



Cosmology and quantum simulation

Non separability of phonon pairs in a time-modulated BEC linked to
inflationary scenario

Victor Gondret, Charlie Leprince, Quentin Marolleau,
Denis Boiron & Chris Westbrook

EDOM Days



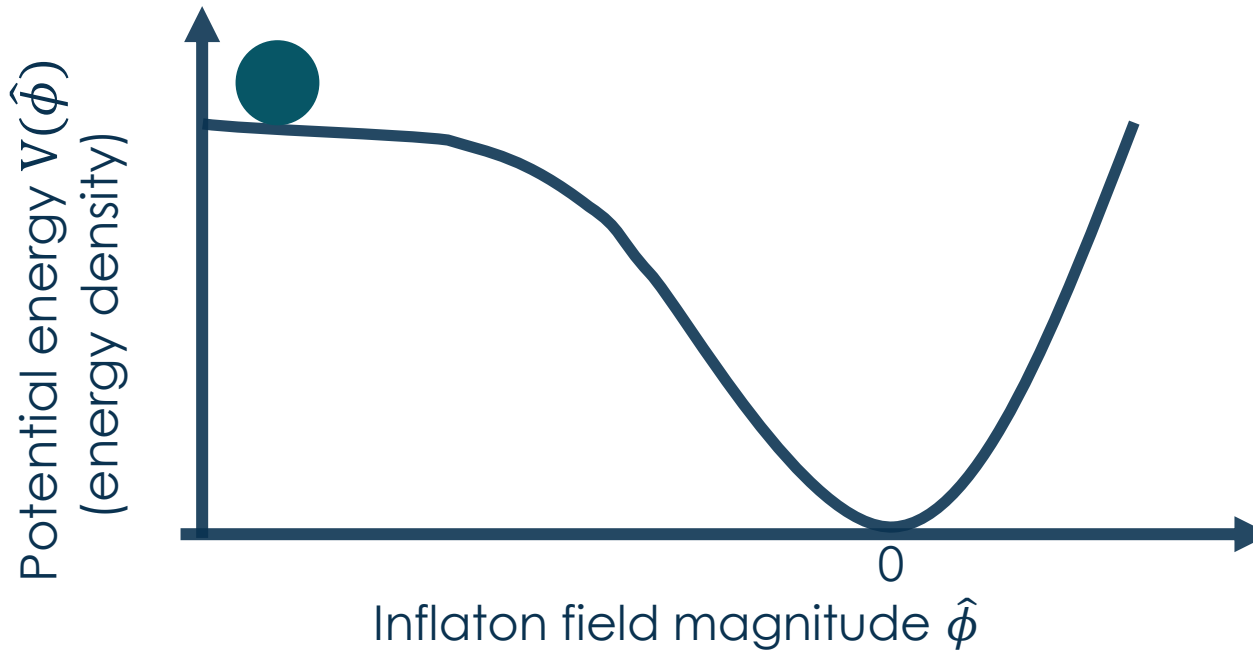
ÉCOLE DOCTORALE
Ondes
et matière
(EDOM)



Theory of Inflation

Add a new field $\hat{\phi}$ called *inflaton*

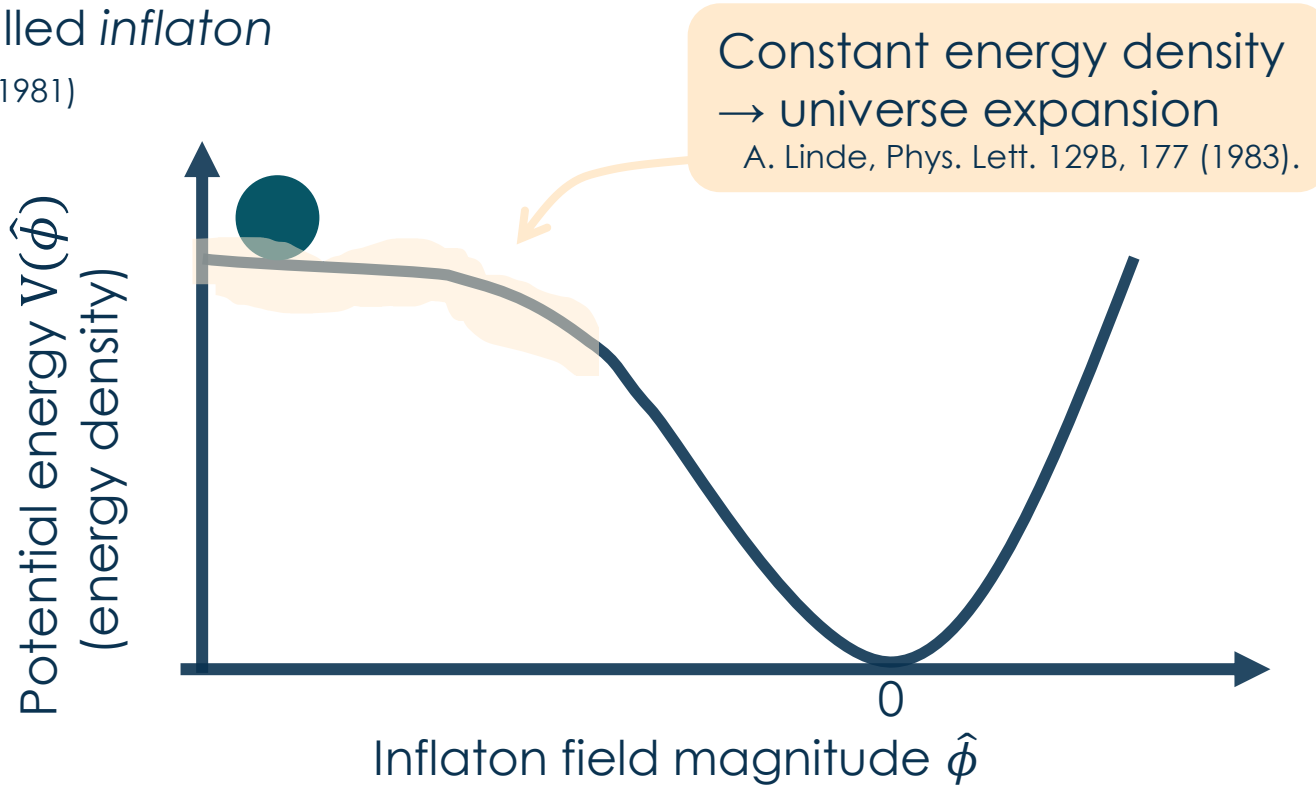
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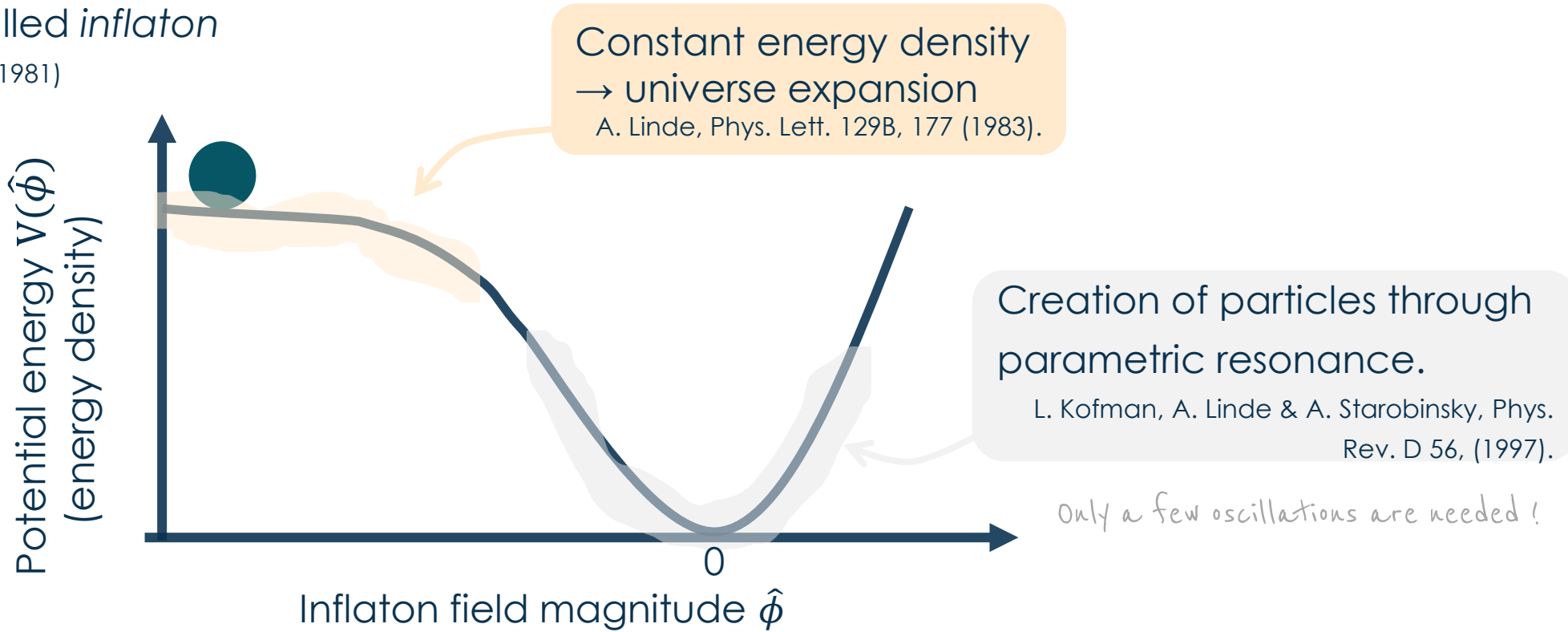
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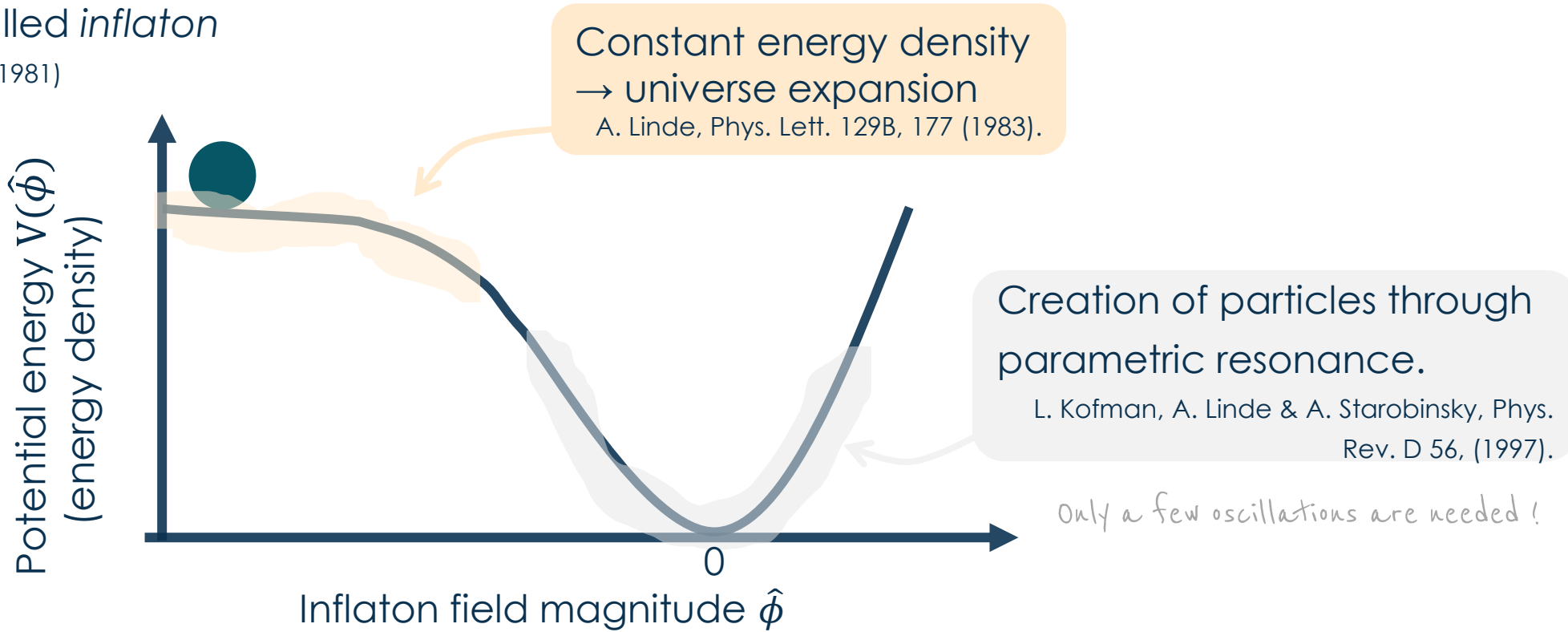
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Interactions lead to decoherence and thermalization

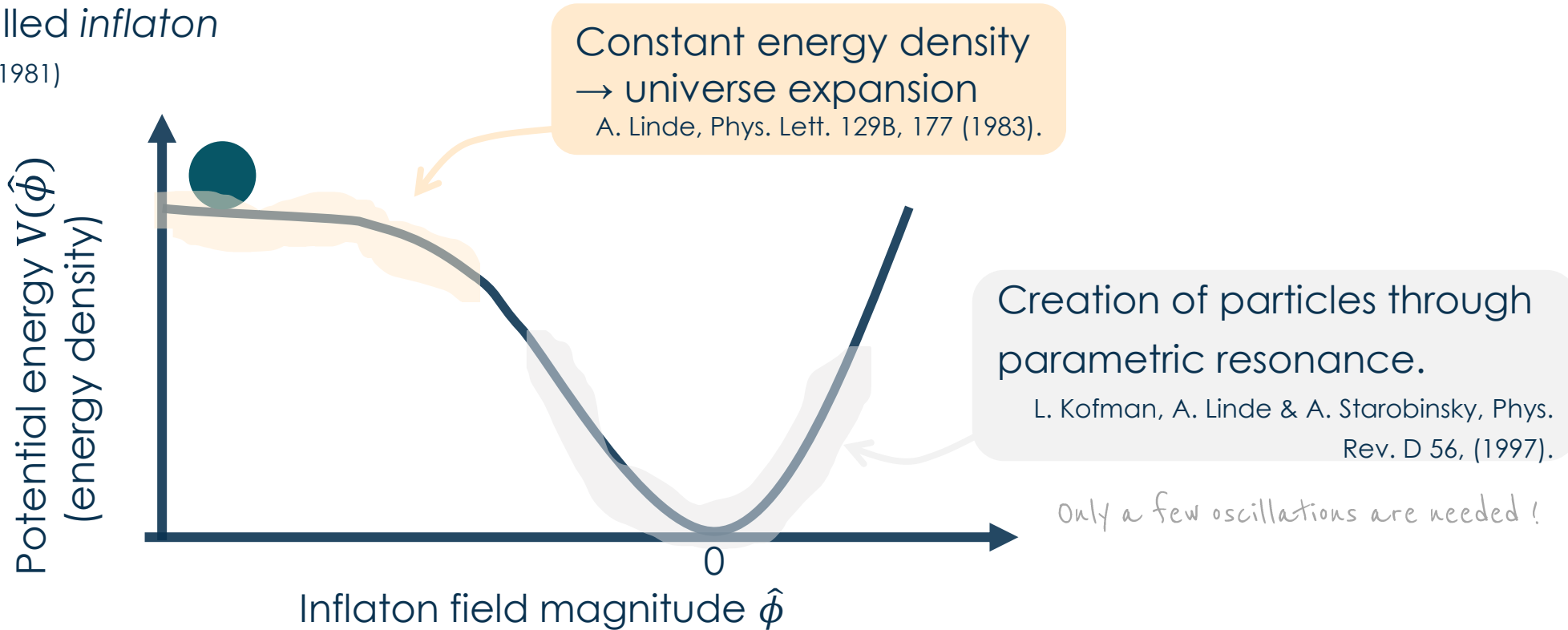
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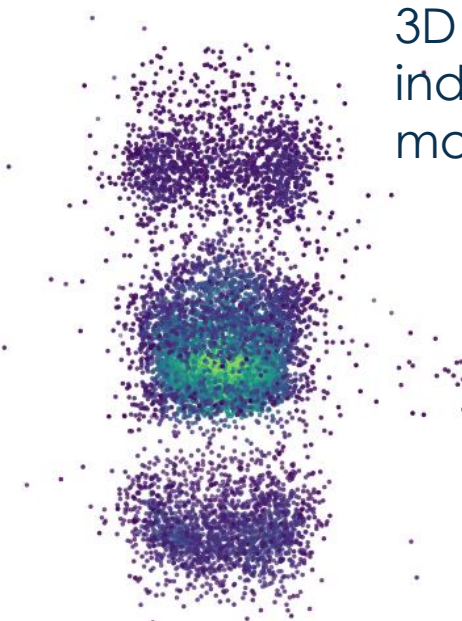
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Not experimentally accessible :
need for analogous phenomena

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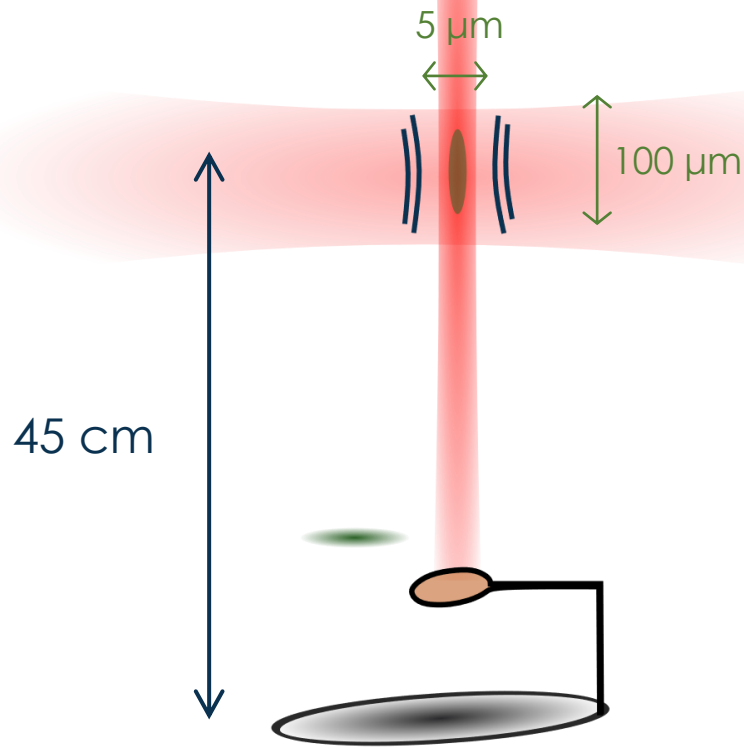
Detection of BEC of metastable helium atoms

3D reconstruction of individual atoms momentum



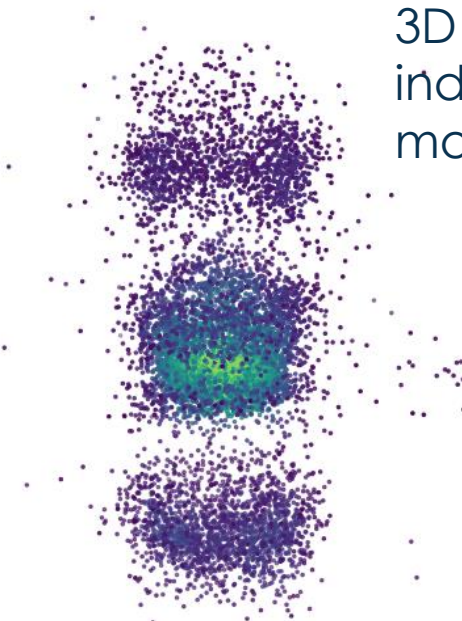
Cigar shape BEC in a crossed dipole trap

- $\omega_{\parallel} = 70 \text{ Hz}$
- $\omega_{\perp} = 1,3 \text{ kHz}$



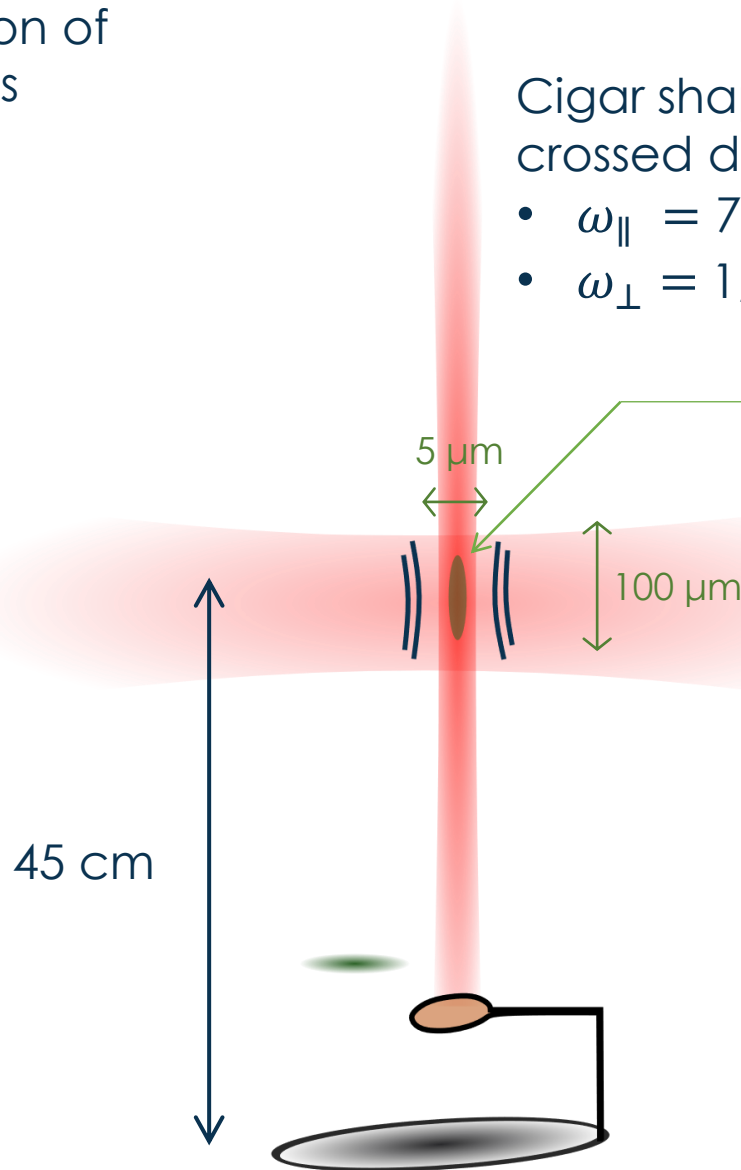
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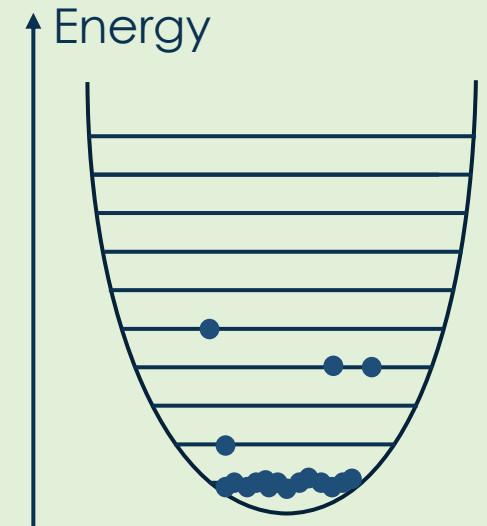


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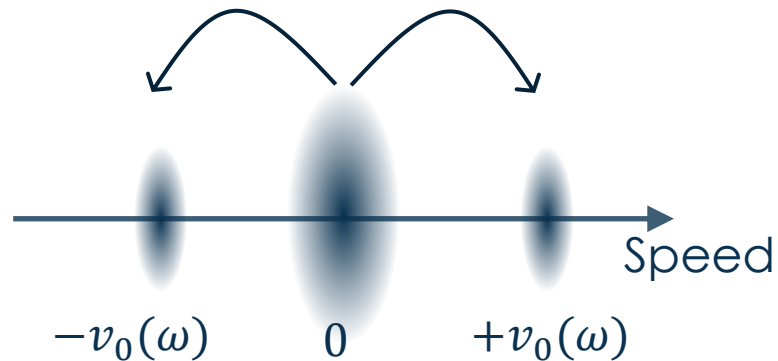
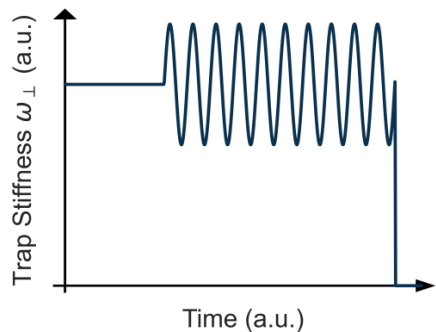
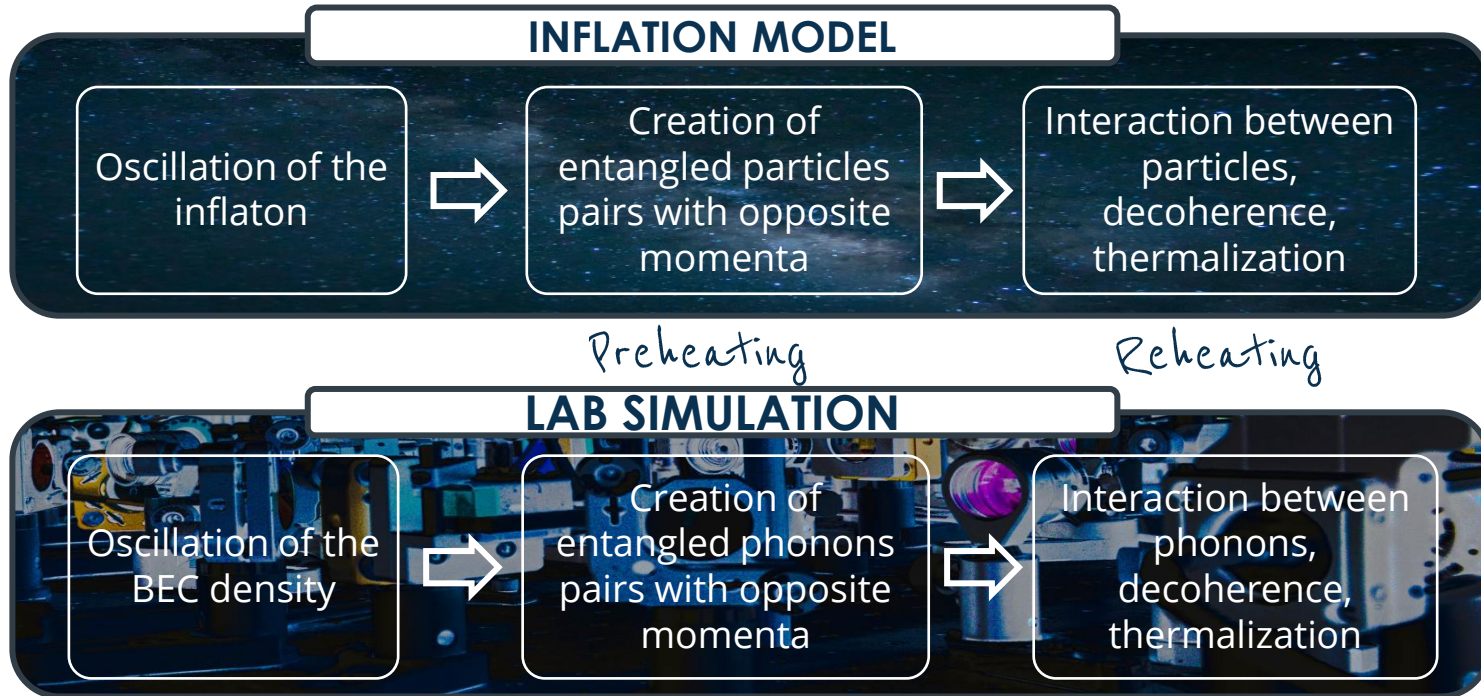
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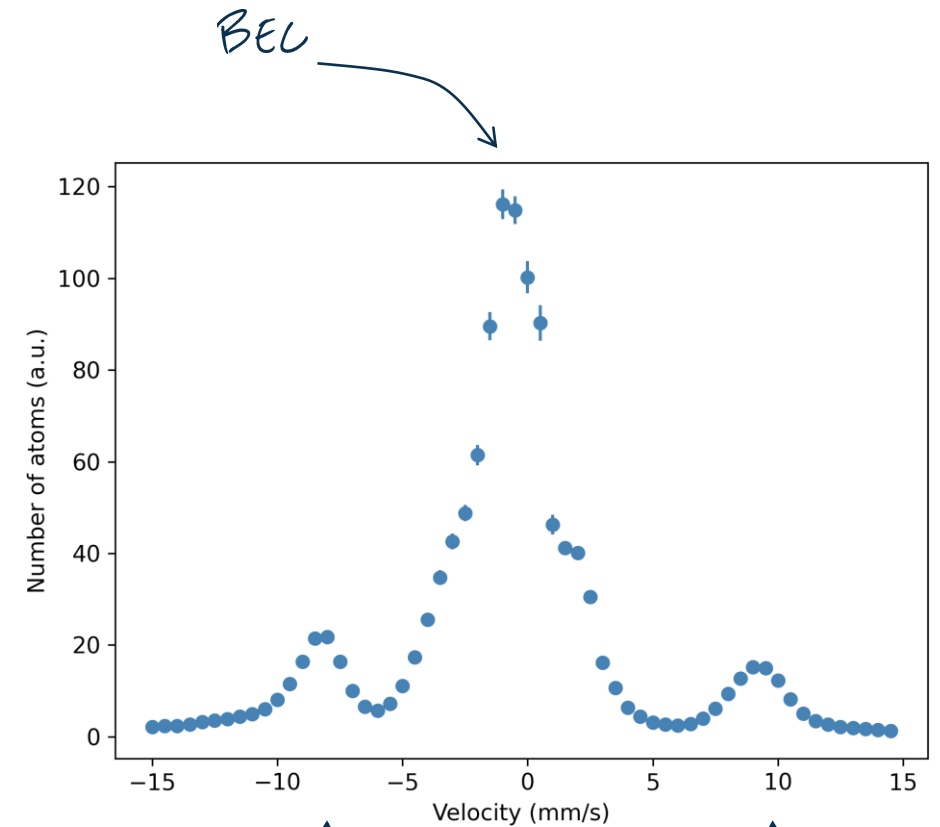
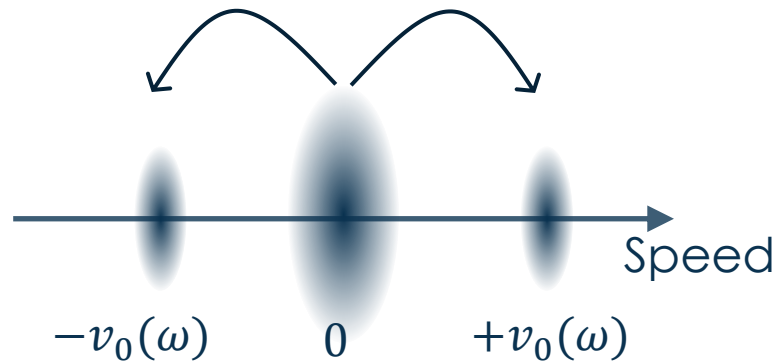
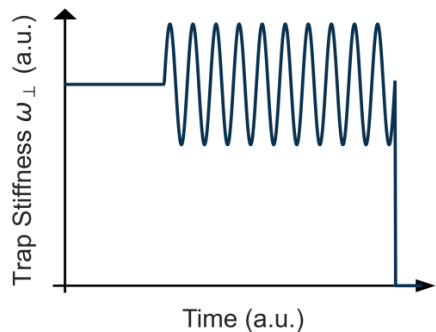
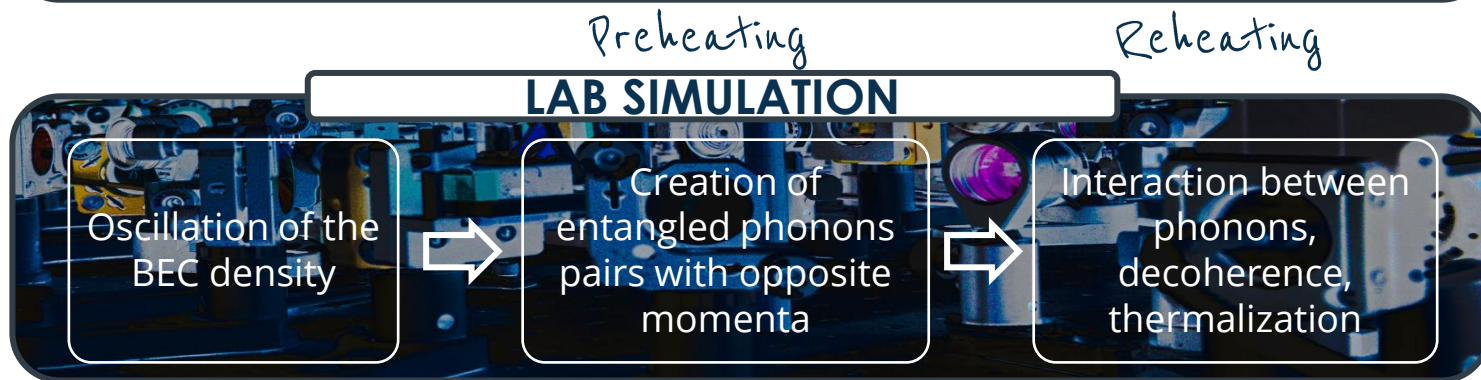
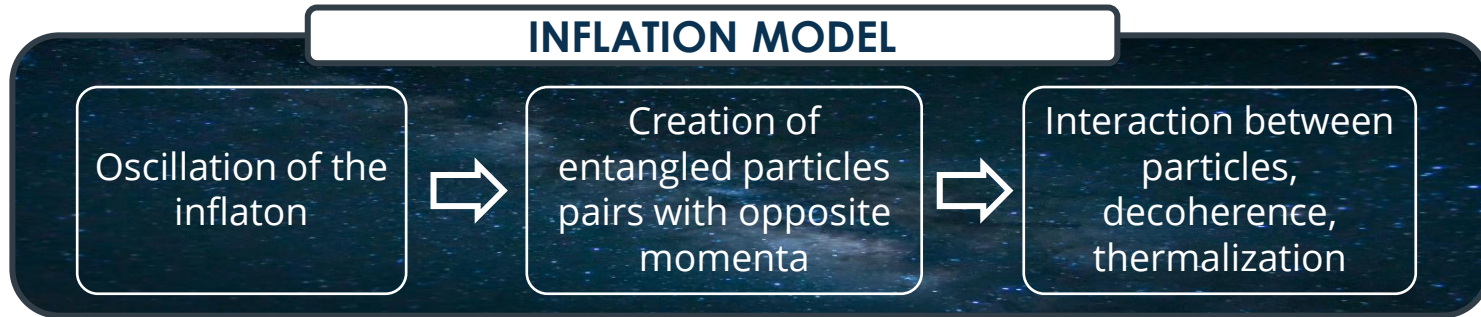
BEC is a macroscopic state at $k=0$



BEC for analog inflation



BEC for analog inflation



Phonon pairs !

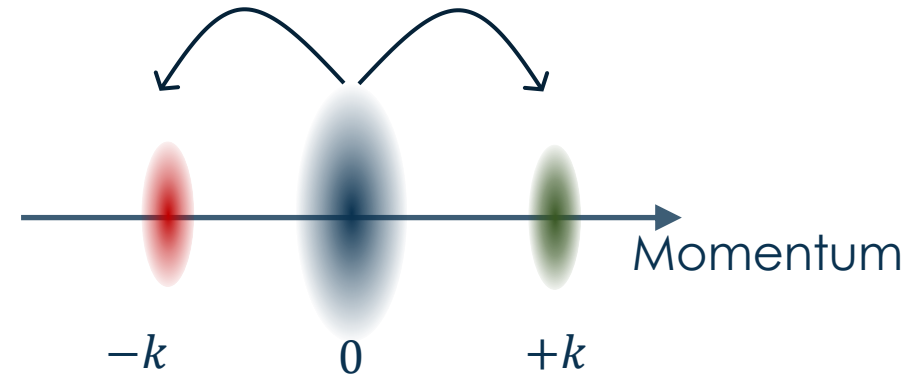
Probing correlations

Second order
correlation function :

$\langle \dots \rangle$: average over
experimental realizations

$$g^{(2)}(-k, k) = \frac{\langle n_{-k} n_k \rangle}{\langle n_{-k} \rangle \langle n_k \rangle}$$

$g^{(2)}(k, -k) > 2$ is *a priori* needed
to claim for entanglement



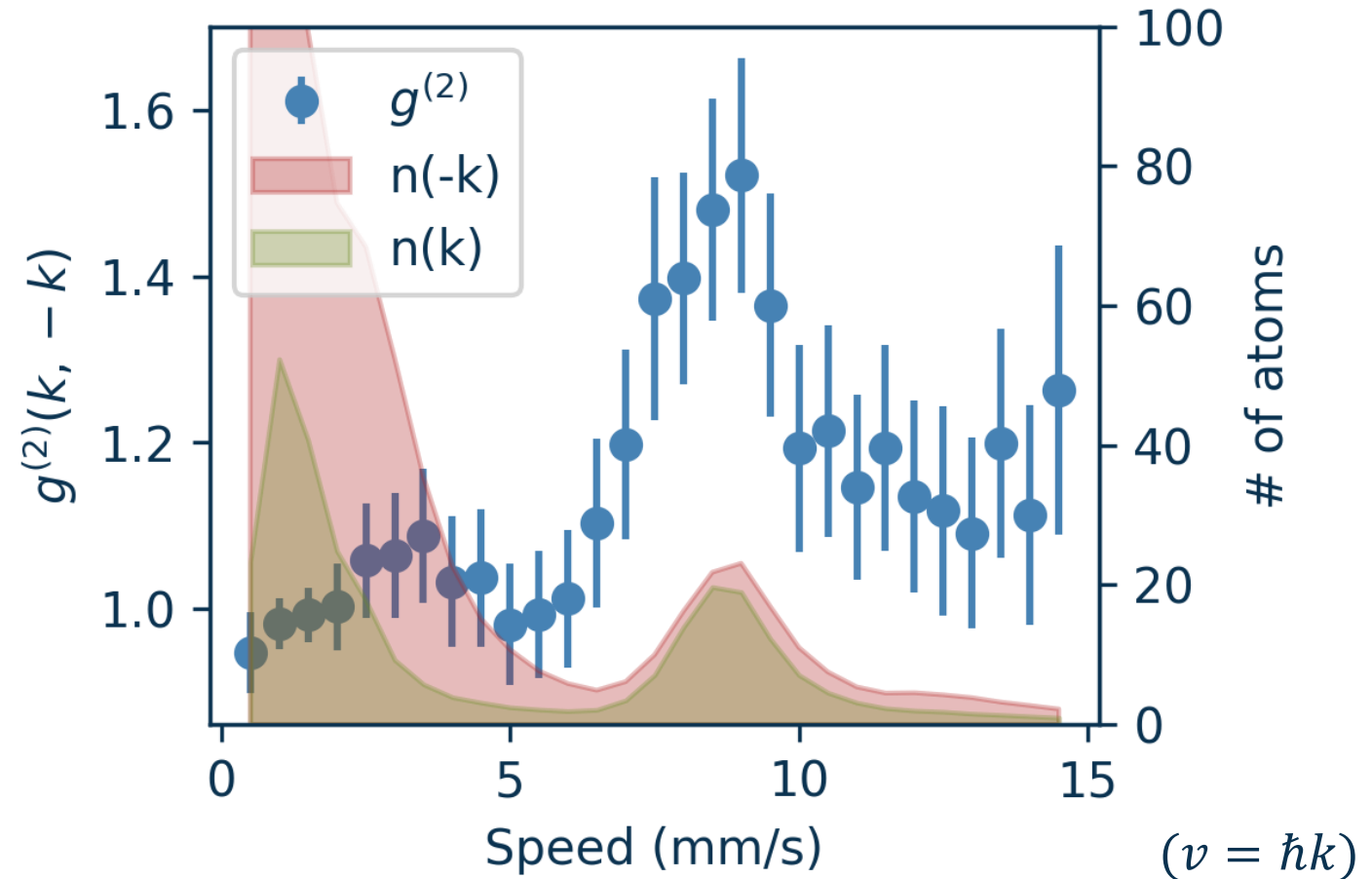
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Probing correlations

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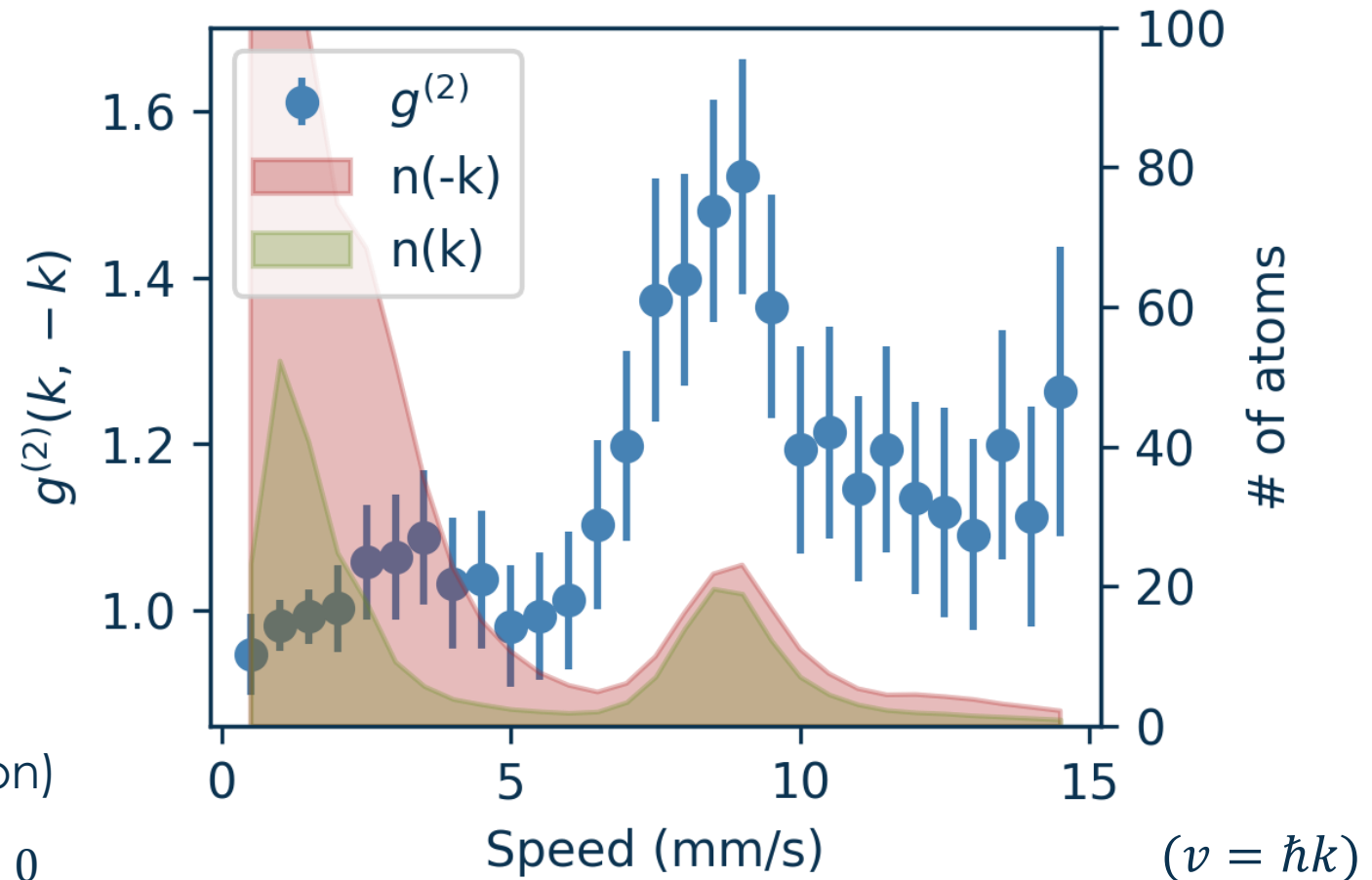
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Perspectives

- 💡 Decrease the temperature
- 💡 Decrease the # of oscillations ($\downarrow$ population)
- 💡 Check $g^{(2)} > 2 \leftrightarrow$ entanglement : $\hat{a}_k \hat{a}_{-k}^\dagger = 0$
- 💡 Study the thermalization



Thank you for your time !

On the experimental side



Some lecture

- S. Watson, *An Exposition on Inflationary Cosmology*, 2000
- J.-C. Jaskula et al., Phys. Rev. Lett. **109**, 220401 (2012).
- S. Robertson, F. Michel, and R. Parentani, Phys. Rev. D **95**, 065020 (2017).
- A. Micheli and S. Robertson, Phys. Rev. B **106**, 214528 (2022).

On the theory side



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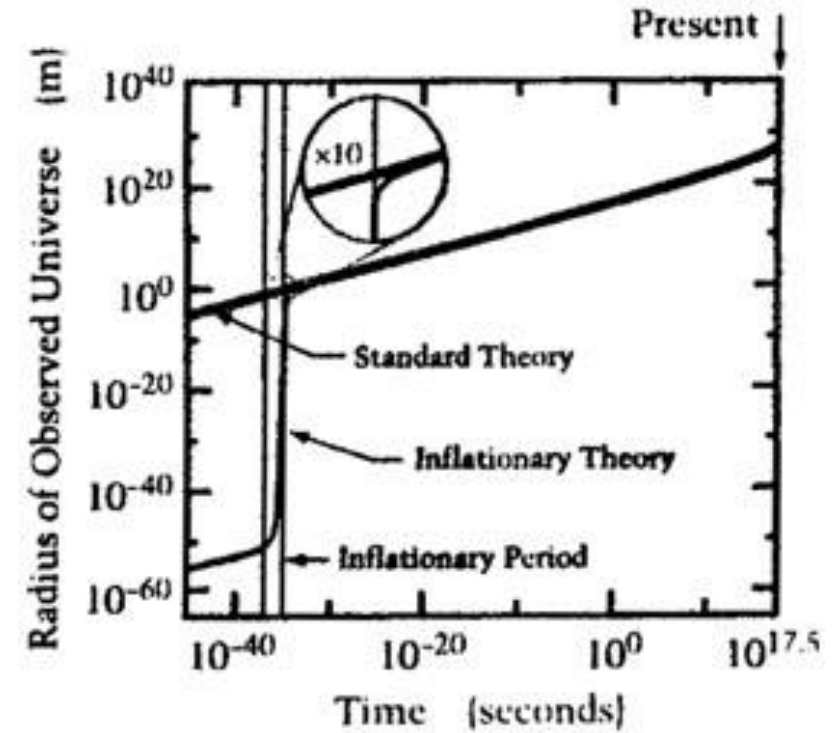
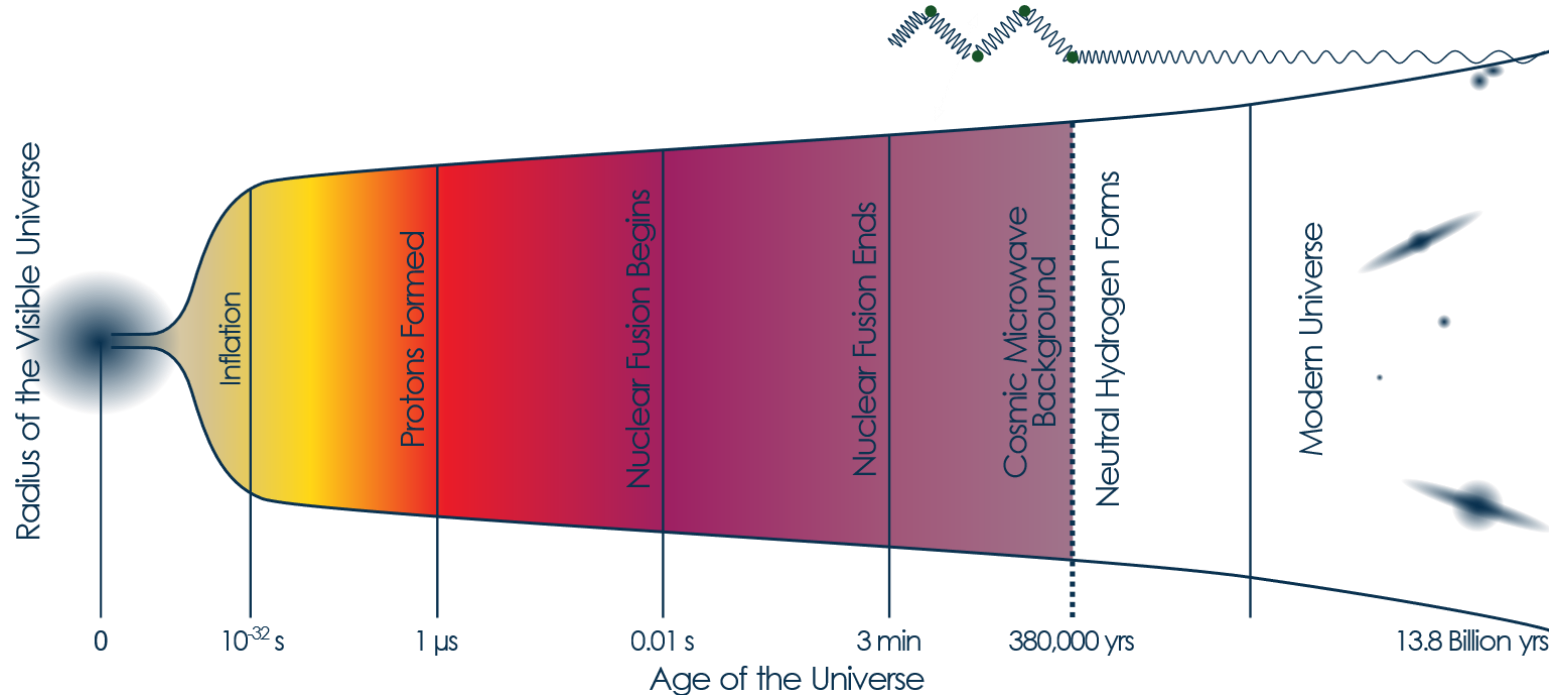
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Theory of Inflation



Large scale homogeneity of the universe is not explained by the standard model of cosmology.

Guth, A.H., 1981. *Inflationary universe: A possible solution to the horizon and flatness problems*. Phys. Rev. D 23, 347–356.

PHYSICAL REVIEW LETTERS

VOLUME 46

25 MAY 1981

NUMBER 21

Experimental Black-Hole Evaporation?

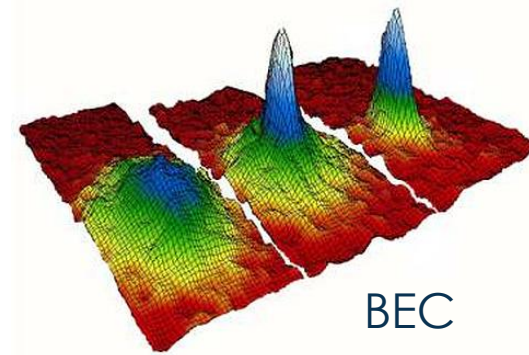
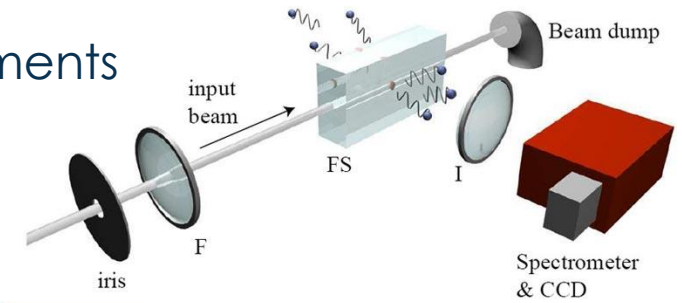
W. G. Unruh

Department of Physics, University of British Columbia, Vancouver, British Columbia V6T2A6, Canada

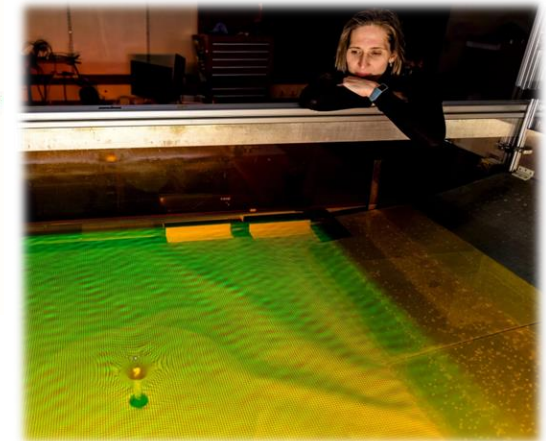
(Received 8 December 1980)

It is shown that the same arguments which lead to black-hole evaporation also predict that a thermal spectrum of sound waves should be given out from the sonic horizon in transsonic fluid flow.

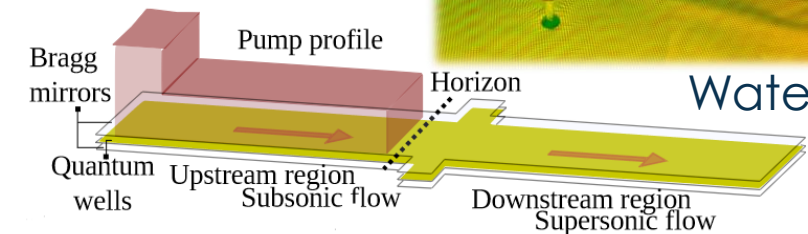
Ultrashort laser pulse filaments



BEC



Water tank



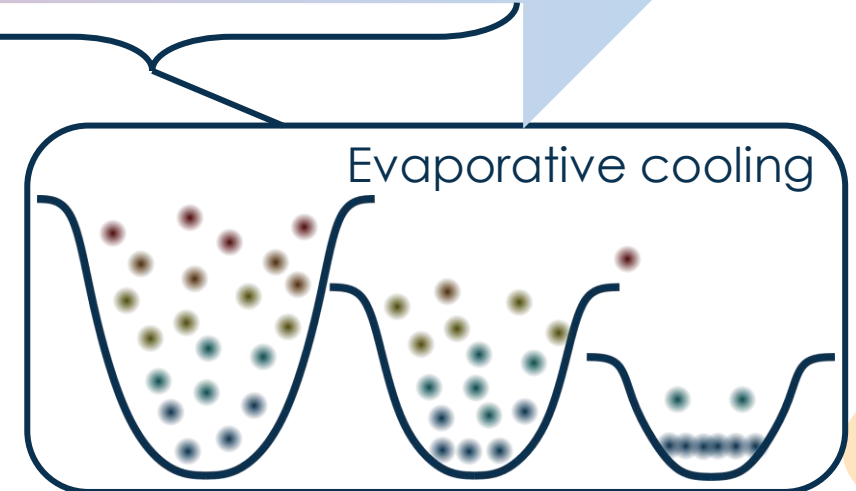
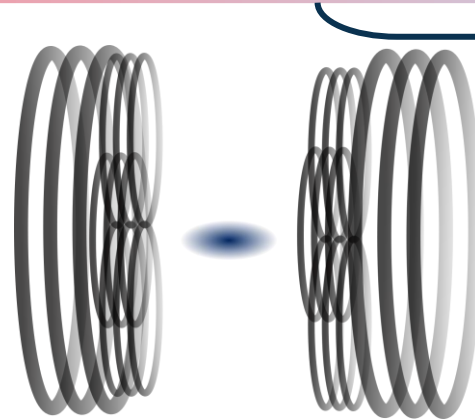
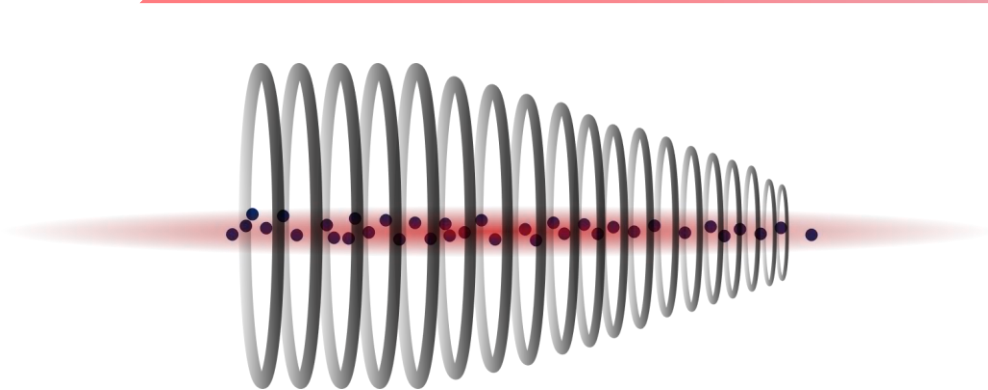
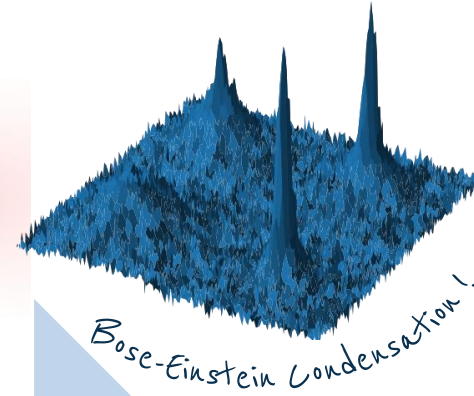
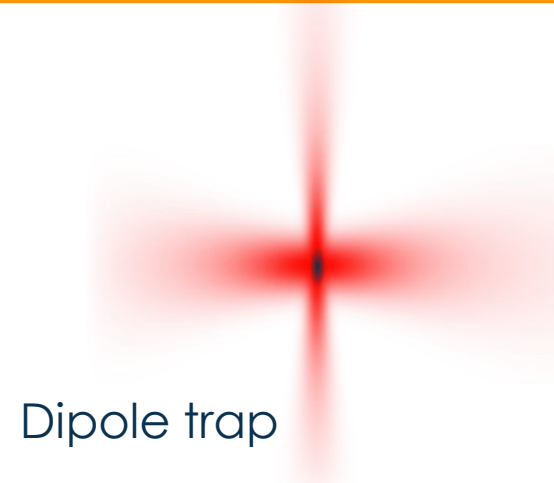
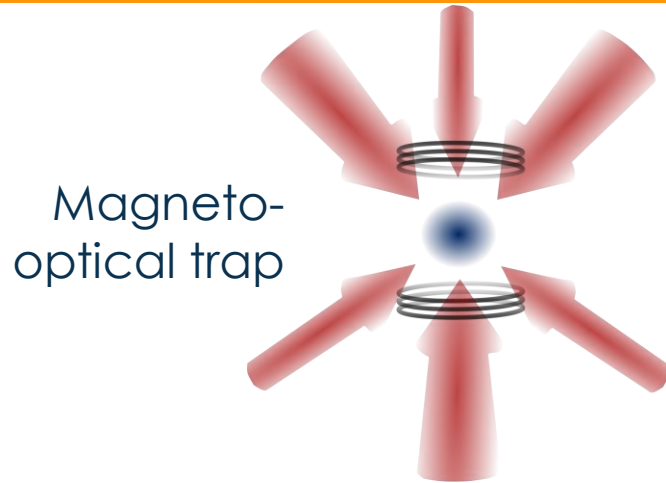
Polariton superfluid

F. Belgiorno, et al. Phys. Rev. Lett. 105.20 (2010): 203901.

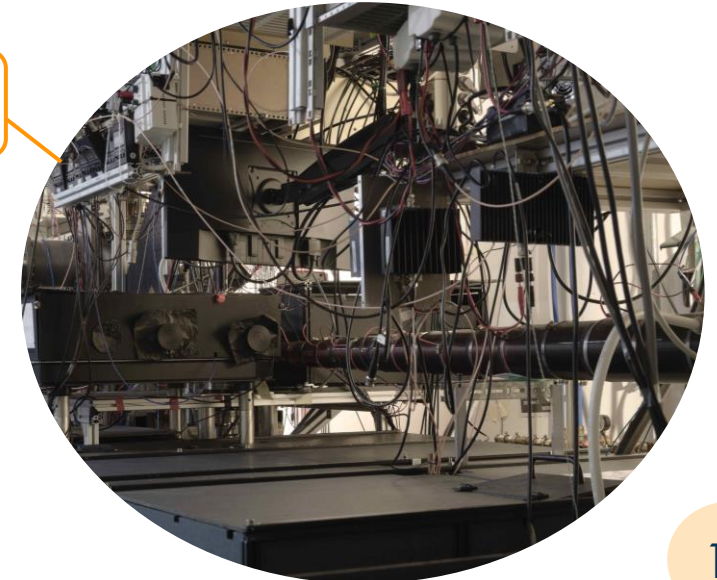
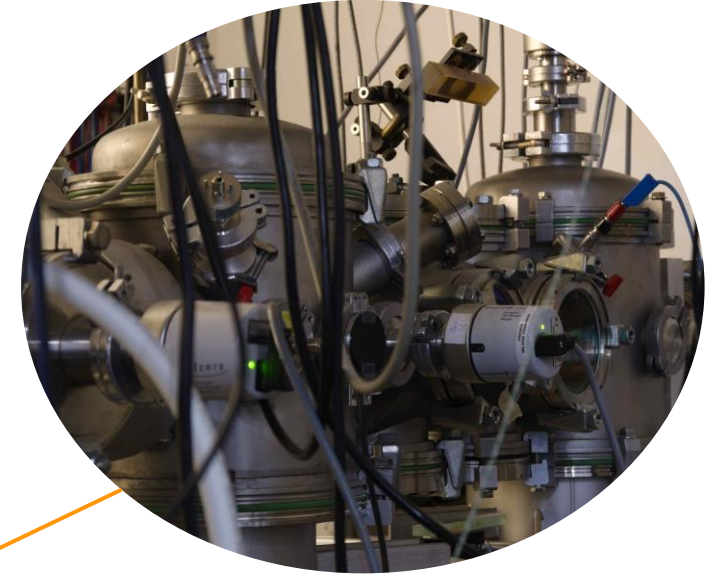
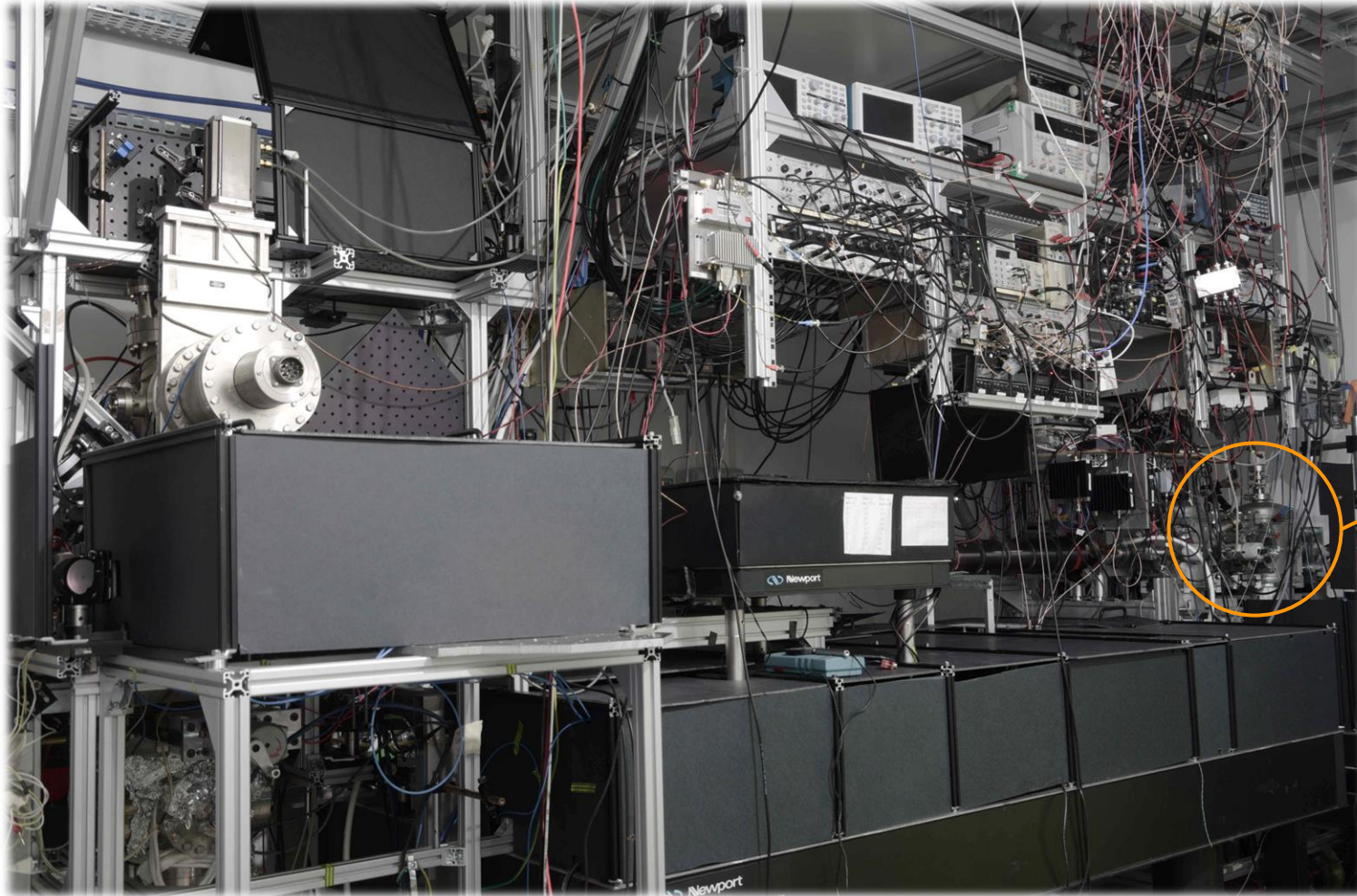
M. Jacquet et al., Eur. Phys. J. D **76**, 152 (2022).

S. Weinfurter et al., Phys. Rev. Lett. **106**, 021302 (2011).

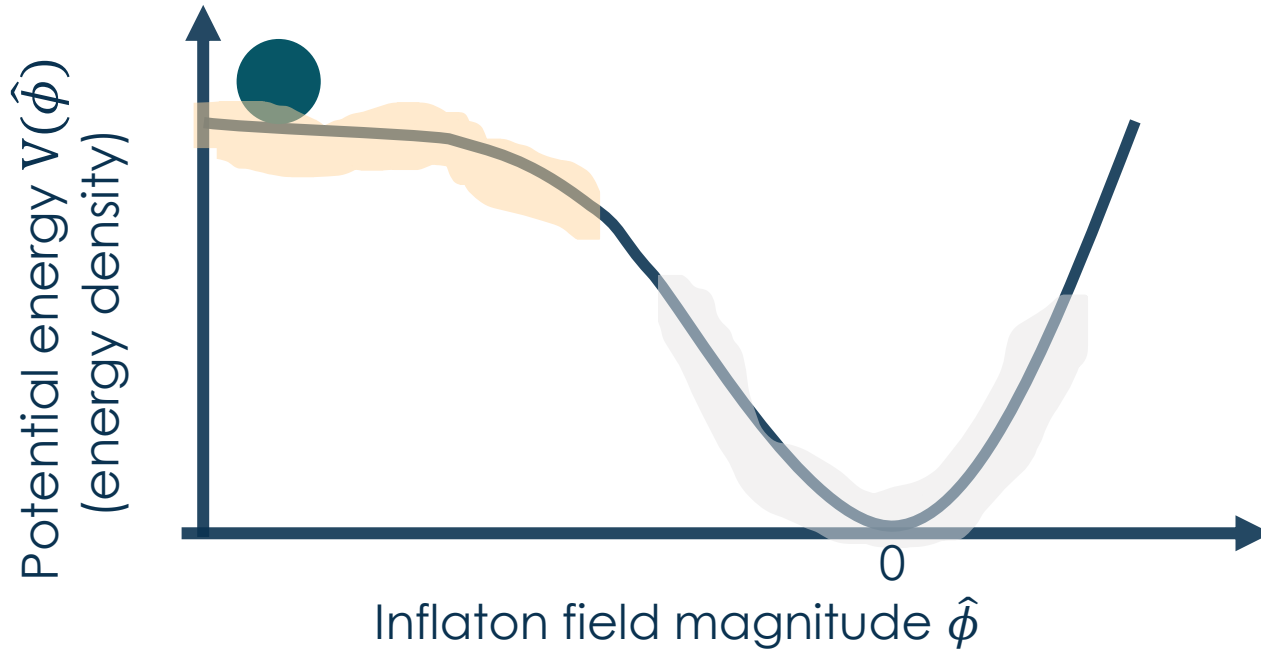
An experimental cycle



Experimental setup



Theory of Inflation



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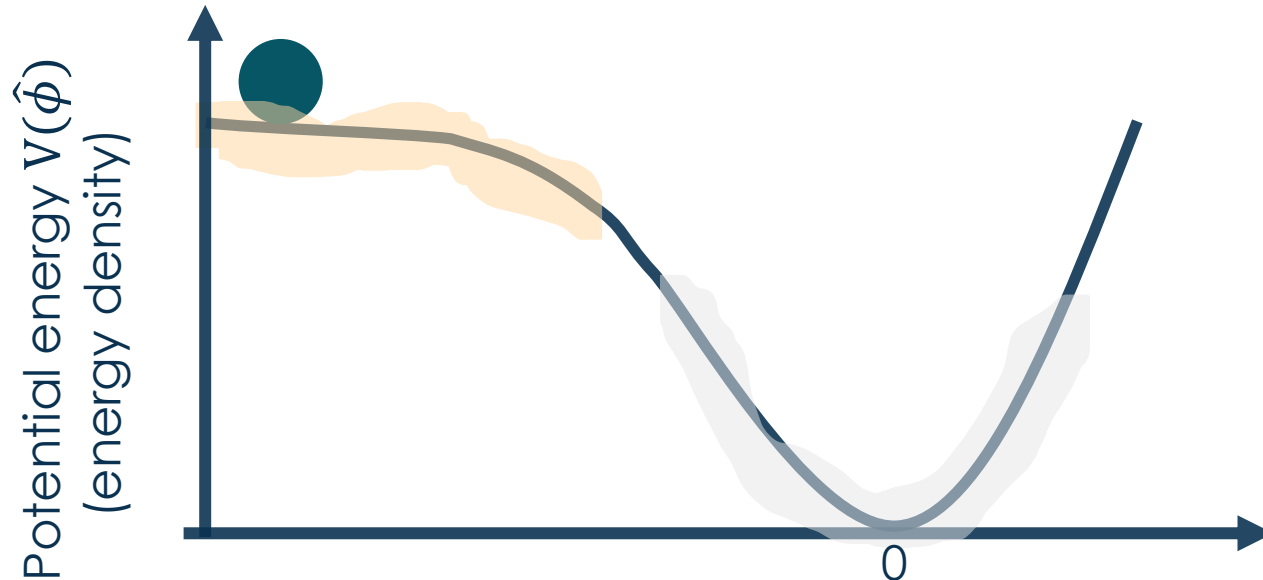
The inflaton starts to oscillate around its minimum and, coupled to matter fields, it creates particles through parametric resonance.

L. Kofman, A. Linde & A. Starobinsky, Phys. Rev. D 56, (1997).

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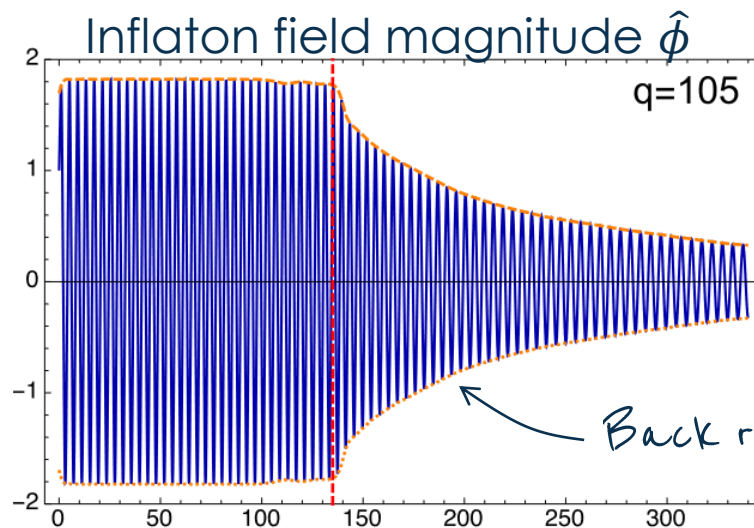
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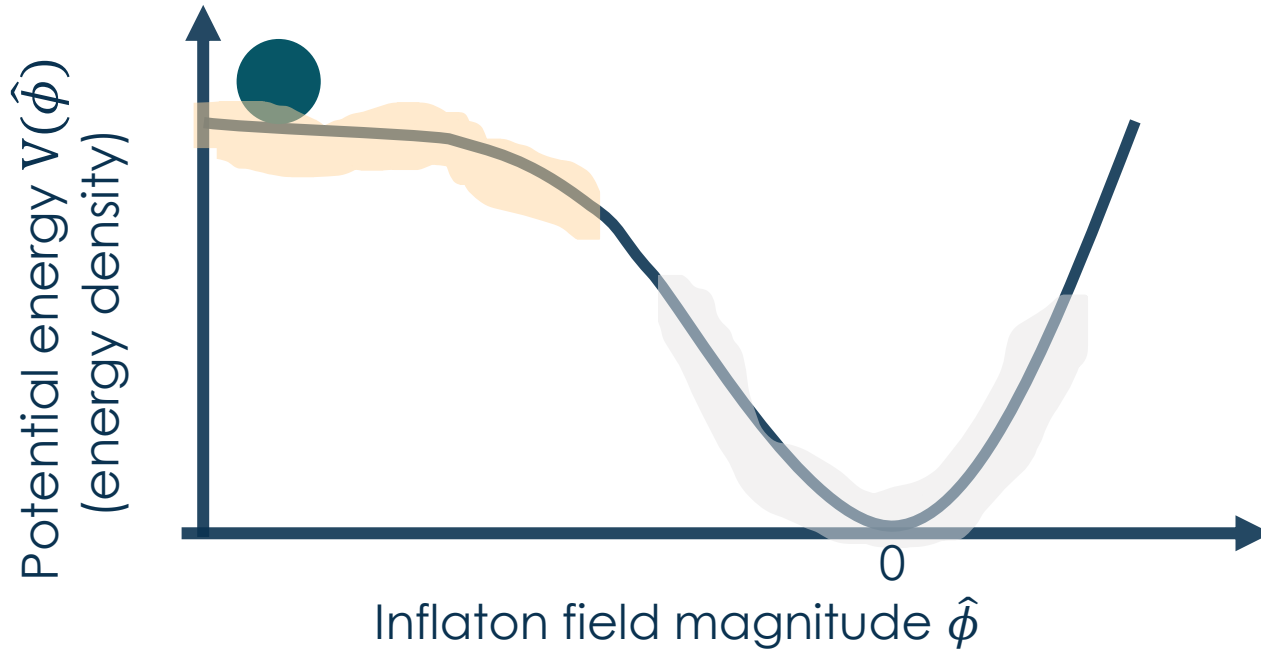
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Decay of the inflaton field into particles



Theory of Inflation



$$V(\phi) = \lambda(\phi^2 - M^2)^2$$

Higgs potential

$$V(\phi) = \frac{1}{2}m^2\phi^2$$

Massive scalar field

$$V(\phi) = \lambda\phi^4$$

Self interacting scalar field

$$V(\phi) = 2H_i^2 \left(3 - \frac{1}{s}\right) e^{-\phi/\sqrt{s}}$$

String theory

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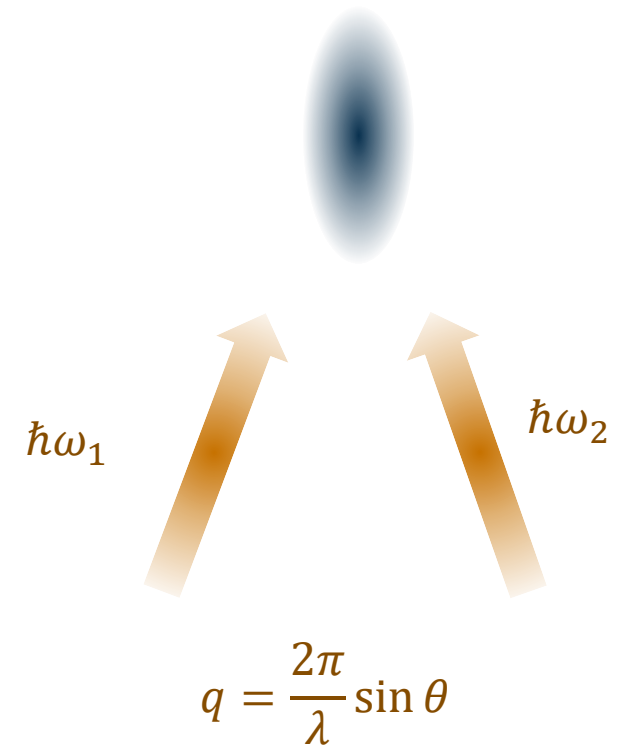
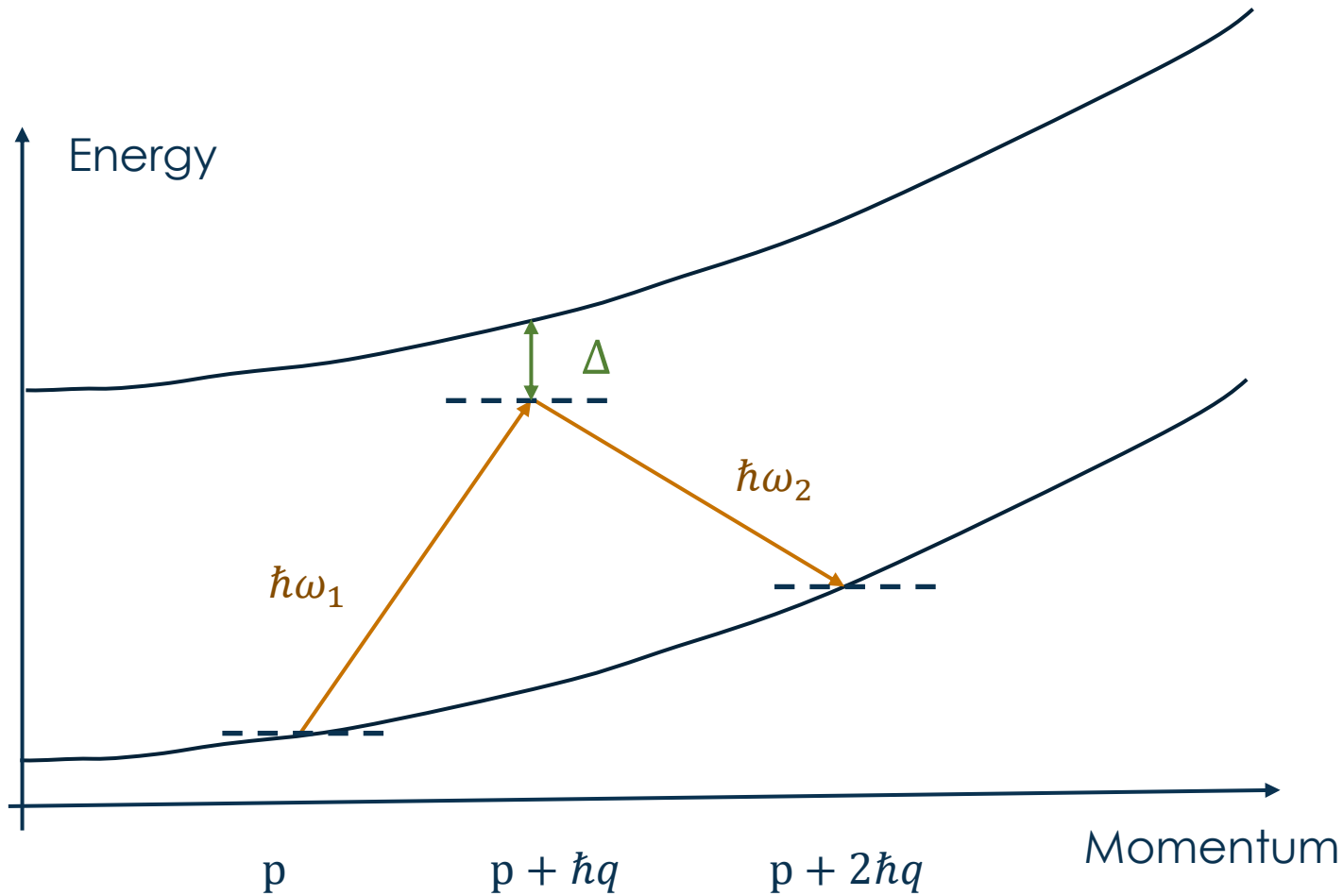
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Supplement : Bragg diffraction for atomic mirrors

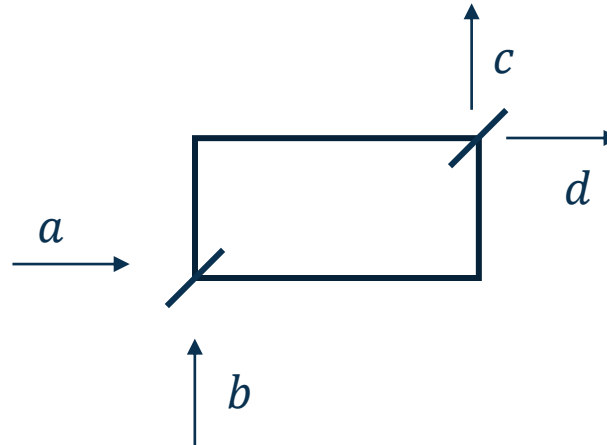


Supplement : checking the non-separability criteria

$$\langle \hat{n}_k \hat{n}_{-k} \rangle = \langle \hat{b}_k^\dagger \hat{b}_{-k}^\dagger \hat{b}_k \hat{b}_{-k} \rangle = n_k n_{-k} + |\langle \hat{b}_k \hat{b}_{-k} \rangle|^2 + |\langle \hat{b}_k^\dagger \hat{b}_{-k} \rangle|^2$$

if the state is separable : $\leq n_k n_{-k}$ $0 \text{ } ????$

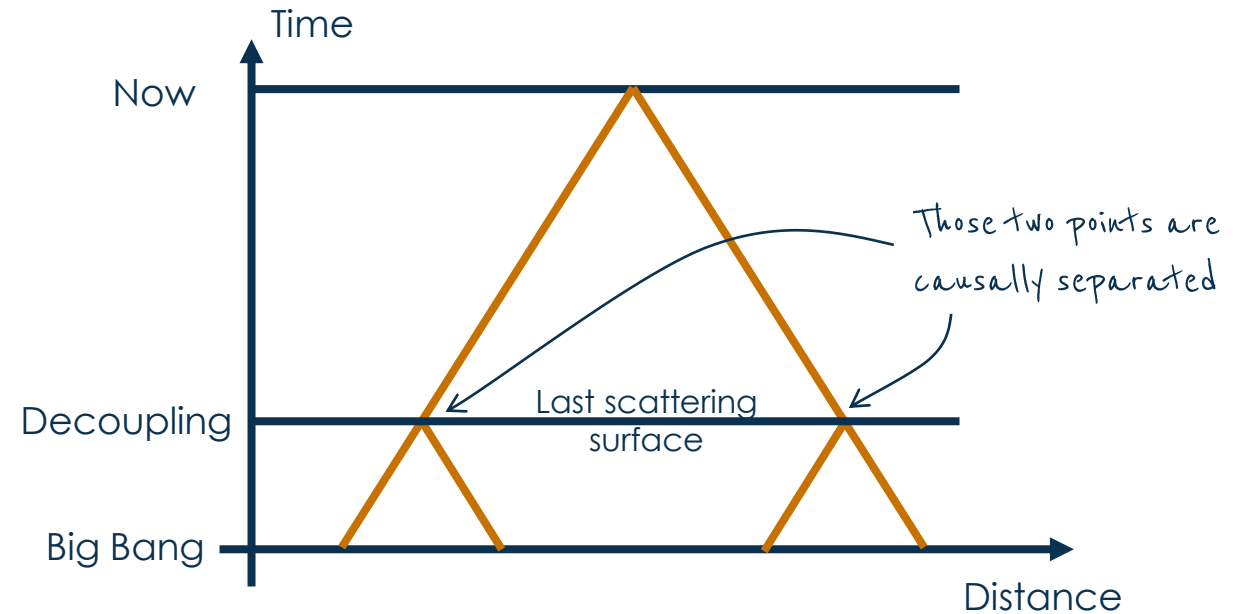
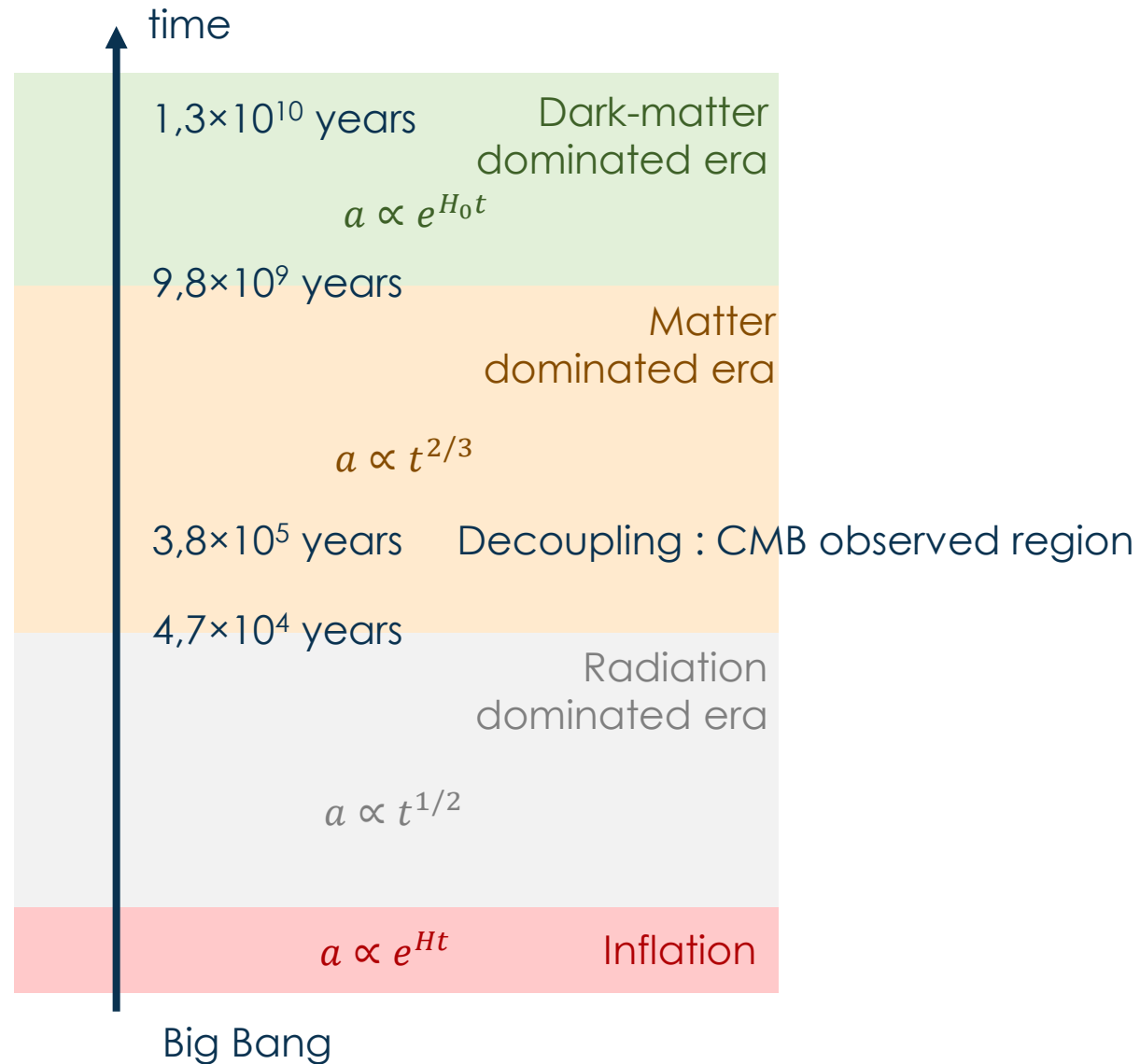
$$c = \cos(\phi) a + \sin(\phi) b$$



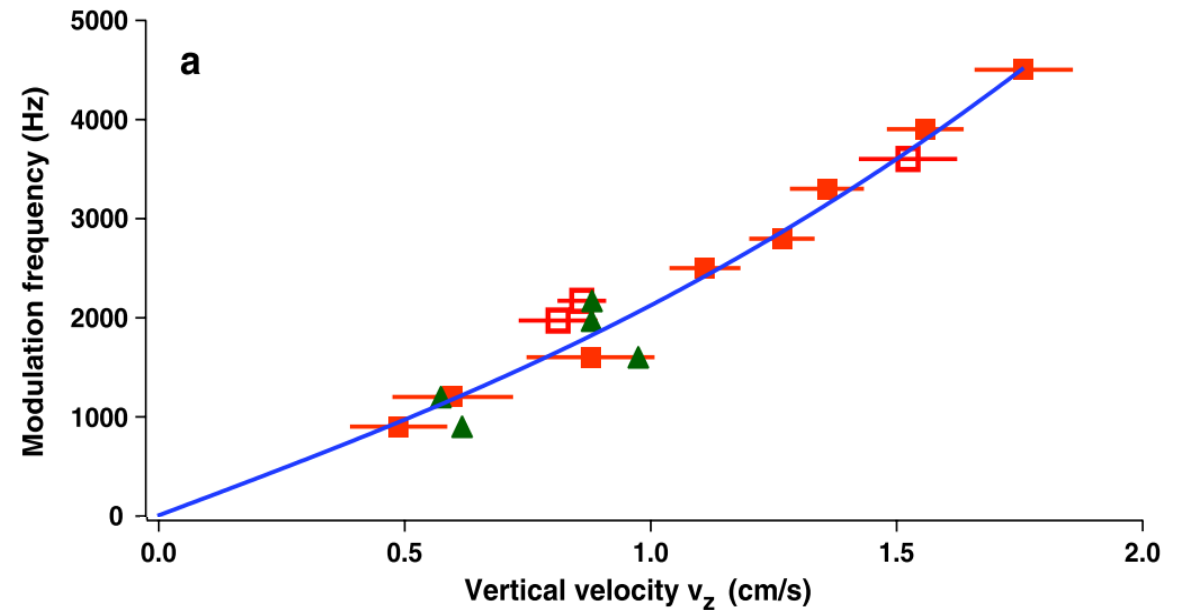
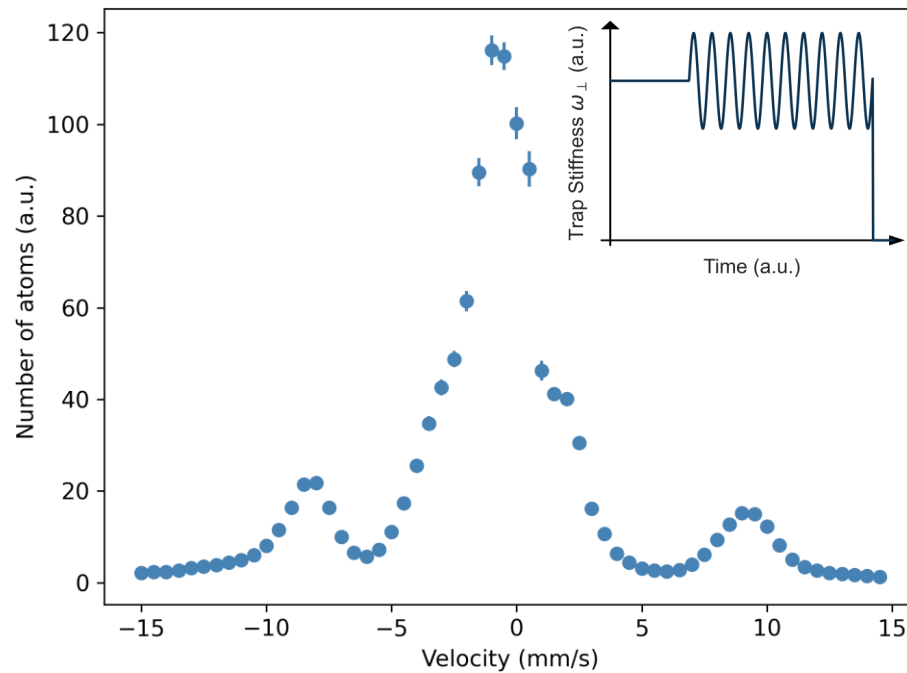
$$n_c = \langle c^\dagger c \rangle = \cos(\phi)^2 a^\dagger a + \sin(\phi)^2 b^\dagger b + \cos \phi \sin \phi (a^\dagger b + b^\dagger a)$$

→ Check that this term is zero.

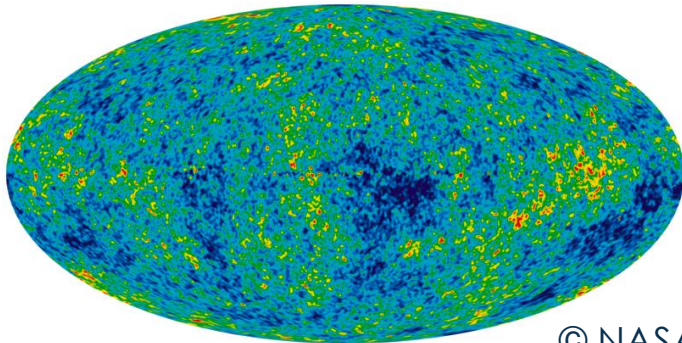
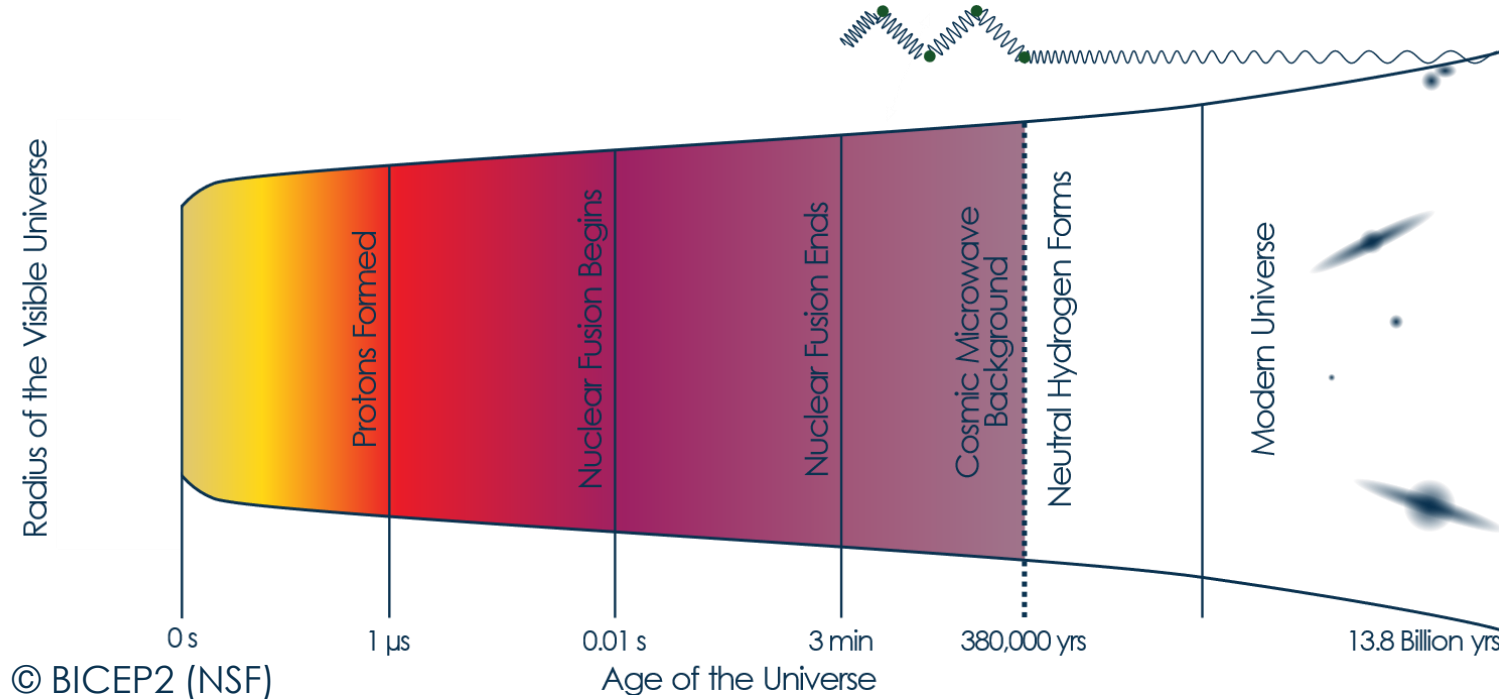
Supplement : inflation scenario



Supplement : excitation spectrum of quasi-particles



The Standard Model



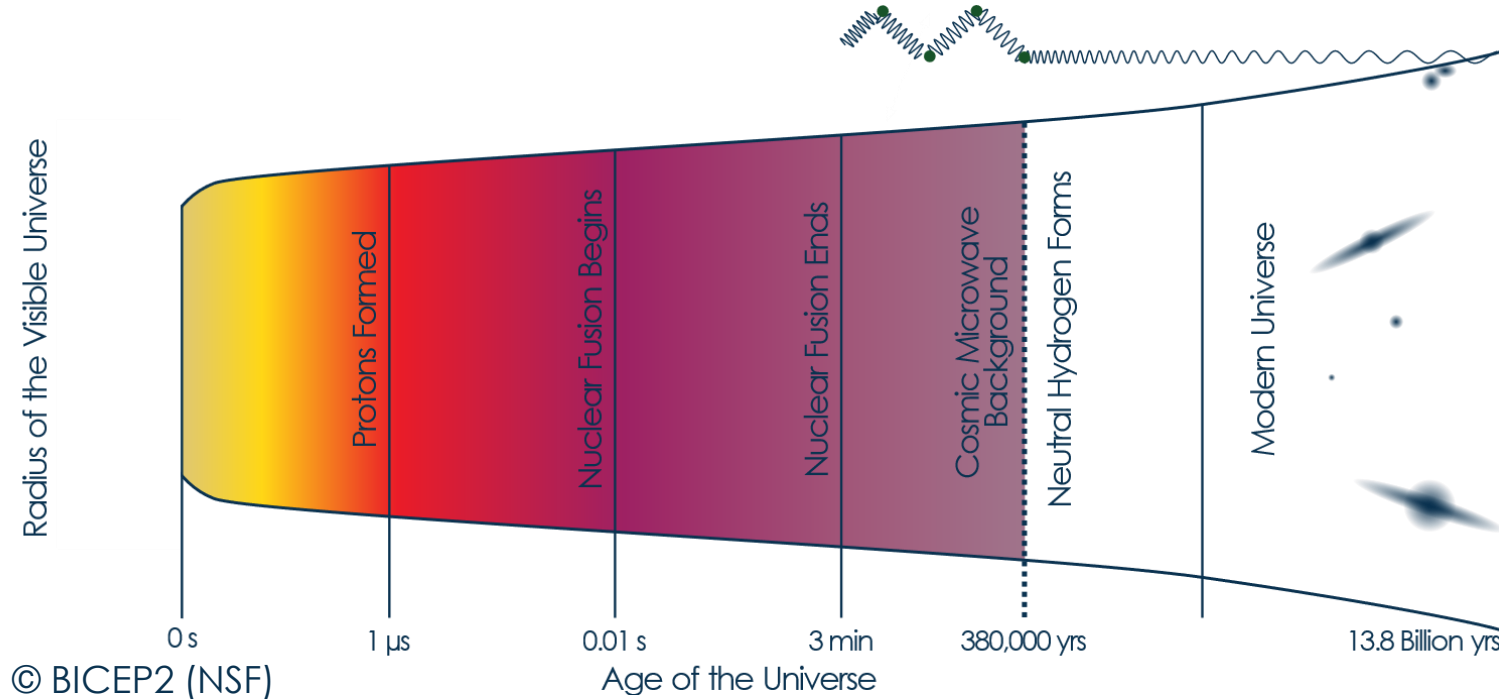
© NASA

Cosmic microwave background at 2.7254 (6) K.

Successes of the Standard Model of Cosmology

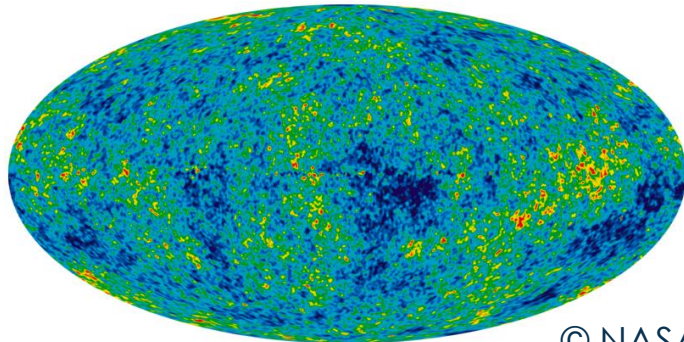
- ✔ Successful account for nucleosynthesis and the relative abundance of light elements,
- ✔ Predicts the fact that universe is expanding (Hubble law)
- ✔ Right prediction of the Cosmic Background Radiation temperature

The Standard Model



Failures of the Standard Model of Cosmology

- 👎 The horizon problem
- 👎 The flatness problem
- 👎 ...

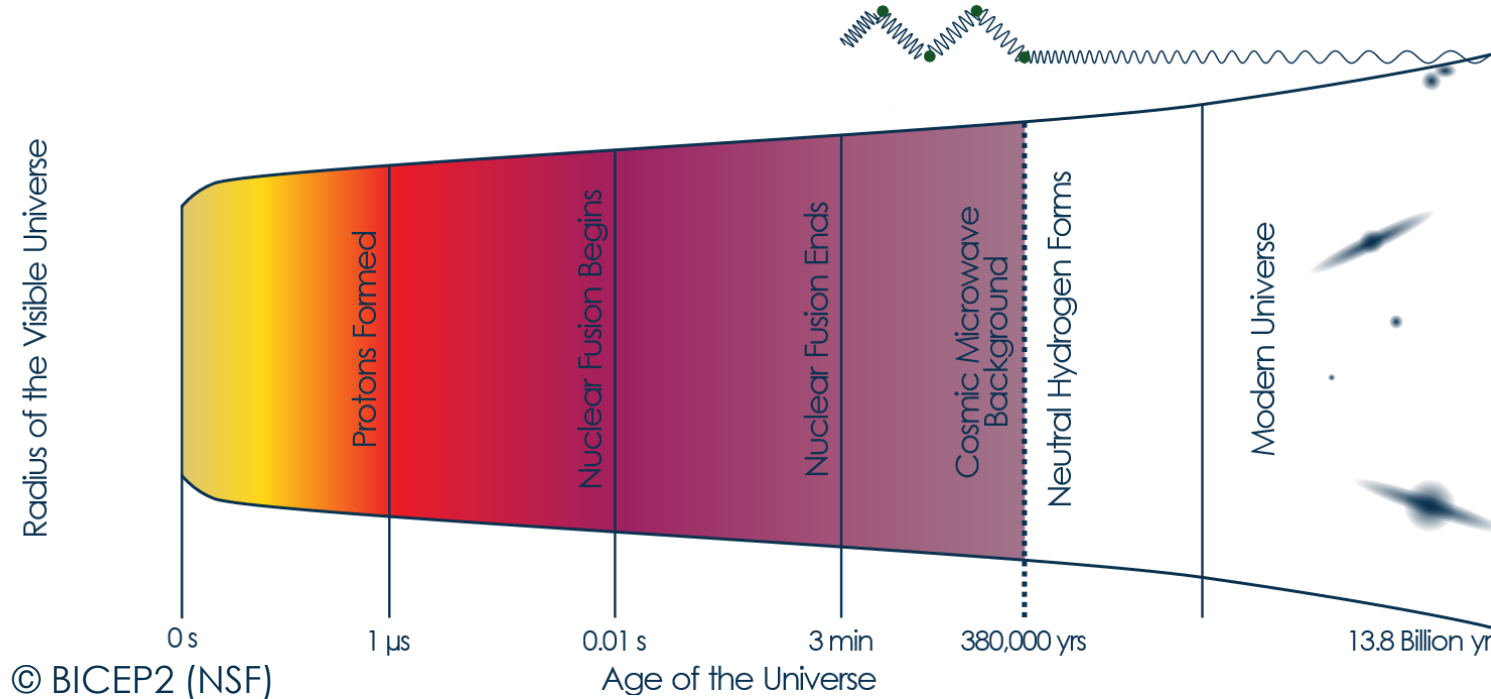


Cosmic microwave background at 2.7254 (6) K.

Horizon problem

Homogeneity of causally disconnected regions of space

The Standard Model



Failures of the Standard Model of Cosmology

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- 👎 ...

Flatness problem

Energy density

critical energy density

$$\frac{\rho}{\rho_c} = 1$$

REALLY equal to one

1,02 ± 0,02 now

Horizon problem

Homogeneity of causally disconnected regions of space

Detection of unique metastable helium atoms

He^*

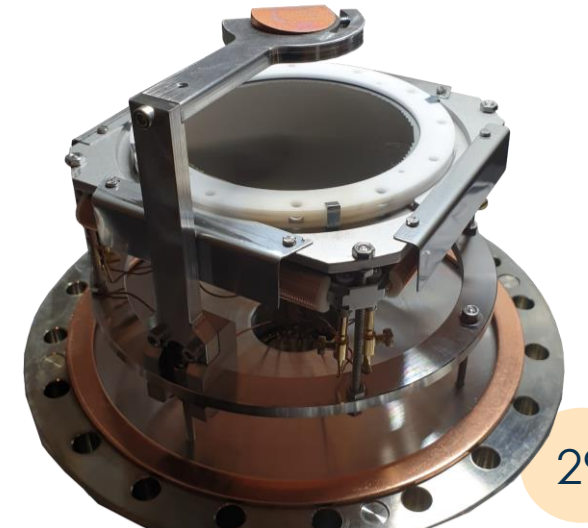
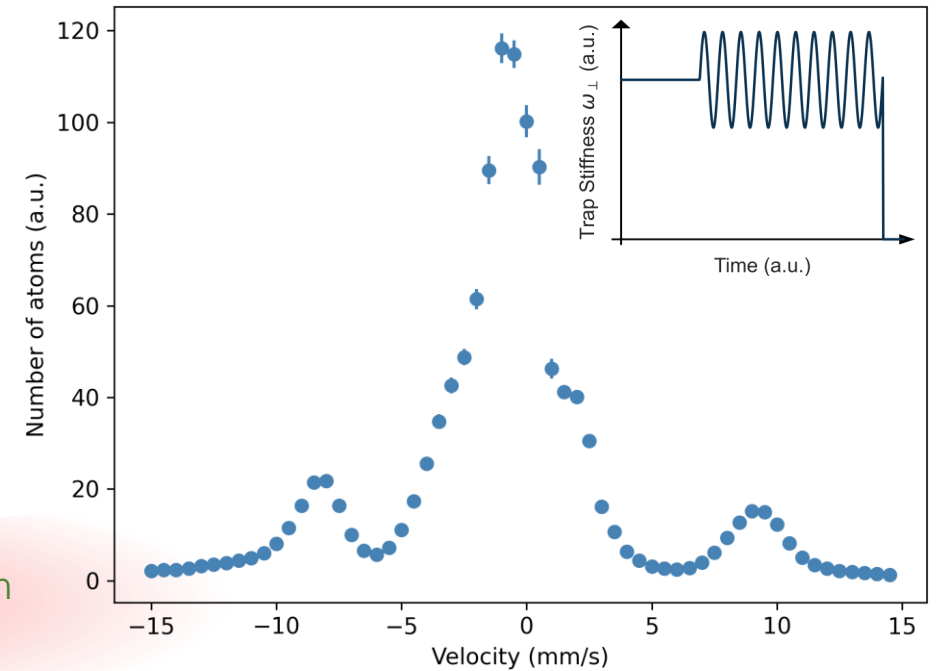
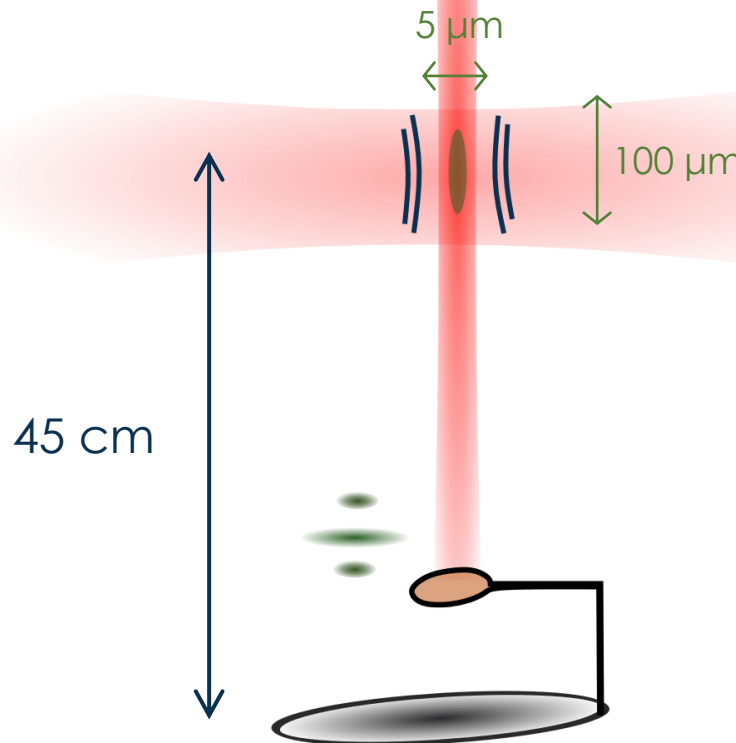


Metastable Helium 4

- Simple atomic structure
- No hyperfine structure
- Internal energy of 20 eV
- Recoil speed of 9 cm/s at 1083 nm

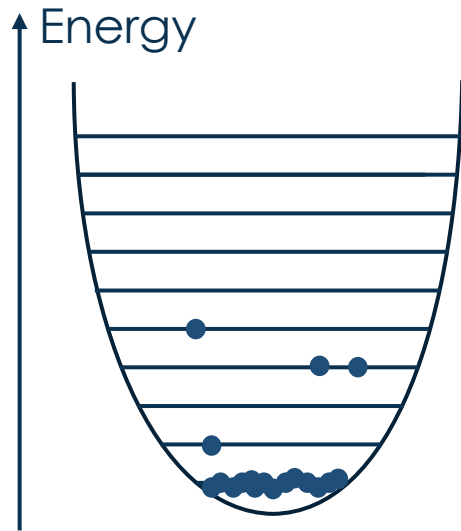
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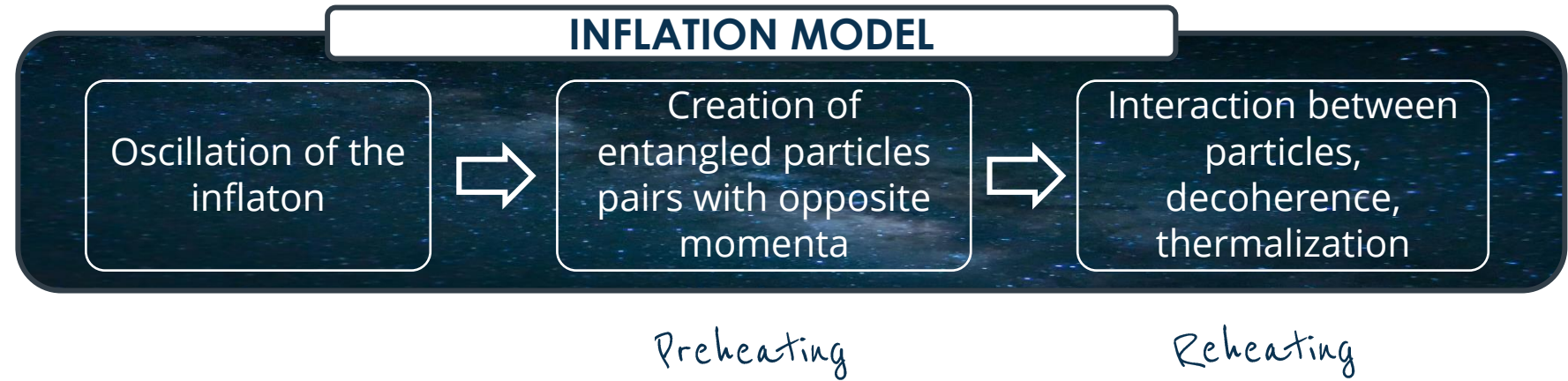
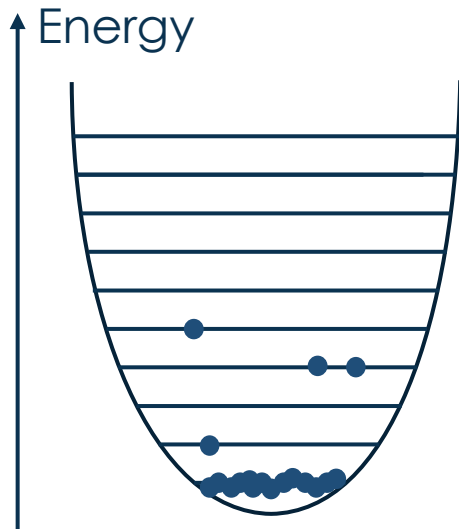
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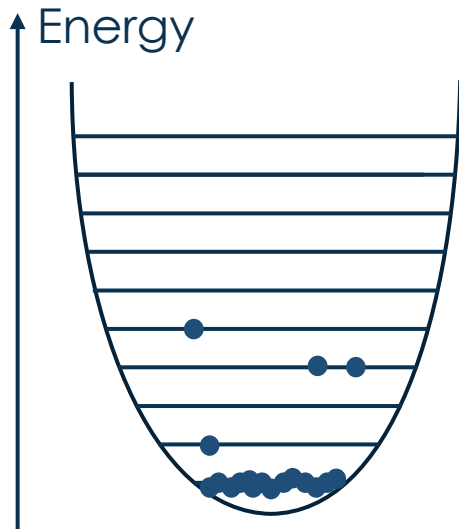
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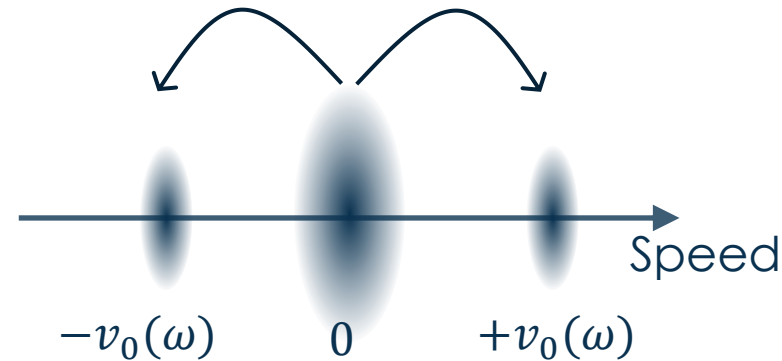
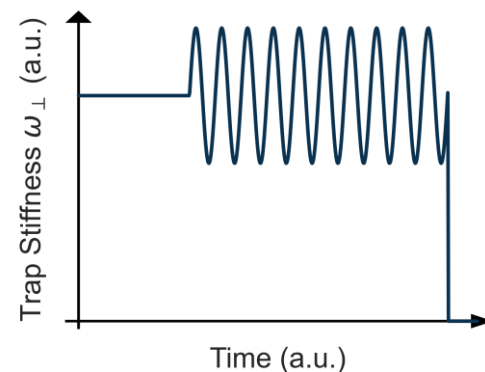
BEC for analog inflation

BEC is a macroscopic state at $k=0$



ω : excitation frequency

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X. Busch and R. Parentani, Phys. Rev. D **88**, 045023 (2013).
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INFLATION MODEL

Oscillation of the inflaton



Creation of entangled particles pairs with opposite momenta



Interaction between particles, decoherence, thermalization

Preheating

Reheating

LAB SIMULATION

Oscillation of the BEC density



Creation of entangled phonons pairs with opposite momenta



Interaction between phonons, decoherence, thermalization