End-to-End Verification of Stack-Space Bounds for C Programs

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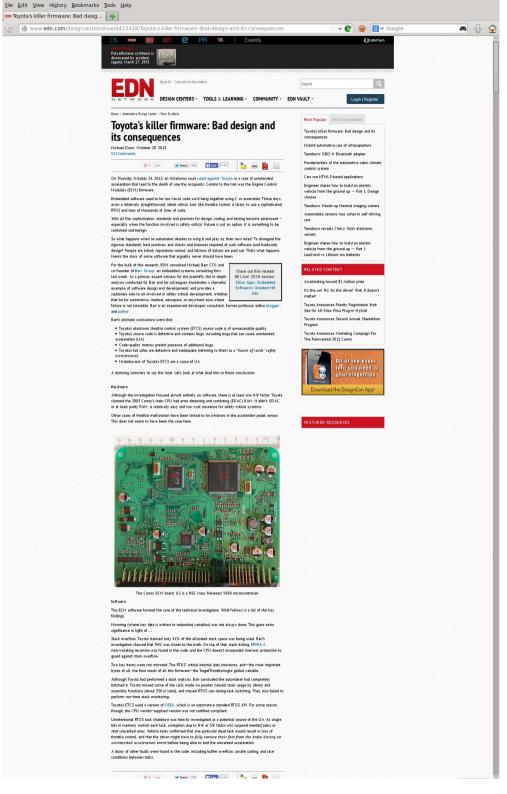


April 14th, 2014

Does this program safely run?

```
#include <stdint.h>
typedef uint64_t t;
void f (t* pa, t* pb) {
  if (*pa == 0) return;
  *pa--;
  f (pa, pb);
  *pb++;
int main (int argc, char*
argv[]) {
  t a = UINT64\_MAX, b = 0;
  f (&a, &b);
  return a;
```

- gcc -O0 && ./a.out
 - Segfault (stack overflow)
- gcc -O1 && ./a.out
 - OK (function inlining)





Control Module's (ECM) firmware.

Stack overflow. Toyota claimed only 41% of the allocated stack space was being used. Barr's investigation showed that 94% was closer to the truth. On top of that, stack-killing, MISRA-C slating recursion was found in the code, and the CPU doesn't incorporate memory protection

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Although Toyota had performed a stack analysis, Barr concluded the automaker had completely botched it. Toyota missed some of the calls made via pointer, missed stack usage by library and assembly functions (about 350 in total), and missed RTOS use during task switching. They also failed to perform run-time stack monitoring.

Does this program stack-overflow?

- Important in embedded software
 - led to deadly software bugs in Toyota cars
- Most stack analysis tools available for compiled code only
 - Harder to analyze
 - User interaction is troublesome
- How to prove, at the source level, that the compiled code does not stack-overflow?
 - How to model stack overflow at the source level?
 - How to prove stack-aware compiler correctness?

CompCert

- Formal C and assembly semantics
- Verified semantics-preserving compiler
 - Safety is preserved
 - For safe programs, I/O events and termination/divergence are preserved

CompCert and stack overflow

- Stack frame allocation always succeeds
 - Stack-overflow not modeled in either C or assembly
 - How to guarantee that, if source program does not crash, then neither does compiled code not even by stack overflow?

[...] it is **hopeless** to prove a stack memory bound on the source program and expect this resource certification to carry out to compiled code: stack consumption, like execution time, is a program property that is not preserved by compilation.



Xavier Leroy (1968-)

Formal Certification of a Compiler Back-end

or: Programming a Compiler with a Proof Assistant

Xavier Leroy INRIA Rocquencou Xavier.Lerov@inria.fr

Abstract

This paper reports on the development and formal certification (proof of semantic preservation) of a compiler from Cminor (a C-like imperative language) to PowerPC assembly code, using the To deprove the suspension of the compiler and for proving its correctness. Such a certified compiler is useful in the context of formal methods applied to the certification of critical software: the certification of the compiler guarantees that the safety properties provided on the source code hold for the executable components of the compiler guarantees that the safety of the safety niled code as well

Categories and Subject Descriptors F.3.1 [Logics and meanings Caregories and superconsect Descriptors 1-3.1 [Logics and meanings of programs]: Specifying and verifying and reasoning about programs—Mechanical verification; D.2.4 [Software engineering]: Software/program verification—Correctness proofs, formal methods, reliability; D.3.4 [Programming languages]: Processors-Compilers, optimization

General Terms Languages, Reliability, Security, Verification.

Keywords Certified compilation, semantic preservation, program proof, compiler transformations and optimizations, the Coq theorem prover

1. Introduction

Can you trust your compiler? Compilers are assumed to be semantically transparent: the compiled code should behave as prescribed by the semantics of the source program. Yet, compilers – and especially optimizing compilers – are complex programs that perform complicated symbolic transformations. We all know horror stories of bugs in compilers silently turning a correct program into an in-

For low-assurance software, validated only by testing, the impact of compiler bugs is negligible: what is tested is the executable code produced by the compiler, rigorous testing will expose errors in the compiler along with errors in the source program. The picture changes dramatically for critical, high-assurance software whose certification at the highest levels requires the use of formal methods (model checking, program proof, etc). What is formally verified using formal methods is almost universally the source code; bugs in the compiler used to turn this verified source into an executable

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and more often, has also been for software industry is aware of this is niques to alleviate it, such as conduct

POPL 2006

the generated assembly code after having turned all compiler optimizations off. These techniques do not fully address the issue, and are costly in terms of development time and program performance. An obviously better approach is to apply formal methods to the compiler itself in order to gain assurance that it preserves the me compiler itsel in order to gain assurance mat preserves ine semantics of the source programs. Many different approaches have been proposed and investigated, including on-paper and on-machine proofs of semantic preservation, proof-carrying code, credible compilation, translation validation, and type-preserving creanie compilators, transiation vaniantion, and type-preserving compilers. (These approaches are compared in section 2.) For the last two years, we have been working on the development of a realistic, certified compiler. By certified, we mean a compiler that is accompanied by a machine-checked proof of semantic preservation. By realistic, we mean a compiler that compiles a language commonly used for critical embedded software (a subseof C) down to assembly code for a processor commonly used in embedded systems (the PowerPC), and that generates reasonably efficient code.

efficient code. This paper reports on the completion of one half of this program: the certification, using the Coq proof assistant [2], of a lightly-optimizing back-end that generates PowerPC assembly code from a simple imperative intermediate language called Cminor. A front-end translating a subset of C to Cminor is being developed and certified, and will be described in a forthcomin-

machine-checked correctness proofs of parts of compilers (see section 7 for a review), our work is novel in two ways. First, recent work tends to focus on a few parts of a compiler, mostly optimizations and the underlying static analyses [18, 6]. In contrast, nurations and the analysis [16] analysis [16] analysis [16] on unwork is modest on the optimization side, but emphasizes the certification of a complete compilation chain from such a from the practive language down to assembly code through 4 intermediate languages. We found that many of the non-optimizing translations performed, while often considered obvious in compiler translations and the properties of are surprisingly tricky to formally prove correct. The other novelty of our work is that most of the compiler is written directly in the Coq specification language, in a purely functional style. The executable compiler is obtained by automatic extraction of Caml code from this specification. This approach has never been applied before to a program of the size and complexity of an optimizing

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Really?

Formal Certification of a Compiler Back-end

or: Programming a Compiler with a Proof Assistant

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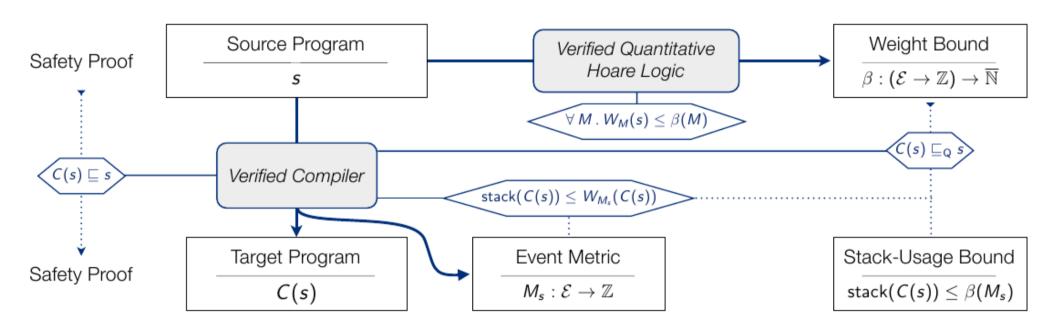
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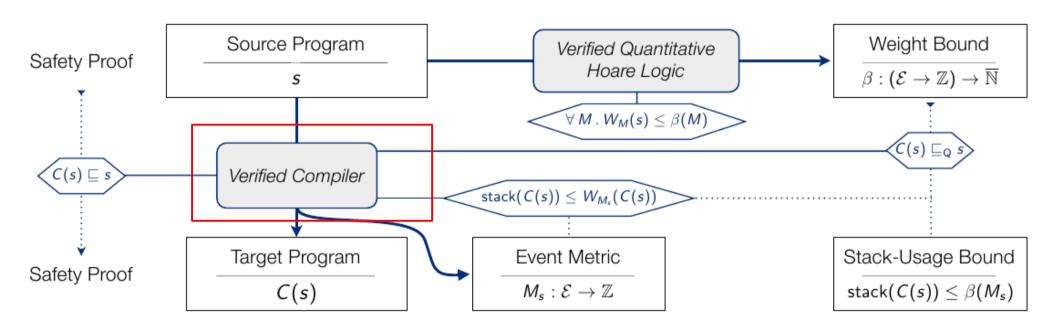
Our solution: Quantitative CompCert

- Introduce stack consumption in C semantics
- Preserve stack consumption by compilation passes: quantitative refinement
- Refine assembly semantics with finite stack
- Make compiler correctness depend on source-level stack bound
 - Introduce a program logic on Clight to derive stack consumption bound
 - Introduce automatic stack analyzer to automatically use program logic on programs without recursion

Overview



Overview



Stack consumption in C semantics

- CompCert C produces an I/O event trace
 - Preserved by compilation
- Add function call/return events
- Model the stack consumption as trace weight parameterized by an event metric for call/return events
 - Preserve the *weights*
 - Stack consumption of a function is parameterized by the stack frame sizes of its callees
- Operational semantics does not go wrong on stack overflow
 - Does not know the event metric, only generates events

Example

```
int f (int x) {
  return x+1;
}

main () {
  f(0);
}
```

int f (int x) { • main() generates trace:

```
call(main) ::
call(f) :: return(f) ::
return(main) :: nil
```

Stack consumption:

```
M(main) + M(f)
```

where M is an *event*metric (giving nonnegative stack frame
size for each function)

Stack consumption

- Events e ::= ... | call(f) | return(f)
- Event and trace valuation:

$$V_{M}(call(f)) = M(f); V_{M}(return(f)) = -M(f);$$

 $V_{M}(e) = 0 \text{ otherwise}$
 $V_{M}(nil) = 0; V_{M}(e::t) = V_{M}(e) + V_{M}(t)$

Trace weight:

$$W_{M}(T) = \sup \{V_{M}(t) \mid T = t . T'\}$$

Stack consumption

Coq implementation: I/O events have constant (maybe non-null) stack consumption

Event and trace valuation:

$$V'_{M}(e) = V_{M}(e)$$
 for call/return
 $V'_{M}(nil) = 0$; $V'_{M}(t++e::nil) = max(V'_{M}(t), V_{M}(t)+V'_{M}(e)$)

Trace weight:

$$W'_{M}(T) = \sup \{V'_{M}(t) \mid T = t . T'\}$$

Quantitative refinement

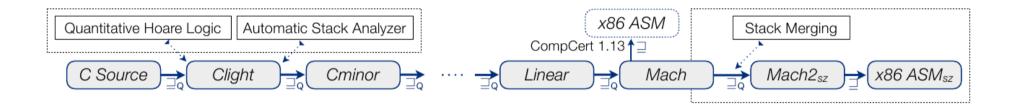
For any target behavior T', there exists a source behavior T such that:

- Pruned traces (call/return events removed) are preserved
- Termination/divergence is preserved
- For all metrics M, $W_M(T') \le W_M(T)$
 - Equality holds for most passes (all events preserved)
 - Do not change the metric during a pass (use the assembly metric)

Quantitative compiler correctness

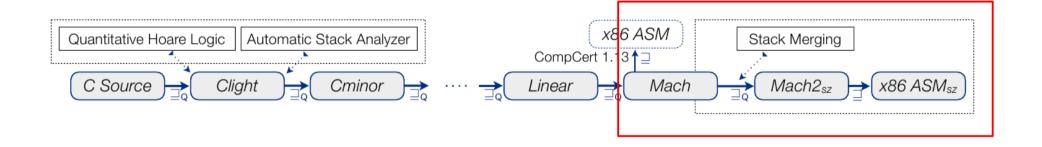
- Given stack size $\beta < 2^{31}$, for all source code s, if all the following hold:
 - The compiler produces assembly code C(s) and event metric M
 - s does not go wrong in infinite stack space
 - All traces T of s have weight $W_{M}(T) \le \beta$
 - Assembly C(s) is run with β stack size
- Then:
 - C(s) refines s (I/O events and termination/divergence are preserved)
 - C(s) does not go wrong
 - In particular, C(s) is guaranteed to not stack overflow

Quantitative CompCert



- Function inlining and tailcall recognition underway
- All other passes supported

Quantitative CompCert



CompCert stack management

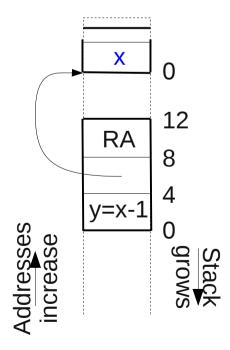
- CompCert memory model: allocate a fresh stack frame memory block upon function entry
 - No pointer arithmetics across different memory blocks
 - Always succeeds
- Still used for assembly language semantics
 - Requires Pallocframe/Pfreeframe pseudo-instructions to manage stack frame blocks
 - Turned into pointer arithmetics by unverified "prettyprinting" phase

CompCert-generated assembly...

```
int g(int y);
int f(int x) {
  return g(x-1)-2;
}
```

```
f:
  Pallocframe
               12, 4
  mov $4(%esp)
                 , %edx
  movl (%edx)
                 , %eax
  subl $1
                 , %eax
  movl %eax
                 , (%esp)
  call q
                 , %eax
  subl $2
  Pfreeframe
               12, 4
  ret.
```

- Formal semantics of Pallocframe/Pfreeframe also:
 - stores/loads return address in/from callee's stack frame
 - Uses RA pseudo-register to model caller's return address slot
 - stores/loads back link to caller's stack frame



... after unverified "pretty-printing"

```
f:
                                f:
 Pallocframe
             12, 4
                                  subl $8
                                                  , %esp
 mov $4(%esp) , %edx
                                  leal $12(%esp) , %edx
 movl (%edx) , %eax
                                  movl %edx , 4(esp)
 subl $1
               , %eax
                                  mov $4(%esp) , %edx
 movl %eax
                , (%esp)
                                  movl (%edx) , %eax
 call q
                                  subl $1
                                                  , %eax
 subl $2
               , %eax
              12, 4
                                  movl %eax
                                                  , (%esp)
 Pfreeframe
 ret
                                  call q
                                  subl $2
                                                  , %eax
                          X
                              12
                          RA
                                  add1 $8
                              8
                                                 , %esp
                                  ret
                              4
                         y=x-1
                              Stack
grows
```

But we can do better and prove it!

, %esp

, %eax

, %eax

(%esp)

%eax

, %esp

X

RA

y=x-1

8

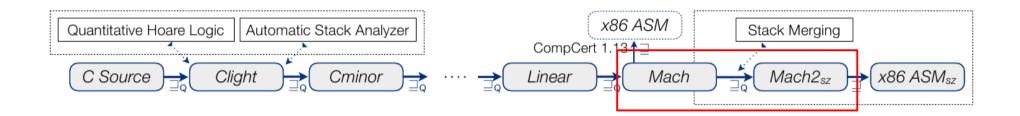
4

```
f:
                                                 f:
  subl $8
                 , %esp
                                                    subl $<u>4</u>
  leal $12(%esp) , %edx
                                                   mov $8(%esp)
 movl %edx
                  , 4(esp)
                  , %edx
  mov $4(%esp)
                                                    subl $1
  movl (%edx)
                  , %eax
                                                   movl %eax
  subl $1
                  , %eax
  movl %eax
                  , (%esp)
                                                   call g
  call q
                                                   subl $2
                  , %eax
  subl $2
                                                   add1 $<u>4</u>
  addl $8
                  , %esp
  ret
                                                    ret
                             X
                                  12
                             RA
                                  8
                                  4
                           y=x-1
                    Addresses increase
```

Assembly with finite stack

- Allocate one single stack block at program start
 - Program goes wrong on stack overflow
 - No need for pseudo-instructions
- Merge all stack frames together into the single stack block
 - Requires *memory injection* proof

Quantitative CompCert



Stack merging

- CompCert Mach to single-stack Mach2 phase
 - Mach already puts arguments into stack
 - Mach no longer stores RA into stack, Mach2 does
 - Mach and Mach2 have same syntax
 - No code transformation: reinterpretation of semantics with single stack
- Mach2 to assembly
 - Implement function entry/exit with stack pointer arithmetics
 - No significant memory changes
- Total changes: 5k LOC (out of CompCert's 90k)

Mach vs. Mach2

```
Registers (x86)r := EAX | EBX | ECX | EDX | FP0
```

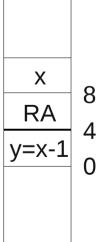
Statements (r* registers, ofs constant integer)

```
S ::=Mload(chunk, raddr, rres)
| Mstore(chunk, raddr, rval)
| Mgetstack(chunk, ofs, rres)
| Msetstack(chunk, ofs, rres)
| Mgetparam(chunk, ofs, rres)
| Mcall func | Mret
```

Mgoto label | Mlabel label: | ...

Mach

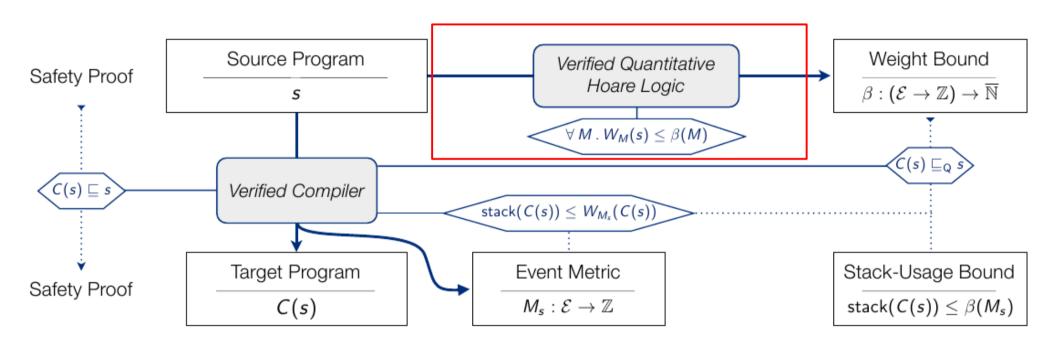
Mach2



Mach vs. Mach2

```
int g {...}
int g(int y);
                               int f {
                                 Mgetparam(Mint32, 0, EAX);
int f(int x) {
                                 Mop(Osubimm 1, EAX);
  return g(x-1)-2;
                                 Msetstack(Mint32, 0, EAX);
                                 Mcall(q);
}
                                 Mop(Osubimm 2, EAX);
      Mach
                        Mach2
                                 Mret
       X
                          X
              Memory
                             8
              injection
                         RA
                             4
      y=x-1
                        y=x-1
                             0
```

Overview



Quantitative program logic

- Hoare-like logic
- Assertions have values in {0, 1, 2, ..., ∞}
 - Represent available stack space
- {P} S {Q} roughly: if P stack space is available before S, then:
 - S does not stack overflow (unless P=∞), and
 - for all possible terminating executions of S,
 Q stack space is available after S

Assertions

- Clight statements S, continuations K, local state θ
- Global state ("heap" = CompCert memory state) H
- Mutable state $\sigma = (\theta, H)$
- Configuration $C = (S, K, \sigma)$
- Assertion P: C → {0, 1, 2, ..., ∞}
 - Coq implementation: C→N→Prop, represents sets of valid bounds

Selected rules

$$\frac{\{P\}\,S_1\,\{R\}}{\{P\}\,S_1;S_2\,\{Q\}}\,(Q\text{:SEQ})$$

$$\frac{c \geqslant 0 \quad \{P\} S \{Q\}}{\{P+c\} S \{Q+c\}}$$
(Q:Frame)

$$\frac{P \geqslant P' \qquad \{P'\}\,S\,\{Q'\} \qquad Q' \geqslant Q}{\{P\}\,S\,\{Q\}}\,(\text{Q:Conseq})$$

Selected rules

$$\frac{\Gamma(f) = (P, Q)}{\Gamma \vdash \{P + M(f)\} f() \{Q + M(f)\}}$$
(Q:Call)

$$\frac{\Gamma' = \Gamma, f: (P_f, Q_f) \qquad \Sigma(f) = S_f \qquad \Gamma' \vdash \{P\} S \{Q\} \qquad \Gamma' \vdash \{P_f\} S_f \{Q_f\}}{\Gamma \vdash \{P\} S \{Q\}}$$
(Q:Abstract)

Selected rules

With:

- Global variable addresses Δ
- Loop break

- Mutable state (θ, H)
- Return valueOne argument

those rules become:

$$\frac{\Gamma(f) = (P_f, Q_f) \qquad P = \lambda(\theta, H) \cdot P_f(\llbracket E \rrbracket_{(\theta, H)}^{\Delta}, H) \qquad Q = \lambda(\theta, H) \cdot Q_f(\llbracket x \rrbracket_{(\theta, H)}^{\Delta}, H)}{\Gamma \vdash \{P + M(f)\} x = f(E) \{(Q + M(f), \bot, \bot)\}}$$
(Q:CALL)

$$\frac{\Gamma' = \Gamma, f: (P_f, Q_f) \quad \Sigma(f) = (x, S_f)}{\Gamma' \vdash \{P\} S \{Q\} \quad \Gamma' \vdash \{P'\} S_f \{\bot, \bot, Q'\} \quad P' = \lambda(\theta, H) \cdot P_f(\theta(x), H) \quad Q' = \lambda(\theta, H) \cdot \lambda r \cdot Q_f(r, H)}{\Gamma \vdash \{P\} S \{Q\}}$$
(Q:Abstract)

But we also support:

- Several function arguments
 Auxiliary state
 Stack framing

See paper for more details.

Example with auxiliary state

```
\{Z = \log_2(\mathsf{h}_\sigma - \mathsf{I}_\sigma) \Rightarrow M_b \cdot Z)\}
bsearch(x,l,h) {
    if (h-l <= 1) return 1;
   \{(Z>0 \land Z = \log_2(\mathsf{h}_{\sigma}-\mathsf{I}_{\sigma})) \Rightarrow M_b \cdot Z\}
   m = 1+(h-1)/2:
   \{(Z>0 \land Z = \log_2(\mathsf{h}_\sigma - \mathsf{I}_\sigma) \land \mathsf{m}_\sigma = \frac{\mathsf{h}_\sigma + \mathsf{I}_\sigma}{2}) \Rightarrow M_b \cdot Z\}
   if (a[m]>x) h=m else l=m;
   \{[Z-1 = \log_2(\mathsf{h}_\sigma - \mathsf{I}_\sigma) \Rightarrow M_b \cdot (Z-1)] + M_b\}
   return bsearch(x,1,h);
   \{[M_b \cdot (Z-1)] + M_b\}
\{M_b \cdot Z\}
```

Soundness

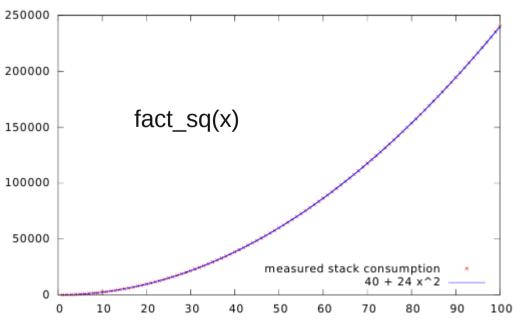
- "C consumes at most P stack space" iff for any t, C' such that C -t → * C', and for any metric M,
 W_M(t) ≤ P(C, M)
- If $\{P\}$ S $\{Q\}$ is derivable, then for any σ , (S, Kstop, σ) consumes at most P stack space
 - Stronger soundness: for any K, σ
 if (skip, K, σ) consumes at most Q stack space,
 then (S, K, σ) consumes at most P stack space
- Logic and soundness: 700 LOC Instantiation to Clight: 950 LOC

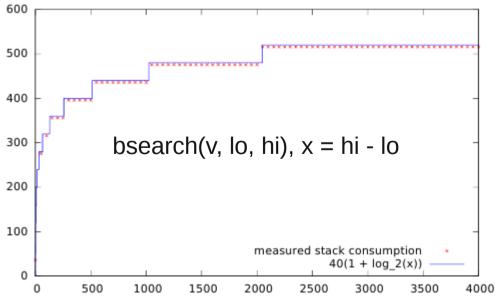
Accuracy

Function Name	Verified Stack Bound	
recid()	8a bytes	
bsearch(x, lo, hi)	$40(1 + \log_2(hi - lo))$ bytes	
fib(n)	24n bytes	
qsort(a, lo, hi)	48(hi - lo) bytes	
filter_pos(a, sz, lo, hi)	48(hi - lo) bytes	
sum(a, lo, hi)	32(hi - lo) bytes	
fact_sq(n)	$40 + 24n^2$ bytes	
filter_find(a, sz, lo, hi)	$128 + 48(hi - lo) + 40 log_2(BL)$ bytes	

Table 1. Manually verified stack bounds for C functions.

- Bound verified manually using our program logic, then instantiated by CompCert-generated stack frame sizes
- Actual stack consumption measured at run-time thanks to a stack monitor using ptrace (200 lines of C+Perl)
- 4 bytes difference due to space reserved for RA in the last callee's stack frame





Automatic stack analyzer

- For C code without recursion (e.g. MISRA C), program logic can be automatically applied to derive stack bound
 - 500 lines of Coq
- Instrumented compiler to generate both compiled code and stack bound
 - 400 lines of Coq + 500 Ocaml

Automatic stack analyzer

```
Let lift0 {A B C: Type} (f: A -> B -> C) (ox: option A) (oy: option B): option C := ...
Fixpoint B M Γ (s: stm): option nat := match s with | scall _ f _ => lift0 plus (Some (M f)) (Γ f) | sseq s1 s2 => lift0 max (B M Γ s1) (B M Γ s2) | sif _ st sf => lift0 max (B M Γ Phi st) (B M Γ sf) | sloop s => B M Γ s | _ => Some 0 end.
```

```
• Lemma sound B:
    forall M \overline{\Gamma} (CVALID: valid bctx M \Gamma) s n
             (BS: B M \Gamma s = Some n),
    valid bound M s n.
 Proof.
  induction s; intros; ...
  + apply sound skip.
  + apply sound_ret with (Q := fun => mkassn 0).
  + apply sound break.
  + ... apply sound_seq with (Q := fun => mkassn (max x y)) ...
 apply valid max I ... apply valid max r ...
  + case eq (\Gamma f) ... eapply valid le; [apply Le.le n Sn |].
    eapply sound consequence;
    [| apply sound call2
     with (C := \Gamma)
         (Pg := fun pre phif)
         (Qg := fun post phif)
         (L := fun => True)].
    ... eapply CVALID; eauto.
   + eapply sound_consequence;
   [| apply sound_loop
     with (I := fun _ => mkassn n)
         (Q := fun _ => mkassn n)
   ]; unfold mkassn; intuition. ...
  eapply IHs; eauto.
 Oed.
```

Automatic stack analyzer: soundness

```
Let lift0 {A B C: Type} (f: A -> B -> C)
                                                 • Fixpoint bound of lvl ge M
(ox: option A) (oy: option B): option C :=
                                                     (lvl: nat) f :=
                                                     match lvl with
                                                        0 \Rightarrow None
Fixpoint B M \Gamma (s: stm): option nat :=
  match s with
                                                        S lvl' =>
  | scall f =>
                                                          match find func ge f with
     liftO plus (Some (M f)) (\Gamma f)
                                                           | Some bdy =>
  | sseq s1 s2 =>
                                                            B M (bound of lvl ge M lvl') bdy
     liftO max (B M Γ s1) (B M Γ s2)
                                                           None => None
  | sif st sf =>
                                                          end
    liftO max (B M \( \text{Phi st} \) (B M \( \text{sf} \)
                                                     end.
    sloop s \Rightarrow B M \Gamma s
   => Some 0
  end.
                                                 • Theorem bound lvl sound:
                                                     forall ge M 1,
Lemma sound B:
  forall M \overline{\Gamma} (CVALID: valid bctx M \Gamma) s n
                                                      valid bctx M (bound of lvl ge M 1).
          (BS: B M \Gamma s = Some n),
                                                   Proof.
  valid bound M s n.
                                                     induction 1.
                                                     ... apply sound B ... apply IHl ...
                                                   Oed.
```

Automatic stack analyzer: "completeness"

```
Fixpoint bound_of_lvl ge M
  (lvl: nat) f :=
   match lvl with

| 0 => None
  | S lvl' =>
        match find_func_ ge f with
        | Some bdy =>
            B M (bound_of_lvl ge M lvl') bdy
        | None => None
        end
end.
```

```
• Theorem bound of lvl complete:
   forall M p
   (CLOSED: ... p ...)
   (CG WELLFOUNDED:
     forall id fi,
     In (id, Gfun fi) p.(prog defs) →
     forall id',
     in stm id' fi.(fi body) →
     id' < id)
   lvl f
   (LVL: f < lvl)
   fi
   (FDEF: In (f, Gfun fi) p.(prog defs)),
   exists n,
     bound of lvl
      (Genv.globalenv p) M
      lvl f = Some n.
```

Automatic stack bounds

File Name /	Function Name	Verified
Line Count		Stack Bound
mibench/net/dijkstra.c	enqueue	40 bytes
(174 LOC)	dequeue	40 bytes
	dijkstra	88 bytes
mibench/auto/bitcount.c	bitcount	16 bytes
(110 LOC)	bitstring	32 bytes
mibench/sec/blowfish.c	BF_encrypt	40 bytes
(233 LOC)	BF_options	8 bytes
	BF_ecb_encrypt	80 bytes
mibench/sec/pgp/md5.c	MD5Init	16 bytes
(335 LOC)	MD5Update	168 bytes
	MD5Final	168 bytes
	MD5Transform	128 bytes
mibench/tele/fft.c	IsPowerOfTwo	16 bytes
(195 LOC)	NumberOfBitsNeeded	24 bytes
	ReverseBits	24 bytes
	fft_float	160 bytes

certikos/vmm.c	palloc	48 bytes
(608 LOC)	pfree	40 bytes
	mem_init	72 bytes
	pmap_init	176 bytes
	pt_free	80 bytes
	pt_init	152 bytes
	pt_init_kern	136 bytes
	pt_insert	80 bytes
	pt_read	56 bytes
	pt_resv	120 bytes
certikos/proc.c	enqueue	48 bytes
(819 LOC)	dequeue	48 bytes
	kctxt_new	72 bytes
	sched_init	232 bytes
	tdqueue_init	208 bytes
	thread_init	192 bytes
	thread_spawn	96 bytes
compcert/mandelbrot.c	main	56 bytes
(92 LOC)	advance	90 bytes
compcert/nbody.c	707 707 707	80 bytes
(174 LOC)	energy	56 bytes
	offset_momentum	24 bytes
	setup_bodies	16 bytes
	main	112 bytes

Table 2. Automatically verified stack bounds for C functions.

Conclusion

- Stack overflow need not be enforced by source semantics
 - Stack consumption as add-on to existing operational semantics
- Yet, stack consumption can be verified at the source level and preserved by compilation
- Paves the way for other quantitative properties:
 - Malloc/free heap memory consumption
 - clock cycles, energy...

Thank you!

 Paper (accepted to PLDI 2014, to appear), TR, Coq development and artifact VM: http://cs.yale.edu/~tahina/certikos/stack

 For any questions: tahina.ramanandro@yale.edu



Function inlining

```
void h();
g() { h(); return 1;}
f() { int i=g(); return i+1; }

* Call(f)::
call(g)::
call(h):: return(h)::
return(g)::
return(f):: nil
void h();
f() { int i=(h(), 1);
return i+1; }

* Call(f)::
call(h):: return(h)::
return(f):: nil
```

• Events are removed in matching pairs

Function inlining

$$(\mathsf{call}(f) \cdot T, \theta) \leadsto (T, \mathsf{call}(f) \cdot \theta)$$

$$(\mathsf{ret}(f) \cdot T, \mathsf{call}(f) \cdot \theta) \leadsto (T, \theta)$$

With θ finite and only containing call events

Coinductively:

$$\epsilon \sqsubseteq_{\theta} \epsilon
e \cdot T' \sqsubseteq_{\theta} t \cdot e \cdot T \qquad \text{if } T' \sqsubseteq_{\theta'} T
\text{and } (t \cdot e \cdot T, \theta) \leadsto^* (e \cdot T, \theta')
\epsilon \sqsubseteq_{\theta} T \qquad \text{if } \epsilon \sqsubseteq_{\theta'} T'
\text{and } (T, \theta) \leadsto^+ (T', \theta')$$

- If $T' \sqsubseteq_{\theta} T$, then
 - for t' finite prefix of T'there is t finite prefix of Tsuch that $V_{M}(t') - V_{M}(\theta) \le V_{M}(t)$
 - So, $W_M(T') - W_M(\theta) \le W_M(T)$
- Thus, it suffices to prove that for any T' of the target, there is T of the source such that T'
 ⊆_E T

Tailcall recognition

- Caller produces return event before transferring to tail-callee
- call(f) :: return(f) :: call(g) :: return(g) :: call(h) :: return(h)

Tailcall recognition

With θ finite and only containing return events

Coinductively:

$$\begin{array}{cccc} \epsilon \sqsubseteq_{\theta} \epsilon \\ & e \cdot T' \sqsubseteq_{\theta} e \cdot T & \text{if } T' \sqsubseteq_{\theta} T \\ & \operatorname{ret}(f) \cdot \epsilon \sqsubseteq_{\theta} \epsilon \\ & \operatorname{ret}(f) \cdot e \cdot T' \sqsubseteq_{\theta} e \cdot T & \text{if } T' \sqsubseteq_{\operatorname{ret}(f) \cdot \theta} T \\ & T' \sqsubseteq_{\operatorname{ret}(f) \cdot \theta} \operatorname{ret}(f) \cdot T & \text{if } T' \sqsubseteq_{\theta} T \end{array}$$

- If T' \sqsubseteq_{θ} T, then
 - for t' finite prefix of T'there is t finite prefix of Tsuch that $V_{M}(t') + V_{M}(\theta) \le V_{M}(t)$
 - So, $W_{M}(T') + W_{M}(\theta) \leq W_{M}(T)$

Function inlining and tailcall recognition

- Need to modify simulation diagrams to take special refinement relations into account
- Proof in progress

Mach configuration

- Continuations
 K ::= Knil | Kcons(SP, f, code, RA, K)
- Configurations
 C ::= State(mem, rset, SP, f, code, K)
 | Callstate(mem, rset, f, K)
 - | Returnstate(mem, rset, K)
- Callstate/Returnstate correspond to CompCert assembly Pallocframe/Pfreeframe pseudos

Mach2 configuration

- ContinuationsK ::= Knil | Kcons(f, code, RA, K)
- Configurations
 C ::= State(mem, rset, SP, f, code, K)
 | Callstate(mem, rset, f, K)
 - | Returnstate(mem, rset, K)
- Callstate/Returnstate do not modify the stack

Thank you!

 Paper (accepted to PLDI 2014, to appear), TR, Coq development and artifact VM: http://cs.yale.edu/~tahina/certikos/stack

 For any questions: tahina.ramanandro@yale.edu

