Shape models derived in this work
- Appendix E: List of observers for the occultation data used in this work

A&A proofs: manuscript no. Barbarians

A stansid	Data of charmetican	N 7	Observer	
Asteroid	Date of observations	N _{lc}	Ubservers M. D	Observatory
(122) Gerda	2015 Jun 09 - Jul 06	0	M. Devogele	Calern observatory, France
(1/2) Baucis	2004 Nov 20 - 2005 Jan 29	2	F. Manzini	Sozzago, Italy
	2005 Feb 22 - Mar 1 2012 Mar 1 Arr 25	3 10	P. Antonini	Bedoin, France
	2013 Mar 1 - Apr 25	10	A. Marciniak, M. Bronikowska	Borowiec, Poland
			K. HIRSCH, I. Santana,	
			F. Berski, J. Nadolny,	
	2012 Mar 4 A 4 17	2	K. SODKOWIAK	
	2013 Mar 4 - Apr 17	3	Ph.Bendjoya, M. Devogele	Libert observatory, France
	2013 Mar 5 - Apr 16	15	P. Hickson	UBC Southern Observatory,
	2012 Mar 5 9	2		La Serena, Unite
	2013 Mar 5 - 8	5	M. Todd and D. Coward	Zadko Telescope, Australia
	2013 Mar 29	1	F. Pilcher	Organ Mesa Observatory, Las Cruces, NM
	2014 Nov 13	I 7	M. Devogele	Calern observatory, France
(02())]]	2014 NOV 18 - 26	2	A. U. Iomatic, K. Kaminski	winer Observatory (RBT), USA
(236) Honoria	2006 Apr 29 - May 3	3	K. Poncy	Le Cres, France
	2007 Jul 31 - Aug 2	3	J. Coloma, H. Pallares	Sabadell, Barcelona, Spain
	2007 Jun 21 - Aug 21	2	E. Forne,	Osservatorio L'Ampolia, Tarragona, Spain
	2012 Sep 19 - Dec 06	9	A. Carbognani, S. Caminiti	OAVdA, Italy
	2012 Aug 20 - Oct 28	6	M. Bronikowska, J. Nadolny	Borowiec, Poland
	2012 0 4 22 2014 02 20	0	I. Santana, K. Sobkowiak	Dense in Data 1
	2013 Oct 23 - 2014 03 20	8	D. Oszkiewicz, R. Hirsch	Borowiec, Poland
			A. Marciniak, P. Irela,	
	20141 02 51 10	-	I. Konstanciak, J. Horbowicz	
	2014 Jan 03 - Feb 19	/	F. Pilcher	Organ Mesa Observatory, Las Cruces, NM
	2014 Feb 0/ - Feb 1/	2	M. Devogele	Calern observatory, France
	2014 Mar 09 - 20	2	P. Kankiewicz	Kielce, Poland
	2015 Mar 21 - 22	2	W. Ogłoza, A. Marciniak,	Mt. Sunora, Poland
	2015 Mar 22 Mai 07	2	V. KUUAK E. Dilahar	Organ Mass Observatory Las Cruses NM
(207) A quitania	2013 Mar 22 - Mar 07	3 4	r. Flicher	Digali Mesa Observatory, Las Cruces, NM Bergyvige, Belend
(387) Aquitania	2012 Mar 22 - May 23	4	A. Marcillak, J. Nadolly,	borowiec, Poland
	2013 Jun 26 Jul 25	2	A. KIUSZEWSKI, I. Salitalia, M. Davogàla	Calarn observatory France
	2013 Jull 20 - Jull 23 2014 Nov 10 Dec 20	2 1	A II Tomatic K Kamiński	Winer Observatory (PRT) USA
	2014 NOV 19 - Dec 29	4	K. U. Tolliauc, K. Kalilliski K. Kamiński	while Observatory (RD1), USA
	2014 Nov 19 Dec 18	2	M Todd and D Coward	Zadko Telescope Australia
	2014 Roy 17 - Dec 18 2014 Dec 17	1	F Char	SARA La Serena Chile
	2014 Dec 17 2014 Dec 18	1	M Devogèle	Calern observatory France
	2014 Dec 10 2015 Jan 10 - 11	2	Toni Santana-Ros Rene Duffard	IA A Sierra Nevada Observatory
	2015 Nov 27 - 2016 Feb 16	$\frac{2}{2}$	M Devogèle	Calern observatory France
(402) Chloe	2015 Jul 01 - 14	$\frac{2}{2}$	M C Quiñones	EABA Argentina
(458) Hercynia	2013 May 20 - Jun 05	$\frac{1}{4}$	M Devogèle	Calern observatory France
(150) Hereyina	2013 May 20 Juli 05	2	M-I Kim Y-I Choi	SOAO South Korea
	2014 Nov 27	1	A Marciniak	Borowiec Poland
	2014 Nov 28 - 29	2	A II Tomatic K Kamiński	Winer Observatory (RBT) USA
	2014 Nov 29	1	M Devogèle	Calern observatory France
	2014 Nov 30	1	N Morales	La Hita Spain
(729) Watsonia	2013 Apr 04 - Jun 06	16	M Devogèle	Calern observatory France
(72)) Watsonia	2014 May 26 - Jun 18	16	R D Stephens	Santana Observatory
	2015 Sep 25	1	O. Erece, M. Kanlan	TUBITAK, Turkey
	-010 bep 20	-	MJ. Kim	
	2015 Oct 05	1	MJ. Kim. YJ. Choi	SOAO. South Korea
	2015 Oct 23 - Nov 30	5	M. Devogèle	Calern observatory. France
(971) Anastasia	2015 Jul 05 25	7	M Davagèla	Calam abaamyatamy Emanas

(824) Anastasia 2015 Jul 05 - 25 7 M. Devogèle Calern observatory, France **Table A.1.** New observations used for period and shape model determination which were presented in this work and observations that are not included in the UAPC.

Devogèle et al.: Shape and spin determination of Barbarian asteroids

Asteroid	Date of observations	$N_{\rm lc}$	Observers	Observatory
(980) Anacostia	2005 Mar 15 - Mar 16	2	J.G. Bosch	Collonges, France
	2009 Feb 14 - Mar 21	6	M. Audejean	Chinon, France
	2012 Aug 18 - Nov 02	7	K. Sobkowiak, M. Bronikowska	Borowiec
			M. Murawiecka, F. Berski	
	2013 Feb 22 - Feb 24	3	M. Devogèle	Calern observatory, France
	2013 Mar 27 - Apr 15	7	A. Carbognani	OAVdA, Italy
	2013 Dec 19 - Feb 23	11	A.U. Tomatic	OAdM, Spain
	2013 Dec 18 - Feb 07	2	R. Hirsch, P. Trela	Borowiec, Poland
	2014 Feb 22 - Mar 27	4	M. Devogèle	Calern observatory, France
	2014 Feb 25 - Mar 7	3	J. Horbowicz, A. Marciniak	Borowiec, Poland
	2014 Feb 27	1	A.U. Tomatic	OAdM, Spain
	2015 Mar 11 - May 28	5	F. Char	SARA, La Serena, Chile
	2015 Jun 09	1	M.C. Quiñones	EABA, Argentina
(1332) Marconia	2015 Apr 12 - May 18	8	M. Devogèle	Calern observatory, France
	2015 May 20	1	A.U. Tomatic, K. Kamiński	Winer Observatory (RBT), USA
	2015 Jun 03	1	R.A. Artola	EABA, Argentina
(1372) Haremari	2009 Nov 03 - Dec 08	8	R. Durkee	Shed of Science Observatory,
				Minneapolis, MN, USA
	2014 Dec 11 - Feb 11	7	M. Devogèle	Calern observatory, France
	2015 Jan 10 - 11	2	T. Santana-Ros, R. Duffard	IAA, Sierra Nevada Observatory, Spain
(1702) Kalahari	2015 Apr 29 - May 18	3	M. Devogèle	Calern observatory, France
	2015 May 19	1	A. U. Tomatic, K. Kamiński	Winer Observatory (RBT), USA
	2015 May 20	1	MJ. Kim, YJ. Choi	SOAO, South Korea
	2015 Jun 04 - Jul 08	8	C.A. Alfredo	EABA, Argentina
(2085) Henan	2015 Jan 09 - 10	2	A. U. Tomatic	OAdM, Spain
	2015 Jan 11	1	T. Santana-Ros, R. Duffard	IAA, Sierra Nevada Observatory, Spain
	2015 Jan 14 - 15	2	M. Todd and D. Coward	Zadko Telescope, Australia
	2015 Jan 14 - Feb 11	7	M. Devogèle	Calern observatory, France
	2015 Mar 11	1	F. Char	SARA, La Serena, Chile
(3844) Lujiaxi	2014 Nov 12 - Dec 23	5	M. Devogèle	Calern observatory, France
	2014 Nov 20 - Dec 18	2	M. Todd and D. Coward	Zadko Telescope, Australia
	2014 Nov 20	1	A.U. Tomatic, K. Kamiński	Winer Observatory (RBT), USA
	2014 Dec 25 - 26	2	A.U. Tomatic	OAdM, Spain
(15552)	2014 Oct 29 - Nov 25	7	A. U. Tomatic, K. Kamiński	Winer Observatory (RBT), USA
Sandashounkan	2014 Oct 30 - Nov 13	2	M. Devogèle	Calern obervatory, France
	2014 Nov 20	1	A U Tomatic	OAdM Spain

Table A.1. Continued

A&A proofs: manuscript no. Barbarians

Asteroid	Date of observations	$N_{\rm lc}$	Reference
(122) Gerda	1987 Jul 28 - Aug 01	2	Shevchenko et al. (2009)
	1981 Mar 13 - 25	3	di Martino et al. (1994)
	1981 Mar 18 - 19	2	Gil-Hutton (1993)
	2003 Mai 02 - 09	3	Shevchenko et al. (2009)
	2005 Sep 11 - Oct 04	2	Shevchenko et al. (2009)
	2005 Sep 31 - Nov 28	3	Buchheim et al. (2007)
	2009 Apr 01 - 03	3	Pilcher (2009)
(172) Baucis	1984 May 11	1	Weidenschilling et al. (1990)
	1989 Nov 21	1	Weidenschilling et al. (1990)
(236) Honoria	1979 Jul 30 - Aug 22	7	Harris and Young (1989)
	1980 Dec 30 - 1981 Feb 1	7	Harris and Young (1989)
(387) Aquitania	1979 Aug 27 - 29	3	Schober et al. (1979)
	1981 May 30	1	Barucci et al. (1985)
	1981 May 30 - Jul 24	8	Harris et al. (1992)
(402) Chloe	1997 Jan 19 - Mar 02	5	Denchev et al. (2000)
	2009 Feb 07 - 17	4	Warner (2009)
	2014 May 15 - 16	2	Stephens (2014)
(458) Hercynia	1987 Feb 18	1	Binzel (1987)
(729) Watsonia	2013 Jan 21 - Feb 14	8	Stephens (2013)
(980) Anacostia	1980 Jul 20 - Aug 18	5	Harris and young (1989)
(1332) Marconia	2012 Aug 27 - Sep 11	6	Stephens (2013)
(1702) Kalahari	2011 Jul 28 - Aug 26	10	Oey (2012)

Table B.1. All observations used for period and shape modelling which have already been published.



Fig. C.1. Composite light-curves of asteroids studied in this works.



Fig. C.1. Continued



Fig. C.2. Continued



Fig. C.2. Continued



Fig. D.1. Asteroid shape models derived in this work. For each shape model, the reference system in which the shape is described by the inversion procedure, is also displayed. The *z* axis corresponds to the rotation axis. The *y* axis is oriented to correspond to the longest direction of the shape model on the plane perpendicular to *z*. Each shape is projected along three different viewing geometries to provide an overall view. The first one (left-most part of the figures) corresponds to a viewing geometry of 0° and 0° for the longitude and latitude respectively (the *x* axis is facing the observer). The second orientation corresponds to $(120^{\circ}, 30^{\circ})$ and the third one to $(240^{\circ}, -30^{\circ})$. The inset plot shows the result of the Bootstrap method. The *x* axis corresponds to the number of light-curves used and the *y* axis is η_a . Since the shape model of (387) Aquitania was derived without sparse data, the bootstrap method was not applied.



Fig. D.1. Continued

List of observers (172) Baucis (2015-12-18) J.A. de los Reyes, Sensi Pastor, SP F. Reyes, SP J.L. Ortiz, SP F. Aceituno, SP

(236) Honoria (2008-10-11) S Conard, Gamber, MD, USA

R Cadmus, Grinnell, IA, USA

(236) Honoria (2012-09-07)

C. Schnabel, SP C. Perello, A. Selva, SP U. Quadri, IT P. Baruffetti, IT J. Rovira, SP

(387) Aquitania (2013-07-26)

T. Blank, West of Uvalde, TX, USA T. Blank, Uvalde, TX, USA T. Blank, D'Hanis, TX, USA T. Blank, Devine, TX, USA S. Degenhardt, Moore, TX, USA M. McCants, TX, USA S. Degenhardt, Bigfoot, TX, USA S. Degenhardt, Poteet, TX, USA S. Degenhardt, Pleasanton, TX, USA

(402) Chloe (2004-12-15)

R. Nugent, Buffalo, TX, USA
R. Venable, Bunnell, FL, USA
R. Venable, DeLand, FL, USA
J. Stamm, Oro Valley, AZ, USA
R. Peterson, Scottsdale, AZ, USA
B. Cudnik, Houston, TX, USA

(402) Chloe (2004-12-23)

S. Preston, Ocean Park, WA, USA J. Preston, Ilwaco, WA, USA T. George, Moro, OR, USA

Fig. E.1. List of observers of stellar occultation by an asteroid.