

# **Formalizing Reliability in the Taxonomic Congruence Approach**

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## Supplementary material

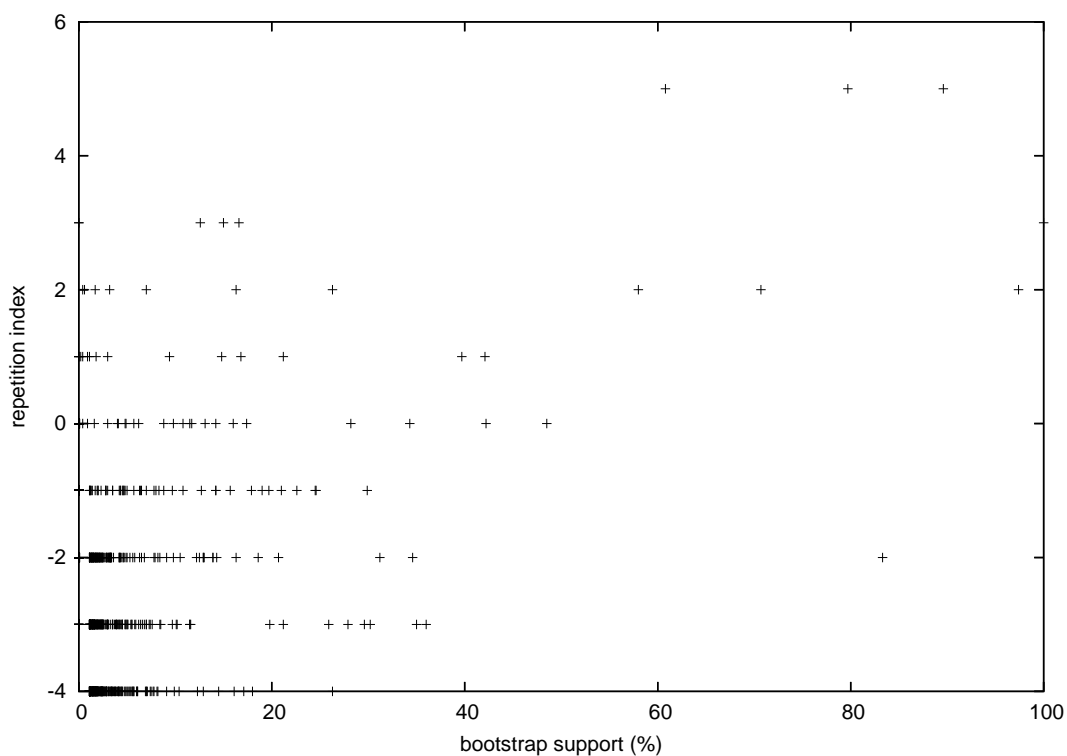


Figure 1: Repetition indices of the clades plotted against their bootstrap supports in the 'total evidence' analysis.

Table 1: Taxonomic sampling (in bold; sequences not present in Dettai, 2004 or in Dettai & Lecointre, 2005)

genus	28S	12S	16S	Rhodopsin	MLL	IRBP
<i>Ammodytes</i>	AY141689-92	AY141380	AY141450	AY141306	AY362234	<b>DQ309871</b>
<i>Antennarius</i>	AY372752-53	AY368287	AY368304	AY368324	AY362215	DQ168037
<i>Apletodon</i>	AY141557-60	AY141348	AY141418	AY141274	AY362213	DQ168039
<i>Arnoglossus</i>	AY141593-96	AY141358	AY141428	AY141283	AY362228	<b>DQ309872</b>
<i>Aulostomus</i>	AY141577-80	AY141353	AY141423	AY141279	AY362226	DQ168040

Table 1: Continued

genus	28S	12S	16S	Rhodopsin	MLL	IRBP
<i>Barbourisia</i>	DQ021385, 93	AY368290	AF221881	AY368333	AY362264	DQ168041
<i>Bathypterois</i>	AY141473-76	AY141326	AY141396	AY141257	AY362219	DQ168042
<i>Bedotia</i>	AY141525-28	AY141339	AY141409	AY141267	AY362271	DQ168043
<i>Belone</i>	AY141529-32	AY141340	AY141410	AY141268	AY362273	DQ168044
<i>Beryx</i>	AY141513-16	AY141336	AY141406	AY141265	AY362238	DQ168045
<i>Bovichtus</i>	AY141661-64	Z32702	<b>AY520101</b>	AY141299	AY362283	DQ168046
<i>Callionymus</i>	AY141541-44	AY141344	AY141414	AY141270	AY362225	DQ168047
<i>Capros</i>	AY141501-04	AY141333	AY141403	AY141262	AY362233	DQ168048
<i>Ceratias</i>	AY141505-08	AY141334	AY141404	AY141263	AY362270	DQ168049
<i>Chaetodon</i>	AY372701-04	<b>AJ748314</b>	AF055613	AY368312	AY362240	DQ168050
<i>Channa</i>	AY141569-72	AY141351	AY141421	AY141277	AY362241	DQ168051
<i>Cheimarrichthys</i>	AY141693-96	AY141381	AY141451	AY141307	AY362229	DQ168052
<i>Chelidonicichthys</i>	AY141609-12	AY141362	AY141432	AY141287	AY362284	DQ168053
<i>Chloroscombrus</i>	AY141717-20	AY141387	AY141457	AY141313	AY362223	DQ168054
<i>Citharus</i>	AY372697-00	AF542220	AY157325	AY141323	AY362232	DQ168055
<i>Ctenochaetus</i>	AY141745-48	AY141394	AY141464	AY141320	AY362242	DQ168057
<i>Ctenopoma</i>	AY141573-76	AY141352	<b>AY662702</b>	AY141278	AY362210	DQ168058
<i>Cyclopterus</i>	AY372737-38	AY368284	AY368299	AY368316	AY362218	<b>DQ309873</b>
<i>Dactylopterus</i>	AY141589-92	AY141357	AY141427	AY141282	AY362243	DQ168059
<i>Echeneis</i>	AY141725-28	AY141389	AY141459	AY141315	AY362245	DQ168062
<i>Epinephelus</i>	AY141629-32	AY141367	AY141437	AY141291	AY362227	DQ168064
<i>Forsterygion</i>	AY141549-52	AY141346	AY141416	AY141272	AY362276	DQ168065
<i>Gymnocephalus</i>	AY141649-52	AY141373	AY141443	AY141296	AY362278	DQ168068
<i>Halobatrachus</i>	AY372743-44	AY368286	AY368308	AY368323	AY362246	DQ168069

Table 1: Continued

genus	28S	12S	16S	Rhodopsin	MLL	IRBP
<i>Holacanthus</i>	AY141753-56	AF055593	AF055614	AY141322	AY362214	DQ168072
<i>Holanthias</i>	AY141625-28	AY141366	AY141436	AY141290	AY362209	DQ168073
<i>Kali</i>	AY141697-00	AY141382	AY141452	AY141308	AY362224	DQ168074
<i>Labrus</i>	AY141737-40	<b>AF414201</b>	AY141462	AY141318	AY362222	DQ168075
<i>Lagocephalus</i>	AY141601-04	AY141360	AY141430	AY141285	AY362221	DQ168076
<i>Lateolabrax</i>	AY141633-36	AY141369	AY141439	AY141293	AY362253	DQ168078
<i>Lepadogaster</i>	AY141553-56	AY141347	AY141417	AY141273	AY362247	DQ168080
<i>Liza</i>	AY141521-24	AY141338	AY141408	AY141266	AY362248	DQ168082
<i>Macroramphosus</i>	AY141581-84	AY141354	AY141424	AY141280	AY362206	DQ168083
<i>Mastacembelus</i>	AY141561-64	AY141349	AY141419	AY141275	AY362249	DQ168084
<i>Mene</i>	AY141729-32	AY141390	AY141460	AY141316	AY362250	DQ168085
<i>Microchirus</i>	AY141597-00	AY141359	AY141429	AY141284	AY362275	DQ168086
<i>Mola</i>	AY141605-08	AY141361	AY141431	AY141286	AY362251	DQ168087
<i>Monopterus</i>	AY141565-68	AY141350	AY141420	AY141276	AY362252	DQ168088
<i>Mullus</i>	AY372719-21	AY368277	AF227680	Y18666	AY362231	DQ168090
<i>Myripristis</i>	AY141517-20	AY141337	AY141407	U57539	AY362265	DQ168091
<i>Notothenia</i>	AY141673-76	Z32712	Z32731	AY141302	AY362282	DQ168093
<i>Ostracion</i>	AY372722-23	AY368281	AF137213	AF137213	AY362207	DQ168095
<i>Pampus</i>	AY141701-04	AY141383	AY141453	AY141309	AY362220	DQ168096
<i>Parablennius</i>	AY141545-48	AY141345	AY141415	AY141271	AY362255	DQ168097
<i>Pentanemus</i>	AY141733-36	AY141391	AY141461	AY141317	AY362272	DQ168098
<i>Perca</i>	AY141645-48	AY141372	AY141442	AY141295	AY362279	DQ168099
<i>Pholis</i>	AY141657-60	AY141375	<b>AF420459</b>	AY141298	AY362285	DQ168100
<i>Poecilia</i>	AY141533-36	AY141342	<b>U80051</b>	AY141269	AY362203	DQ168102

Table 1: Continued

genus	28S	12S	16S	Rhodopsin	MLL	IRBP
<i>Pogonoperca</i>	AY372711-14	AY141368	<b>AF297322</b>	AY141292	AY362256	DQ168103
<i>Polymixia</i>	AY372724-26	AF049730	AF049740	AY368320	AY362208	DQ168104
<i>Pomadasy</i>	DQ021392	AY368293	AY368298	DQ021404	AY363643	AY362230
<i>Psenopsis</i>	AY141705-08	AY141384	AY141454	AY141310	AY362269	DQ168107
<i>Psettodes</i>	AY372717-18	AY368282	AY368302	AY368332	AY362259	DQ168108
<i>Regalecus</i>	AY372729-30	AY368292	AY368296	AY368328	AY362266	DQ168109
<i>Rypticus</i>	DQ021391	AY368295	<b>AF297327</b>	AY368329	AY362257	DQ168111
<i>Scarus</i>	AY141741-44	AY141393	AY141463	AY141319	AY362212	DQ168112
<i>Scomber</i>	AY141709-12	AY141385	<b>AB032521</b>	AY141311	AY362237	DQ168113
<i>Scorpaena</i>	AY141617-20	AY141364	AY141434	AY141288	AY362236	DQ168114
<i>Serranus</i>	AY141621-24	AY141365	AY141435	AY141289	AY362202	DQ168115
<i>Sphyraena</i>	AY141713-16	AY141386	AY141456	AY141312	AY362254	DQ168118
<i>Taurulus</i>	AH011857	AY141363	AY141433	U97275	AY362217	DQ168121
<i>Trachinotus</i>	AY141721-24	AY141388	AY141458	AY141314	AY362263	DQ168120
<i>Trachinus</i>	AY141681-84	AY141378	AY141448	AY141304	AY362277	DQ168123
<i>Trachyrincus</i>	AY372708-10	AY368280	AY368301	AY368318	AY362289	DQ168124
<i>Triacanthodes</i>	DQ021383, 96	AY368289	AY368311	AY368331	AY362258	DQ168125
<i>Uranoscopus</i>	AY141685-88	AY141379	AY141449	AY141305	AY362239	DQ168126
<i>Zenopsis</i>	AY372748-50	AY368278	AY368300	AY368314	AY362286	DQ168127
<i>Zeus</i>	AY141493-96	AY141331	AY141401	Y14484	AY362287	DQ168128

## Why two clades with the same repetition index, same number of occurrences and contradicting one another should not have a high repetition index?

Let  $\alpha$  and  $\beta$  be two clades that have the same repetition index  $R$  and the same number of occurrences  $M$ , and that contradict one another.

Let's also assume that each clade has a stable best contradictor.

If  $\beta$  is the best contradictor of  $\alpha$ , then their repetition index is 0.

Is it possible that  $\alpha$  and  $\beta$  have a strictly positive repetition index?

Let  $r$  be the function that to a clade  $\gamma$  associates its final repetition index  $r(\gamma)$ .

Let  $O$  be the function that to a clade  $\gamma$  associates its maximum number of occurrences (or sum of supports) over independant analyses  $O(\gamma)$ .

Let  $C$  be the function that to a clade  $\gamma$  associates its best contradictor  $C(\gamma)$ .

$$r(\gamma) = O(\gamma) - O(C(\gamma))$$

Let  $C_i$  be the sequence of the clades such that  $C_0 = \alpha$  and for  $i \geq 0$ :  $C_{i+1} = C(C_i)$ .

Let  $O_i$  be the sequence of the number of occurrences of the clades  $C_i$ . For  $i \geq 0$ :  $O_i = O(C_i)$ .

Let  $r_i$  be the sequence of the repetition indices of the clades  $C_i$ . For  $i \geq 0$ :  $r_i = r(C_i)$ .

$$C_0 = \alpha$$

$$O_0 = O(\alpha) = M$$

$$r_0 = r(\alpha) = R$$

Let us suppose (1):  $R > 0$ .

$\beta$  is one of the contradictors of  $\alpha$ , therefore  $r_1 \geq r(\beta) = R$ .

If  $r_1 = R$ , then  $O_1 \geq O(\beta) = M$ .

Then  $R = r_0 = O_0 - O_1 \leq M - M = 0$ : impossible because (1).

Therefore (2):  $r_1 > R$ .

$r_0 = O_0 - O_1$ , therefore  $O_1 = O_0 - r_0 = M - R$ .

$\alpha$  is one of the contradictors of  $C_1$ , therefore  $r_2 \geq r(\alpha) = R$ .

If  $r_2 = R$ , then  $O_2 \geq O(\alpha) = M$ .

Now  $O_1 = M - R$  and  $r_1 = O_1 - O_2$ .

Therefore  $r_1 = O_1 - O_2 \leq M - R - M = -R$ : impossible because (1) and (2).

Therefore  $r_2 > R$ .

$r_1 = O_1 - O_2$ , therefore  $O_2 = O_1 - r_1 = M - R - r_1 < M - 2R$ .

Property  $P_i$ :  $r_i > r_{i-2} \geq R$  and  $O_i < M - iR$ .

Let us try to demonstrate  $P_i$ , for  $i \geq 2$ .

$P_2$  is true:  $r_2 > R = r_0$  and  $O_2 < M - 2R$ .

Let  $j$  be an interger such that  $j > 2$ .

Let us suppose that  $P_i$  is true for each integer  $i$  such that  $2 \leq i < j$ .

$C_{j-2}$  is a contradictor of  $C_{j-1}$ , therefore  $r_j \geq r_{j-2}$ .

If  $r_j = r_{j-2}$ , then  $O_j \geq O_{j-2}$ .

Then  $r_{j-1} = O_{j-1} - O_j \leq O_{j-1} - O_{j-2}$ .

Now  $O_{j-1} - O_{j-2} = -r_{j-2}$  and  $r_{j-2} > R$  (from (2) if  $j = 3$ , or from  $P_{j-2}$ ).

Therefore  $r_{j-1} < -r_{j-2} < -R$ : impossible because  $r_{j-1} > R$  (from  $P_{j-1}$ ).

Therefore  $r_j > r_{j-2} \geq R$ .

$r_{j-1} = O_{j-1} - O_j$ , therefore  $O_j = O_{j-1} - r_{j-1}$ .

Now  $O_{j-1} < M - (j - 1)R$  and  $r_{j-1} > R$  (from  $P_{j-1}$ ).

Therefore  $O_j < M - (j - 1)R - R = M - jR$ :  $P_j$  is true.

$P_2$  is true, therefore  $P_i$  is true for every integer  $i$  such that  $i \geq 2$ .

For  $i$  an integer such that  $i > M/R$ ,  $O_i < 0$  (from  $P_i$ ).

However, by definition,  $O_i \geq 0$  for every value of  $i$ .

Therefore (1) cannot be true:

Two clades with the same repetition index and the same number of occurrences that contradict one another cannot have a strictly positive repetition index (in the case where all clades have a stable best contradictor).

If the repetition index is an average, it's more difficult to see if  $\alpha$  and  $\beta$  have a low repetition index.

## References

Dettaï, A. (2004), *La phylogénie des Acanthomorpha (Teleostei) inférée par l'étude de la congruence taxinomique*. Ph.D. thesis, Université Paris VI Pierre et Marie Curie.

Dettaï, A. & Lecointre, G. (2005), Further support for the clades obtained by multiple molecular phylogenies in the acanthomorph bush. *Comptes Rendus Biologies*, 328, 674–689.